

A group is a set G (finite or infinite) with a binary operation $.$ such that the operation is

1. Closed within G ($a.b$ belongs to G)
2. Associative ($a.b).c = a.(b.c)$)
3. A unique identity element e exist such that $a.e = e.a = a$
4. Every element ' a ' has unique inverse a^{-1} such that $a.a^{-1} = a^{-1}.a = e$ (a, b, c are elements of G)

A group that is commutative as well (with $a.b = b.a$) is Abelian Group.

Addition and multiplication over integers and real numbers are examples of infinite groups.

Addition of numbers (modulo some number) is example of finite group.

Order of group is number of elements within the group.

Order of an element within that group is the smallest power of that element which gives the identity element of that group.

Order of every element is always a divisor of the order of group.

A generator is an element of a group whose order is equal to the order of that group.

A cyclic group contains atleast one generator.

A group F is a subgroup of G if a subset of elements of G forms a group. (The identity element of G should belong to F , for every two elements of F the binary operation should be closed within F , every element within F should have its inverse within F itself).

The order of subgroup is always a divisor of the order of that group.

Two groups H and G are isomorphic (similar) to each other if for every pair of elements we have that $f(a.b) = f(a).f(b)$, where $f(x)$ is some function that maps the elements of G to H . Some such function $f(x)$ exists, note that two isomorphic groups should always have the same element order sequence (as two isomorphic graphs always have the same degree sequence).

For example, the group formed by using addition of integers over Z_6 is isomorphic to multiplication of non-zero integers over Z_7 , both are being cyclic with 6 elements, thus they need not be listed out twice at all. Also note that direct product of cyclic group of order m with cyclic group of order n ($C_m \times C_n$) is isomorphic to that cyclic group of order $m \times n$ ($C_{m \times n}$) if in any case that m, n are being co-prime numbers. Again, note that $D_{10} \times C_2$ is rather isomorphic to D_{20} , and so is that group D_{28} being isomorphic to $D_{14} \times C_2$.

Let's examine the structure of all distinct (non-isomorphic) groups that are being possible upto order of 31 elements.

For finite groups with prime number of elements, only the trivial cyclic group is possible (that is formed by addition modulo that prime number of elements). All such cyclic groups that are formed are Abelian as well.

When the order of group is less than 16, the cycle graph uniquely determines the group. In this case, two non-isomorphic groups of the same order (less than 16) have different cycle graphs. The order of the smallest group which is not isomorphic with another group of the same order, but have the same cycle graph is 16. In this case, since one of such groups is Abelian, and then the other is non-Abelian, thus we can immediately say that they are, of course, not isomorphic to each other at all.

A normal subgroup N of group G is a subgroup of G such that for every element n in N , and for every element g in G , gng^{-1} belongs to N . A group for which every subgroup is normal is known as Hamiltonian Group. The Quaternion Group of order 8 is the smallest group that is not Abelian, though every subgroup of it is normal.

Order 2 (1 group)

	0	1
0	0	1
1	1	0

Cycle graph

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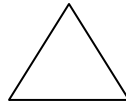
C_2 , cyclic, identity element $e = 0$, element $x = 1$, $x^2 = e$

Element	0	1
Order	1	2

Order 3 (1 group)

	0	1	2
0	0	1	2
1	1	2	0
2	2	0	1

Cycle graph



C_3 , cyclic, identity element $e = 0$, element $x = 1$, $x^2 = 2$, $x^3 = e$

Element	0	1	2
Order	1	3	3

Order 4 (2 groups)

	0	1	2	3
0	0	1	2	3
1	1	2	3	0
2	2	3	0	1
3	3	0	1	2

Cycle graph

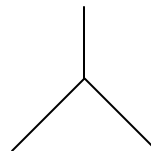


C_4 , cyclic, identity element $e = 0$, element $x = 1$, $x^2 = 2$, $x^3 = 3$, $x^4 = e$

Element	0	1	2	3
Order	1	4	2	4

	0	1	2	3
0	0	1	2	3
1	1	0	3	2
2	2	3	0	1
3	3	2	1	0

Cycle graph



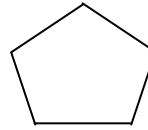
$C_2 \times C_2$, abelian, identity element $e = 0$, Klein 4 group, $a^2 = e$, $b^2 = e$

	e	a	b	ab
Element	0	1	2	3
Order	1	2	2	2

Order 5 (1 group)

	0	1	2	3	4
0	0	1	2	3	4
1	1	2	3	4	0
2	2	3	4	0	1
3	3	4	0	1	2
4	4	0	1	2	3

Cycle graph



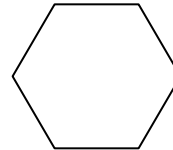
C_5 , cyclic, identity element $e = 0$, $a^5 = e$

	e	a	a^2	a^3	a^4
Element	0	1	2	3	4
Order	1	5	5	5	5

Order 6 (2 groups)

	0	1	2	3	4	5
0	0	1	2	3	4	5
1	1	2	3	4	5	0
2	2	3	4	5	0	1
3	3	4	5	0	1	2
4	4	5	0	1	2	3
5	5	0	1	2	3	4

Cycle graph

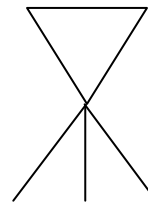


C_6 , cyclic, identity element $e = 0$, $a^6 = e$

	e	a	a^2	a^3	a^4	a^5
Element	0	1	2	3	4	5
Order	1	6	3	2	3	6

	0	1	2	3	4	5
0	0	1	2	3	4	5
1	1	0	5	4	3	2
2	2	4	0	5	1	3
3	3	5	4	0	2	1
4	4	2	3	1	5	0
5	5	3	1	2	0	4

Cycle graph



D_6 , dihedral, identity element $e = 0$, $a^3 = e$, $b^2 = e$, $ba = a^{-1}b$

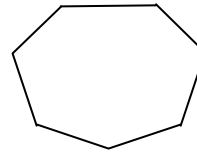
This group is isomorphic to S_3 , the symmetry group that is being formed by using permutations upon three elements. For $n > 3$, however notice that S_n is never being isomorphic to that group D_{2n} at all.

	e	ab	a^2b	b	a	a^2
Element	0	1	2	3	4	5
Order	1	2	2	2	3	3

Order 7 (1 group)

	0	1	2	3	4	5	6
0	0	1	2	3	4	5	6
1	1	2	3	4	5	6	0
2	2	3	4	5	6	0	1
3	3	4	5	6	0	1	2
4	4	5	6	0	1	2	3
5	5	6	0	1	2	3	4
6	6	0	1	2	3	4	5

Cycle graph



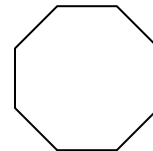
C_7 , cyclic, identity element $e = 0$, $a^7 = e$

	e	a	a^2	a^3	a^4	a^5	a^6
Element	0	1	2	3	4	5	6
Order	1	7	7	7	7	7	7

Order 8 (5 groups)

	0	1	2	3	4	5	6	7
0	0	1	2	3	4	5	6	7
1	1	2	3	4	5	6	7	0
2	2	3	4	5	6	7	0	1
3	3	4	5	6	7	0	1	2
4	4	5	6	7	0	1	2	3
5	5	6	7	0	1	2	3	4
6	6	7	0	1	2	3	4	5
7	7	0	1	2	3	4	5	6

Cycle graph

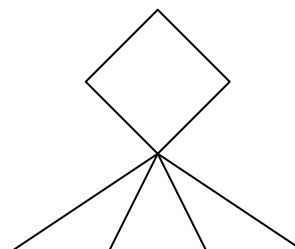


C_8 , cyclic, identity element $e = 0$, $a^8 = e$

	e	a	a^2	a^3	a^4	a^5	a^6	a^7
Element	0	1	2	3	4	5	6	7
Order	1	8	4	8	2	8	4	8

	0	1	2	3	4	5	6	7
0	0	1	2	3	4	5	6	7
1	1	2	3	0	5	6	7	4
2	2	3	0	1	6	7	4	5
3	3	0	1	2	7	4	5	6
4	4	7	6	5	0	3	2	1
5	5	4	7	6	1	0	3	2
6	6	5	4	7	2	1	0	3
7	7	6	5	4	3	2	1	0

Cycle graph

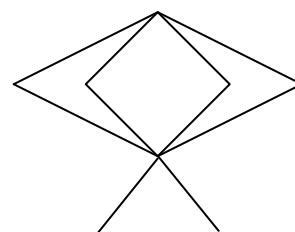


D_8 , dihedral, nilpotent, identity element $e = 0$, $a^4 = e$, $b^2 = e$, $ba = a^{-1}b$

	e	a	a^2	a^3	b	ab	a^2b	a^3b
Element	0	1	2	3	4	5	6	7
Order	1	4	2	4	2	2	2	2

	0	1	2	3	4	5	6	7
0	0	1	2	3	4	5	6	7
1	1	2	3	0	5	6	7	4
2	2	3	0	1	6	7	4	5
3	3	0	1	2	7	4	5	6
4	4	5	6	7	0	1	2	3
5	5	6	7	4	1	2	3	0
6	6	7	4	5	2	3	0	1
7	7	4	5	6	3	0	1	2

Cycle graph

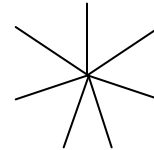


$C_2 \times C_4$, abelian, identity element $e = 0$, $a^4 = e$, $b^2 = e$, $ba = ab$

	e	a	a^2	a^3	b	ab	a^2b	a^3b
Element	0	1	2	3	4	5	6	7
Order	1	4	2	4	2	4	2	4

	0	1	2	3	4	5	6	7
0	0	1	2	3	4	5	6	7
1	1	0	3	2	5	4	7	6
2	2	3	0	1	6	7	4	5
3	3	2	1	0	7	6	5	4
4	4	5	6	7	0	1	2	3
5	5	4	7	6	1	0	3	2
6	6	7	4	5	2	3	0	1
7	7	6	5	4	3	2	1	0

Cycle graph

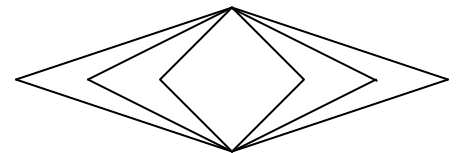


C_2^3 , abelian, identity element $e = 0$, $a^2 = e$, $b^2 = e$, $c^2 = e$, $ab = ba$, $bc = cb$, $ac = ca$

	e	a	b	ab	c	ac	bc	abc
Element	0	1	2	3	4	5	6	7
Order	1	2	2	2	2	2	2	2

	0	1	2	3	4	5	6	7
0	0	1	2	3	4	5	6	7
1	1	2	3	0	5	6	7	4
2	2	3	0	1	6	7	4	5
3	3	0	1	2	7	4	5	6
4	4	7	6	5	2	1	0	3
5	5	4	7	6	3	2	1	0
6	6	5	4	7	0	3	2	1
7	7	6	5	4	1	0	3	2

Cycle graph



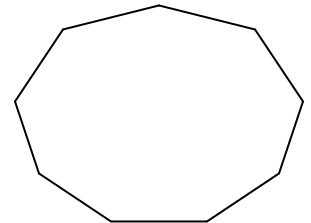
Q_8 , nilpotent, dicyclic group, Quaternion Group, identity element $e = 0$, $a^4 = e$, $b^2 = a^2$, $ba = a^{-1}b$

	e	a	a^2	a^3	b	ab	a^2b	a^3b
Element	0	1	2	3	4	5	6	7
Order	1	4	2	4	4	4	4	4

Order 9 (2 groups)

	0	1	2	3	4	5	6	7	8
0	0	1	2	3	4	5	6	7	8
1	1	2	3	4	5	6	7	8	0
2	2	3	4	5	6	7	8	0	1
3	3	4	5	6	7	8	0	1	2
4	4	5	6	7	8	0	1	2	3
5	5	6	7	8	0	1	2	3	4
6	6	7	8	0	1	2	3	4	5
7	7	8	0	1	2	3	4	5	6
8	8	0	1	2	3	4	5	6	7

Cycle graph

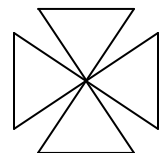


C_9 , cyclic, identity element $e = 0$, $a^9 = e$

	e	a	a^2	a^3	a^4	a^5	a^6	a^7	a^8
Element	0	1	2	3	4	5	6	7	8
Order	1	9	9	3	9	9	3	9	9

	0	1	2	3	4	5	6	7	8
0	0	1	2	3	4	5	6	7	8
1	1	2	0	4	5	3	7	8	6
2	2	0	1	5	3	4	8	6	7
3	3	4	5	6	7	8	0	1	2
4	4	5	3	7	8	6	1	2	0
5	5	3	4	8	6	7	2	0	1
6	6	7	8	0	1	2	3	4	5
7	7	8	6	1	2	0	4	5	3
8	8	6	7	2	0	1	5	3	4

Cycle graph



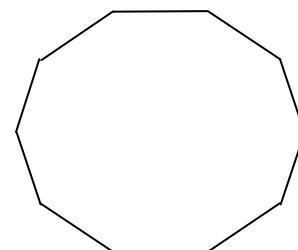
$C_3 \times C_3$, abelian, identity element $e = 0$, $a^3 = e$, $b^3 = e$, $ba = ab$

	e	a	a^2	b	ab	a^2b	b^2	ab^2	a^2b^2
Element	0	1	2	3	4	5	6	7	8
Order	1	3	3	3	3	3	3	3	3

Order 10 (2 groups)

	0	1	2	3	4	5	6	7	8	9
0	0	1	2	3	4	5	6	7	8	9
1	1	2	3	4	5	6	7	8	9	0
2	2	3	4	5	6	7	8	9	0	1
3	3	4	5	6	7	8	9	0	1	2
4	4	5	6	7	8	9	0	1	2	3
5	5	6	7	8	9	0	1	2	3	4
6	6	7	8	9	0	1	2	3	4	5
7	7	8	9	0	1	2	3	4	5	6
8	8	9	0	1	2	3	4	5	6	7
9	9	0	1	2	3	4	5	6	7	8

Cycle graph

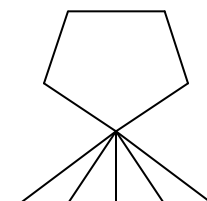


C_{10} , cyclic, identity element $e = 0$, $a^{10} = e$

	e	a	a ²	a ³	a ⁴	a ⁵	a ⁶	a ⁷	a ⁸	a ⁹
Element	0	1	2	3	4	5	6	7	8	9
Order	1	10	5	10	5	2	5	10	5	10

	0	1	2	3	4	5	6	7	8	9
0	0	1	2	3	4	5	6	7	8	9
1	1	2	3	4	0	6	7	8	9	5
2	2	3	4	0	1	7	8	9	5	6
3	3	4	0	1	2	8	9	5	6	7
4	4	0	1	2	3	9	5	6	7	8
5	5	9	8	7	6	0	4	3	2	1
6	6	5	9	8	7	1	0	4	3	2
7	7	6	5	9	8	2	1	0	4	3
8	8	7	6	5	9	3	2	1	0	4
9	9	8	7	6	5	4	3	2	1	0

Cycle graph



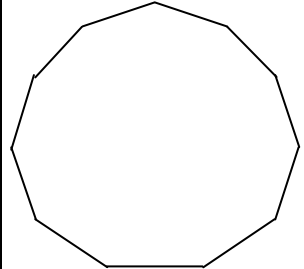
D_{10} , dihedral, identity element $e = 0$, $a^5 = e$, $b^2 = e$, $ba = a^{-1}b$

	e	a	a ²	a ³	a ⁴	b	ab	a ² b	a ³ b	a ⁴ b
Element	0	1	2	3	4	5	6	7	8	9
Order	1	5	5	5	5	2	2	2	2	2

Order 11 (1 group)

	0	1	2	3	4	5	6	7	8	9	10
0	0	1	2	3	4	5	6	7	8	9	10
1	1	2	3	4	5	6	7	8	9	10	0
2	2	3	4	5	6	7	8	9	10	0	1
3	3	4	5	6	7	8	9	10	0	1	2
4	4	5	6	7	8	9	10	0	1	2	3
5	5	6	7	8	9	10	0	1	2	3	4
6	6	7	8	9	10	0	1	2	3	4	5
7	7	8	9	10	0	1	2	3	4	5	6
8	8	9	10	0	1	2	3	4	5	6	7
9	9	10	0	1	2	3	4	5	6	7	8
10	10	0	1	2	3	4	5	6	7	8	9

Cycle graph



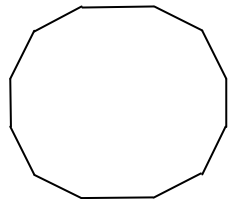
C_{11} , cyclic, identity element $e = 0$, $a^{11} = e$

	e	a	a ²	a ³	a ⁴	a ⁵	a ⁶	a ⁷	a ⁸	a ⁹	a ¹⁰
Element	0	1	2	3	4	5	6	7	8	9	10
Order	1	11	11	11	11	11	11	11	11	11	11

Order 12 (5 groups)

	0	1	2	3	4	5	6	7	8	9	10	11
0	0	1	2	3	4	5	6	7	8	9	10	11
1	1	2	3	4	5	6	7	8	9	10	11	0
2	2	3	4	5	6	7	8	9	10	11	0	1
3	3	4	5	6	7	8	9	10	11	0	1	2
4	4	5	6	7	8	9	10	11	0	1	2	3
5	5	6	7	8	9	10	11	0	1	2	3	4
6	6	7	8	9	10	11	0	1	2	3	4	5
7	7	8	9	10	11	0	1	2	3	4	5	6
8	8	9	10	11	0	1	2	3	4	5	6	7
9	9	10	11	0	1	2	3	4	5	6	7	8
10	10	11	0	1	2	3	4	5	6	7	8	9
11	11	0	1	2	3	4	5	6	7	8	9	10

Cycle graph



C_{12} , cyclic, identity element $e = 0$, $a^{12} = e$

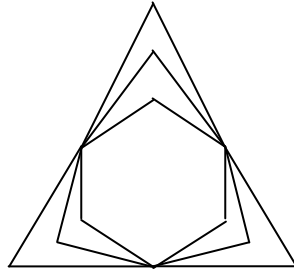
	e	a	a ²	a ³	a ⁴	a ⁵	a ⁶	a ⁷	a ⁸	a ⁹	a ¹⁰	a ¹¹
Element	0	1	2	3	4	5	6	7	8	9	10	11
Order	1	12	6	4	3	12	2	12	3	4	6	12

	0	1	2	3	4	5	6	7	8	9	10	11
0	0	1	2	3	4	5	6	7	8	9	10	11
1	1	2	3	4	5	0	7	8	9	10	11	6
2	2	3	4	5	0	1	8	9	10	11	6	7
3	3	4	5	0	1	2	9	10	11	6	7	8
4	4	5	0	1	2	3	10	11	6	7	8	9
5	5	0	1	2	3	4	11	6	7	8	9	10
6	6	7	8	9	10	11	0	1	2	3	4	5
7	7	8	9	10	11	6	1	2	3	4	5	0
8	8	9	10	11	6	7	2	3	4	5	0	1
9	9	10	11	6	7	8	3	4	5	0	1	2
10	10	11	6	7	8	9	4	5	0	1	2	3
11	11	6	7	8	9	10	5	0	1	2	3	4

$C_2 \times C_6$, $C_2^2 \times C_3$, abelian, identity element $e = 0$, $a^6 = e$, $b^2 = e$, $ba = ab$

	e	a	a ²	a ³	a ⁴	a ⁵	b	ab	a ² b	a ³ b	a ⁴ b	a ⁵ b
Element	0	1	2	3	4	5	6	7	8	9	10	11
Order	1	6	3	2	3	6	2	6	6	2	6	6

Cycle graph

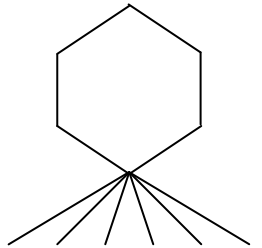


	0	1	2	3	4	5	6	7	8	9	10	11
0	0	1	2	3	4	5	6	7	8	9	10	11
1	1	2	3	4	5	0	7	8	9	10	11	6
2	2	3	4	5	0	1	8	9	10	11	6	7
3	3	4	5	0	1	2	9	10	11	6	7	8
4	4	5	0	1	2	3	10	11	6	7	8	9
5	5	0	1	2	3	4	11	6	7	8	9	10
6	6	11	10	9	8	7	0	5	4	3	2	1
7	7	6	11	10	9	8	1	0	5	4	3	2
8	8	7	6	11	10	9	2	1	0	5	4	3
9	9	8	7	6	11	10	3	2	1	0	5	4
10	10	9	8	7	6	11	4	3	2	1	0	5
11	11	10	9	8	7	6	5	4	3	2	1	0

D_{12} , dihedral, identity element $e = 0$, $a^6 = e$, $b^2 = e$, $ba = a^{-1}b$

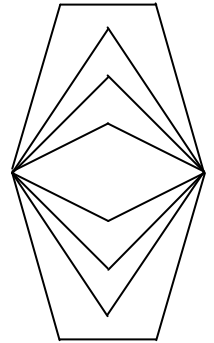
	e	a	a ²	a ³	a ⁴	a ⁵	b	ab	a ² b	a ³ b	a ⁴ b	a ⁵ b
Element	0	1	2	3	4	5	6	7	8	9	10	11
Order	1	6	3	2	3	6	2	2	2	2	2	2

Cycle graph



	0	1	2	3	4	5	6	7	8	9	10	11
0	0	1	2	3	4	5	6	7	8	9	10	11
1	1	2	3	0	5	6	7	4	9	10	11	8
2	2	3	0	1	6	7	4	5	10	11	8	9
3	3	0	1	2	7	4	5	6	11	8	9	10
4	4	9	6	11	8	1	10	3	0	5	2	7
5	5	10	7	8	9	2	11	0	1	6	3	4
6	6	11	4	9	10	3	8	1	2	7	0	5
7	7	8	5	10	11	0	9	2	3	4	1	6
8	8	5	10	7	0	9	2	11	4	1	6	3
9	9	6	11	4	1	10	3	8	5	2	7	0
10	10	7	8	5	2	11	0	9	6	3	4	1
11	11	4	9	6	3	8	1	10	7	0	5	2

Cycle graph

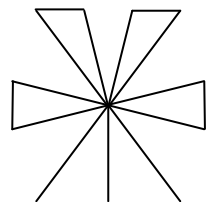


T_{12} , dicyclic group, formed by using semi-direct product of C_3 with C_4 , solvable, identity element $e = 0$, $a^4 = e$, $b^3 = e$, $ab = b^{-1}a$
Also formed with $e = 0$, $s^6 = e$, $s^3 = t^2$, $ts = s^{-1}t$

	e	a	a ²	a ³	b	ab	a ² b	a ³ b	b ²	ab ²	a ² b ²	a ³ b ²
Element	0	1	2	3	4	5	6	7	8	9	10	11
Order	1	4	2	4	3	4	6	4	3	4	6	4

	0	1	2	3	4	5	6	7	8	9	10	11
0	0	1	2	3	4	5	6	7	8	9	10	11
1	1	0	3	2	5	4	7	6	9	8	11	10
2	2	3	0	1	6	7	4	5	10	11	8	9
3	3	2	1	0	7	6	5	4	11	10	9	8
4	4	7	5	6	8	11	9	10	0	3	1	2
5	5	6	4	7	9	10	8	11	1	2	0	3
6	6	5	7	4	10	9	11	8	2	1	3	0
7	7	4	6	5	11	8	10	9	3	0	2	1
8	8	10	11	9	0	2	3	1	4	6	7	5
9	9	11	10	8	1	3	2	0	5	7	6	4
10	10	8	9	11	2	0	1	3	6	4	5	7
11	11	9	8	10	3	1	0	2	7	5	4	6

Cycle graph



A_4 , alternating group formed by using even elements from over S_4 , that is the group being formed by using permutations upon four elements, solvable, identity element $e = 0$, $a^2 = e$, $b^2 = e$, $c^3 = e$, $ba = ab$, $ca = abc$, $cb = ac$

	e	a	b	ab	c	ac	bc	abc	c ²	ac ²	bc ²	abc ²
Element	0	1	2	3	4	5	6	7	8	9	10	11
Order	1	2	2	2	3	3	3	3	3	3	3	3

Number of distinct groups possible are:

For prime number: That only 1 cyclic group is always being possible

Square of prime: 2

Cube of prime: 5

Product of two primes ($p \times q$, p, q are primes):

1 if p does not divide up with $q-1$, 2 if p divides up with $q-1$

n is the product of distinct primes: $\sum_{d|n} \prod_{\substack{p|d \\ d \neq 1}} (p^{\sigma_p(n/d)} - 1) / (p - 1)$

where $\sigma_p(m)$ is the number of primes q such that $q|m$, $p|q-1$

Here is the table for that list below 2000:

1: 1	25: 2	49: 2	73: 1
2: 1	26: 2	50: 5	74: 2
3: 1	27: 5	51: 1	75: 3
4: 2	28: 4	52: 5	76: 4
5: 1	29: 1	53: 1	77: 1
6: 2	30: 4	54: 15	78: 6
7: 1	31: 1	55: 2	79: 1
8: 5	32: 51	56: 13	80: 52
9: 2	33: 1	57: 2	81: 15
10: 2	34: 2	58: 2	82: 2
11: 1	35: 1	59: 1	83: 1
12: 5	36: 14	60: 13	84: 15
13: 1	37: 1	61: 1	85: 1
14: 2	38: 2	62: 2	86: 2
15: 1	39: 2	63: 4	87: 1
16: 14	40: 14	64: 267	88: 12
17: 1	41: 1	65: 1	89: 1
18: 5	42: 6	66: 4	90: 10
19: 1	43: 1	67: 1	91: 1
20: 5	44: 4	68: 5	92: 4
21: 2	45: 2	69: 1	93: 2
22: 2	46: 2	70: 4	94: 2
23: 1	47: 1	71: 1	95: 1
24: 15	48: 52	72: 50	96: 231

97: 1	137: 1	177: 1	217: 1
98: 5	138: 4	178: 2	218: 2
99: 2	139: 1	179: 1	219: 2
100: 16	140: 11	180: 37	220: 15
101: 1	141: 1	181: 1	221: 1
102: 4	142: 2	182: 4	222: 6
103: 1	143: 1	183: 2	223: 1
104: 14	144: 197	184: 12	224: 197
105: 2	145: 1	185: 1	225: 6
106: 2	146: 2	186: 6	226: 2
107: 1	147: 6	187: 1	227: 1
108: 45	148: 5	188: 4	228: 15
109: 1	149: 1	189: 13	229: 1
110: 6	150: 13	190: 4	230: 4
111: 2	151: 1	191: 1	231: 2
112: 43	152: 12	192: 1543	232: 14
113: 1	153: 2	193: 1	233: 1
114: 6	154: 4	194: 2	234: 16
115: 1	155: 2	195: 2	235: 1
116: 5	156: 18	196: 17	236: 4
117: 4	157: 1	197: 1	237: 2
118: 2	158: 2	198: 10	238: 4
119: 1	159: 1	199: 1	239: 1
120: 47	160: 238	200: 52	240: 208
121: 2	161: 1	201: 2	241: 1
122: 2	162: 55	202: 2	242: 5
123: 1	163: 1	203: 2	243: 67
124: 4	164: 5	204: 12	244: 5
125: 5	165: 2	205: 2	245: 2
126: 16	166: 2	206: 2	246: 4
127: 1	167: 1	207: 2	247: 1
128: 2328	168: 57	208: 51	248: 12
129: 2	169: 2	209: 1	249: 1
130: 4	170: 4	210: 12	250: 15
131: 1	171: 5	211: 1	251: 1
132: 10	172: 4	212: 5	252: 46
133: 1	173: 1	213: 1	253: 2
134: 2	174: 4	214: 2	254: 2
135: 5	175: 2	215: 1	255: 1
136: 15	176: 42	216: 177	256: 56092

257: 1	297: 5	337: 1	377: 1
258: 6	298: 2	338: 5	378: 60
259: 1	299: 1	339: 1	379: 1
260: 15	300: 49	340: 15	380: 11
261: 2	301: 2	341: 1	381: 2
262: 2	302: 2	342: 18	382: 2
263: 1	303: 1	343: 5	383: 1
264: 39	304: 42	344: 12	384: 20169
265: 1	305: 2	345: 1	385: 2
266: 4	306: 10	346: 2	386: 2
267: 1	307: 1	347: 1	387: 4
268: 4	308: 9	348: 12	388: 5
269: 1	309: 2	349: 1	389: 1
270: 30	310: 6	350: 10	390: 12
271: 1	311: 1	351: 14	391: 1
272: 54	312: 61	352: 195	392: 44
273: 5	313: 1	353: 1	393: 1
274: 2	314: 2	354: 4	394: 2
275: 4	315: 4	355: 2	395: 1
276: 10	316: 4	356: 5	396: 30
277: 1	317: 1	357: 2	397: 1
278: 2	318: 4	358: 2	398: 2
279: 4	319: 1	359: 1	399: 5
280: 40	320: 1640	360: 162	400: 221
281: 1	321: 1	361: 2	401: 1
282: 4	322: 4	362: 2	402: 6
283: 1	323: 1	363: 3	403: 1
284: 4	324: 176	364: 11	404: 5
285: 2	325: 2	365: 1	405: 16
286: 4	326: 2	366: 6	406: 6
287: 1	327: 2	367: 1	407: 1
288: 1045	328: 15	368: 42	408: 46
289: 2	329: 1	369: 2	409: 1
290: 4	330: 12	370: 4	410: 6
291: 2	331: 1	371: 1	411: 1
292: 5	332: 4	372: 15	412: 4
293: 1	333: 5	373: 1	413: 1
294: 23	334: 2	374: 4	414: 10
295: 1	335: 1	375: 7	415: 1
296: 14	336: 228	376: 12	416: 235

417: 2	457: 1	497: 2	537: 1
418: 4	458: 2	498: 4	538: 2
419: 1	459: 5	499: 1	539: 2
420: 41	460: 11	500: 56	540: 119
421: 1	461: 1	501: 1	541: 1
422: 2	462: 12	502: 2	542: 2
423: 2	463: 1	503: 1	543: 2
424: 14	464: 51	504: 202	544: 246
425: 2	465: 4	505: 2	545: 1
426: 4	466: 2	506: 6	546: 24
427: 1	467: 1	507: 6	547: 1
428: 4	468: 55	508: 4	548: 5
429: 2	469: 1	509: 1	549: 4
430: 4	470: 4	510: 8	550: 16
431: 1	471: 2	511: 1	551: 1
432: 775	472: 12	512: 10494213	552: 39
433: 1	473: 1	513: 15	553: 1
434: 4	474: 6	514: 2	554: 2
435: 1	475: 2	515: 1	555: 2
436: 5	476: 11	516: 15	556: 4
437: 1	477: 2	517: 1	557: 1
438: 6	478: 2	518: 4	558: 16
439: 1	479: 1	519: 1	559: 1
440: 51	480: 1213	520: 49	560: 180
441: 13	481: 1	521: 1	561: 1
442: 4	482: 2	522: 10	562: 2
443: 1	483: 2	523: 1	563: 1
444: 18	484: 12	524: 4	564: 10
445: 1	485: 1	525: 6	565: 1
446: 2	486: 261	526: 2	566: 2
447: 1	487: 1	527: 1	567: 49
448: 1396	488: 14	528: 170	568: 12
449: 1	489: 2	529: 2	569: 1
450: 34	490: 10	530: 4	570: 12
451: 1	491: 1	531: 2	571: 1
452: 5	492: 12	532: 9	572: 11
453: 2	493: 1	533: 1	573: 1
454: 2	494: 4	534: 4	574: 4
455: 1	495: 4	535: 1	575: 2
456: 54	496: 42	536: 12	576: 8681

577: 1	617: 1	657: 5	697: 1
578: 5	618: 6	658: 4	698: 2
579: 2	619: 1	659: 1	699: 1
580: 15	620: 15	660: 40	700: 36
581: 1	621: 5	661: 1	701: 1
582: 6	622: 2	662: 2	702: 62
583: 1	623: 1	663: 2	703: 1
584: 15	624: 260	664: 12	704: 1387
585: 4	625: 15	665: 1	705: 1
586: 2	626: 2	666: 18	706: 2
587: 1	627: 2	667: 1	707: 1
588: 66	628: 5	668: 4	708: 10
589: 1	629: 1	669: 2	709: 1
590: 4	630: 32	670: 4	710: 6
591: 1	631: 1	671: 1	711: 4
592: 51	632: 12	672: 1280	712: 15
593: 1	633: 2	673: 1	713: 1
594: 30	634: 2	674: 2	714: 12
595: 1	635: 1	675: 17	715: 2
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599: 1	639: 2	679: 1	719: 1
600: 205	640: 21541	680: 53	720: 840
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602: 6	642: 4	682: 4	722: 5
603: 4	643: 1	683: 1	723: 2
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605: 7	645: 2	685: 1	725: 2
606: 4	646: 4	686: 15	726: 13
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609: 3	649: 1	689: 2	729: 504
610: 6	650: 10	690: 8	730: 4
611: 1	651: 5	691: 1	731: 1
612: 36	652: 4	692: 5	732: 18
613: 1	653: 1	693: 4	733: 1
614: 2	654: 6	694: 2	734: 2
615: 2	655: 2	695: 1	735: 6
616: 35	656: 53	696: 44	736: 195

737: 2	777: 5	817: 1	857: 1
738: 10	778: 2	818: 2	858: 12
739: 1	779: 1	819: 11	859: 1
740: 15	780: 53	820: 20	860: 11
741: 5	781: 1	821: 1	861: 2
742: 4	782: 4	822: 4	862: 2
743: 1	783: 5	823: 1	863: 1
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746: 2	786: 4	826: 4	866: 2
747: 2	787: 1	827: 1	867: 3
748: 11	788: 5	828: 30	868: 9
749: 1	789: 1	829: 1	869: 1
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751: 1	791: 2	831: 2	871: 1
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753: 1	793: 1	833: 2	873: 4
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755: 2	795: 1	835: 1	875: 5
756: 189	796: 4	836: 9	876: 18
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762: 6	802: 2	842: 2	882: 68
763: 1	803: 1	843: 1	883: 1
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765: 2	805: 1	845: 2	885: 1
766: 2	806: 4	846: 10	886: 2
767: 1	807: 1	847: 2	887: 1
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769: 1	809: 1	849: 2	889: 2
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771: 1	811: 1	851: 1	891: 15
772: 5	812: 16	852: 10	892: 4
773: 1	813: 2	853: 1	893: 1
774: 16	814: 4	854: 4	894: 4
775: 4	815: 1	855: 5	895: 1
776: 15	816: 205	856: 12	896: 19349

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898: 2	938: 4	978: 6	1018: 2
899: 1	939: 2	979: 2	1019: 1
900: 150	940: 11	980: 34	1020: 37
901: 1	941: 1	981: 5	1021: 1
902: 4	942: 6	982: 2	1022: 4
903: 7	943: 1	983: 1	1023: 2
904: 15	944: 42	984: 46	1024: 49487365422
905: 2	945: 13	985: 1	1025: 4
906: 6	946: 4	986: 4	1026: 66
907: 1	947: 1	987: 2	1027: 2
908: 4	948: 15	988: 11	1028: 5
909: 2	949: 1	989: 1	1029: 19
910: 8	950: 10	990: 30	1030: 4
911: 1	951: 1	991: 1	1031: 1
912: 222	952: 42	992: 196	1032: 54
913: 1	953: 1	993: 2	1033: 1
914: 2	954: 10	994: 6	1034: 4
915: 4	955: 2	995: 1	1035: 2
916: 5	956: 4	996: 10	1036: 11
917: 1	957: 1	997: 1	1037: 1
918: 30	958: 2	998: 2	1038: 4
919: 1	959: 1	999: 15	1039: 1
920: 39	960: 11394	1000: 199	1040: 231
921: 2	961: 2	1001: 1	1041: 1
922: 2	962: 4	1002: 4	1042: 2
923: 1	963: 2	1003: 1	1043: 1
924: 34	964: 5	1004: 4	1044: 36
925: 2	965: 1	1005: 2	1045: 2
926: 2	966: 12	1006: 2	1046: 2
927: 4	967: 1	1007: 1	1047: 2
928: 235	968: 42	1008: 954	1048: 12
929: 1	969: 2	1009: 1	1049: 1
930: 18	970: 4	1010: 6	1050: 40
931: 2	971: 1	1011: 2	1051: 1
932: 5	972: 900	1012: 13	1052: 4
933: 1	973: 1	1013: 1	1053: 51
934: 2	974: 2	1014: 23	1054: 4
935: 2	975: 6	1015: 2	1055: 2
936: 222	976: 51	1016: 12	1056: 1028

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1058: 5	1098: 16	1138: 2	1178: 4
1059: 1	1099: 1	1139: 1	1179: 2
1060: 15	1100: 51	1140: 41	1180: 11
1061: 1	1101: 2	1141: 1	1181: 1
1062: 10	1102: 4	1142: 2	1182: 4
1063: 1	1103: 1	1143: 5	1183: 3
1064: 35	1104: 170	1144: 39	1184: 235
1065: 2	1105: 1	1145: 1	1185: 2
1066: 4	1106: 4	1146: 4	1186: 2
1067: 1	1107: 5	1147: 1	1187: 1
1068: 12	1108: 5	1148: 11	1188: 99
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1071: 4	1111: 1	1151: 1	1191: 2
1072: 42	1112: 12	1152: 157877	1192: 14
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1082: 2	1122: 8	1162: 4	1202: 2
1083: 6	1123: 1	1163: 1	1203: 1
1084: 4	1124: 5	1164: 18	1204: 13
1085: 2	1125: 14	1165: 1	1205: 2
1086: 6	1126: 2	1166: 4	1206: 16
1087: 1	1127: 2	1167: 1	1207: 1
1088: 1681	1128: 39	1168: 53	1208: 12
1089: 6	1129: 1	1169: 1	1209: 5
1090: 4	1130: 4	1170: 32	1210: 27
1091: 1	1131: 2	1171: 1	1211: 1
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1093: 1	1133: 1	1173: 1	1213: 1
1094: 2	1134: 254	1174: 2	1214: 2
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1220: 20	1260: 131	1300: 50	1340: 11
1221: 2	1261: 1	1301: 1	1341: 2
1222: 4	1262: 2	1302: 24	1342: 4
1223: 1	1263: 2	1303: 1	1343: 1
1224: 164	1264: 42	1304: 12	1344: 11720
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1226: 2	1266: 6	1306: 2	1346: 2
1227: 2	1267: 1	1307: 1	1347: 1
1228: 4	1268: 5	1308: 18	1348: 5
1229: 1	1269: 5	1309: 1	1349: 1
1230: 12	1270: 4	1310: 6	1350: 112
1231: 1	1271: 1	1311: 2	1351: 1
1232: 153	1272: 44	1312: 244	1352: 52
1233: 2	1273: 1	1313: 1	1353: 1
1234: 2	1274: 10	1314: 18	1354: 2
1235: 1	1275: 3	1315: 1	1355: 2
1236: 15	1276: 11	1316: 9	1356: 12
1237: 1	1277: 1	1317: 2	1357: 1
1238: 2	1278: 10	1318: 2	1358: 4
1239: 2	1279: 1	1319: 1	1359: 4
1240: 51	1280: 1116461	1320: 181	1360: 245
1241: 1	1281: 5	1321: 1	1361: 1
1242: 30	1282: 2	1322: 2	1362: 4
1243: 1	1283: 1	1323: 51	1363: 1
1244: 4	1284: 10	1324: 4	1364: 9
1245: 1	1285: 1	1325: 2	1365: 5
1246: 4	1286: 2	1326: 12	1366: 2
1247: 1	1287: 4	1327: 1	1367: 1
1248: 1460	1288: 35	1328: 42	1368: 211
1249: 1	1289: 1	1329: 1	1369: 2
1250: 55	1290: 12	1330: 8	1370: 4
1251: 4	1291: 1	1331: 5	1371: 2
1252: 5	1292: 11	1332: 61	1372: 38
1253: 1	1293: 1	1333: 1	1373: 1
1254: 12	1294: 2	1334: 4	1374: 6
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1256: 14	1296: 3609	1336: 12	1376: 195

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1379: 2	1419: 2	1459: 1	1499: 1
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1381: 1	1421: 4	1461: 2	1501: 1
1382: 2	1422: 16	1462: 4	1502: 2
1383: 1	1423: 1	1463: 1	1503: 2
1384: 14	1424: 53	1464: 61	1504: 195
1385: 1	1425: 6	1465: 1	1505: 2
1386: 32	1426: 4	1466: 2	1506: 4
1387: 1	1427: 1	1467: 5	1507: 1
1388: 4	1428: 40	1468: 4	1508: 15
1389: 2	1429: 1	1469: 1	1509: 1
1390: 4	1430: 12	1470: 46	1510: 6
1391: 1	1431: 5	1471: 1	1511: 1
1392: 198	1432: 12	1472: 1387	1512: 889
1393: 1	1433: 1	1473: 1	1513: 1
1394: 4	1434: 4	1474: 6	1514: 2
1395: 8	1435: 2	1475: 2	1515: 2
1396: 5	1436: 4	1476: 36	1516: 4
1397: 1	1437: 1	1477: 2	1517: 1
1398: 4	1438: 2	1478: 2	1518: 12
1399: 1	1439: 1	1479: 1	1519: 2
1400: 153	1440: 5958	1480: 49	1520: 178
1401: 1	1441: 1	1481: 1	1521: 13
1402: 2	1442: 4	1482: 24	1522: 2
1403: 1	1443: 5	1483: 1	1523: 1
1404: 227	1444: 12	1484: 11	1524: 15
1405: 2	1445: 2	1485: 10	1525: 4
1406: 4	1446: 6	1486: 2	1526: 4
1407: 5	1447: 1	1487: 1	1527: 1
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1409: 1	1449: 4	1489: 1	1529: 1
1410: 8	1450: 10	1490: 4	1530: 20
1411: 1	1451: 1	1491: 3	1531: 1
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1413: 4	1453: 1	1493: 1	1533: 5
1414: 4	1454: 2	1494: 10	1534: 4
1415: 1	1455: 2	1495: 1	1535: 1
1416: 39	1456: 179	1496: 41	1536: 408641062

1537: 1	1577: 1	1617: 6	1657: 1
1538: 2	1578: 4	1618: 2	1658: 2
1539: 60	1579: 1	1619: 1	1659: 5
1540: 36	1580: 11	1620: 477	1660: 11
1541: 1	1581: 2	1621: 1	1661: 1
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1543: 1	1583: 1	1623: 2	1663: 1
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1545: 2	1585: 1	1625: 5	1665: 5
1546: 2	1586: 4	1626: 6	1666: 10
1547: 1	1587: 3	1627: 1	1667: 1
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1549: 1	1589: 1	1629: 5	1669: 1
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1553: 1	1593: 5	1633: 1	1673: 2
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1555: 2	1595: 2	1635: 2	1675: 2
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1562: 4	1602: 10	1642: 2	1682: 5
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1564: 11	1604: 5	1644: 12	1684: 5
1565: 1	1605: 1	1645: 1	1685: 1
1566: 30	1606: 4	1646: 2	1686: 4
1567: 1	1607: 1	1647: 13	1687: 1
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1569: 2	1609: 1	1649: 1	1689: 1
1570: 4	1610: 8	1650: 38	1690: 10
1571: 1	1611: 2	1651: 1	1691: 1
1572: 10	1612: 11	1652: 9	1692: 30
1573: 2	1613: 1	1653: 2	1693: 1
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1576: 14	1616: 51	1656: 137	1696: 235

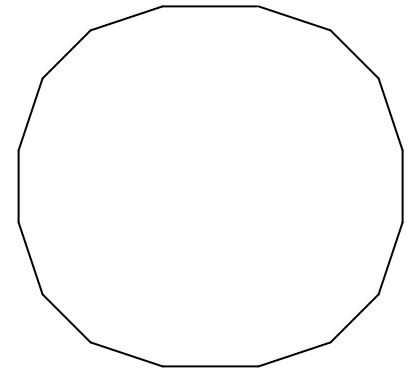
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1701: 309	1741: 1	1781: 1	1821: 2
1702: 4	1742: 4	1782: 110	1822: 2
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1705: 7	1745: 1	1785: 2	1825: 2
1706: 2	1746: 16	1786: 4	1826: 4
1707: 1	1747: 1	1787: 1	1827: 6
1708: 11	1748: 9	1788: 12	1828: 5
1709: 1	1749: 1	1789: 1	1829: 1
1710: 36	1750: 30	1790: 4	1830: 18
1711: 2	1751: 2	1791: 5	1831: 1
1712: 42	1752: 64	1792: 1083553	1832: 14
1713: 2	1753: 1	1793: 1	1833: 2
1714: 2	1754: 2	1794: 12	1834: 4
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1717: 1	1757: 1	1797: 1	1837: 1
1718: 2	1758: 4	1798: 4	1838: 2
1719: 2	1759: 1	1799: 1	1839: 2
1720: 39	1760: 1285	1800: 749	1840: 178
1721: 1	1761: 1	1801: 1	1841: 1
1722: 12	1762: 2	1802: 4	1842: 6
1723: 1	1763: 1	1803: 2	1843: 1
1724: 4	1764: 228	1804: 11	1844: 5
1725: 3	1765: 1	1805: 3	1845: 4
1726: 2	1766: 2	1806: 30	1846: 4
1727: 1	1767: 5	1807: 1	1847: 1
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1729: 1	1769: 1	1809: 13	1849: 2
1730: 4	1770: 8	1810: 6	1850: 10
1731: 2	1771: 2	1811: 1	1851: 1
1732: 5	1772: 4	1812: 15	1852: 4
1733: 1	1773: 2	1813: 2	1853: 1
1734: 13	1774: 2	1814: 2	1854: 16
1735: 1	1775: 4	1815: 9	1855: 1
1736: 35	1776: 260	1816: 12	1856: 1630

1857: 2	1897: 1	1937: 1	1977: 1
1858: 2	1898: 4	1938: 12	1978: 4
1859: 2	1899: 4	1939: 1	1979: 1
1860: 56	1900: 36	1940: 15	1980: 120
1861: 1	1901: 1	1941: 1	1981: 1
1862: 10	1902: 4	1942: 2	1982: 2
1863: 15	1903: 1	1943: 1	1983: 2
1864: 15	1904: 186	1944: 3973	1984: 1388
1865: 1	1905: 2	1945: 1	1985: 1
1866: 4	1906: 2	1946: 4	1986: 6
1867: 1	1907: 1	1947: 1	1987: 1
1868: 4	1908: 36	1948: 4	1988: 13
1869: 2	1909: 1	1949: 1	1989: 4
1870: 12	1910: 6	1950: 40	1990: 4
1871: 1	1911: 15	1951: 1	1991: 1
1872: 1096	1912: 12	1952: 235	1992: 39
1873: 1	1913: 1	1953: 11	1993: 1
1874: 2	1914: 8	1954: 2	1994: 2
1875: 21	1915: 1	1955: 1	1995: 5
1876: 9	1916: 4	1956: 15	1996: 4
1877: 1	1917: 5	1957: 1	1997: 1
1878: 6	1918: 4	1958: 6	1998: 66
1879: 1	1919: 1	1959: 1	1999: 1
1880: 39	1920: 241004	1960: 144	2000: 963
1881: 5	1921: 1	1961: 1	
1882: 2	1922: 5	1962: 18	
1883: 1	1923: 1	1963: 1	
1884: 18	1924: 15	1964: 4	
1885: 1	1925: 4	1965: 2	
1886: 4	1926: 10	1966: 2	
1887: 2	1927: 1	1967: 2	
1888: 195	1928: 15	1968: 203	
1889: 1	1929: 2	1969: 1	
1890: 120	1930: 4	1970: 4	
1891: 1	1931: 1	1971: 15	
1892: 9	1932: 34	1972: 15	
1893: 2	1933: 1	1973: 1	
1894: 2	1934: 2	1974: 12	
1895: 1	1935: 4	1975: 2	
1896: 54	1936: 167	1976: 39	

There are 14 non-isomorphic group structures of order 16

	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15
0	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15
1	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	0
2	2	3	4	5	6	7	8	9	10	11	12	13	14	15	0	1
3	3	4	5	6	7	8	9	10	11	12	13	14	15	0	1	2
4	4	5	6	7	8	9	10	11	12	13	14	15	0	1	2	3
5	5	6	7	8	9	10	11	12	13	14	15	0	1	2	3	4
6	6	7	8	9	10	11	12	13	14	15	0	1	2	3	4	5
7	7	8	9	10	11	12	13	14	15	0	1	2	3	4	5	6
8	8	9	10	11	12	13	14	15	0	1	2	3	4	5	6	7
9	9	10	11	12	13	14	15	0	1	2	3	4	5	6	7	8
10	10	11	12	13	14	15	0	1	2	3	4	5	6	7	8	9
11	11	12	13	14	15	0	1	2	3	4	5	6	7	8	9	10
12	12	13	14	15	0	1	2	3	4	5	6	7	8	9	10	11
13	13	14	15	0	1	2	3	4	5	6	7	8	9	10	11	12
14	14	15	0	1	2	3	4	5	6	7	8	9	10	11	12	13
15	15	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14

Cycle graph

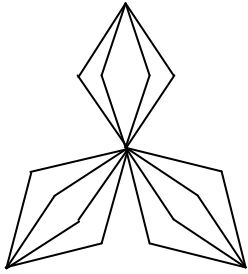


C_{16} , cyclic, identity element $e = 0$, $a^{16} = e$

	e	a	a^2	a^3	a^4	a^5	a^6	a^7	a^8	a^9	a^{10}	a^{11}	a^{12}	a^{13}	a^{14}	a^{15}
Element	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15
Order	1	16	8	16	4	16	8	16	2	16	8	16	4	16	8	16

	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15
0	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15
1	1	2	3	0	5	6	7	4	9	10	11	8	13	14	15	12
2	2	3	0	1	6	7	4	5	10	11	8	9	14	15	12	13
3	3	0	1	2	7	4	5	6	11	8	9	10	15	12	13	14
4	4	5	6	7	8	9	10	11	12	13	14	15	0	1	2	3
5	5	6	7	4	9	10	11	8	13	14	15	12	1	2	3	0
6	6	7	4	5	10	11	8	9	14	15	12	13	2	3	0	1
7	7	4	5	6	11	8	9	10	15	12	13	14	3	0	1	2
8	8	9	10	11	12	13	14	15	0	1	2	3	4	5	6	7
9	9	10	11	8	13	14	15	12	1	2	3	0	5	6	7	4
10	10	11	8	9	14	15	12	13	2	3	0	1	6	7	4	5
11	11	8	9	10	15	12	13	14	3	0	1	2	7	4	5	6
12	12	13	14	15	0	1	2	3	4	5	6	7	8	9	10	11
13	13	14	15	12	1	2	3	0	5	6	7	4	9	10	11	8
14	14	15	12	13	2	3	0	1	6	7	4	5	10	11	8	9
15	15	12	13	14	3	0	1	2	7	4	5	6	11	8	9	10

Cycle graph

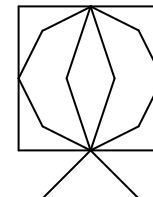


$C_4 \times C_4$, abelian, identity element $e = 0$, $a^4 = e$, $b^4 = e$, $ba = ab$

	e	a	a ²	a ³	b	ab	a ² b	a ³ b	b ²	ab ²	a ² b ²	a ³ b ²	b ³	ab ³	a ² b ³	a ³ b ³
Element	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15
Order	1	4	2	4	4	4	4	4	2	4	2	4	4	4	4	4

	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15
0	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15
1	1	2	3	4	5	6	7	0	9	10	11	12	13	14	15	8
2	2	3	4	5	6	7	0	1	10	11	12	13	14	15	8	9
3	3	4	5	6	7	0	1	2	11	12	13	14	15	8	9	10
4	4	5	6	7	0	1	2	3	12	13	14	15	8	9	10	11
5	5	6	7	0	1	2	3	4	13	14	15	8	9	10	11	12
6	6	7	0	1	2	3	4	5	14	15	8	9	10	11	12	13
7	7	0	1	2	3	4	5	6	15	8	9	10	11	12	13	14
8	8	9	10	11	12	13	14	15	0	1	2	3	4	5	6	7
9	9	10	11	12	13	14	15	8	1	2	3	4	5	6	7	0
10	10	11	12	13	14	15	8	9	2	3	4	5	6	7	0	1
11	11	12	13	14	15	8	9	10	3	4	5	6	7	0	1	2
12	12	13	14	15	8	9	10	11	4	5	6	7	0	1	2	3
13	13	14	15	8	9	10	11	12	5	6	7	0	1	2	3	4
14	14	15	8	9	10	11	12	13	6	7	0	1	2	3	4	5
15	15	8	9	10	11	12	13	14	7	0	1	2	3	4	5	6

Cycle graph

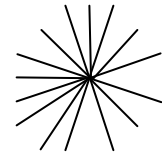


$C_2 \times C_8$, abelian, identity element $e = 0$, $a^8 = e$, $b^2 = e$, $ba = ab$

	e	a	a^2	a^3	a^4	a^5	a^6	a^7	b	ab	a^2b	a^3b	a^4b	a^5b	a^6b	a^7b
Element	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15
Order	1	8	4	8	2	8	4	8	2	8	4	8	2	8	4	8

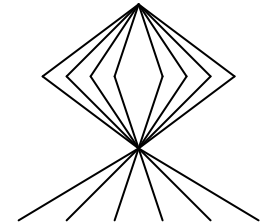
	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15
0	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15
1	1	0	3	2	5	4	7	6	9	8	11	10	13	12	15	14
2	2	3	0	1	6	7	4	5	10	11	8	9	14	15	12	13
3	3	2	1	0	7	6	5	4	11	10	9	8	15	14	13	12
4	4	5	6	7	0	1	2	3	12	13	14	15	8	9	10	11
5	5	4	7	6	1	0	3	2	13	12	15	14	9	8	11	10
6	6	7	4	5	2	3	0	1	14	15	12	13	10	11	8	9
7	7	6	5	4	3	2	1	0	15	14	13	12	11	10	9	8
8	8	9	10	11	12	13	14	15	0	1	2	3	4	5	6	7
9	9	8	11	10	13	12	15	14	1	0	3	2	5	4	7	6
10	10	11	8	9	14	15	12	13	2	3	0	1	6	7	4	5
11	11	10	9	8	15	14	13	12	3	2	1	0	7	6	5	4
12	12	13	14	15	8	9	10	11	4	5	6	7	0	1	2	3
13	13	12	15	14	9	8	11	10	5	4	7	6	1	0	3	2
14	14	15	12	13	10	11	8	9	6	7	4	5	2	3	0	1
15	15	14	13	12	11	10	9	8	7	6	5	4	3	2	1	0

Cycle graph


$$C_2^4, \text{ abelian, identity element } e = 0, a^2 = e, b^2 = e, c^2 = e, d^2 = e, ba = ab, cb = bc, db = bd, ca = ac, da = ad, dc = cd$$
[illegible]

	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15
0	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15
1	1	2	3	0	5	6	7	4	9	10	11	8	13	14	15	12
2	2	3	0	1	6	7	4	5	10	11	8	9	14	15	12	13
3	3	0	1	2	7	4	5	6	11	8	9	10	15	12	13	14
4	4	5	6	7	0	1	2	3	12	13	14	15	8	9	10	11
5	5	6	7	4	1	2	3	0	13	14	15	12	9	10	11	8
6	6	7	4	5	2	3	0	1	14	15	12	13	10	11	8	9
7	7	4	5	6	3	0	1	2	15	12	13	14	11	8	9	10
8	8	9	10	11	12	13	14	15	0	1	2	3	4	5	6	7
9	9	10	11	8	13	14	15	12	1	2	3	0	5	6	7	4
10	10	11	8	9	14	15	12	13	2	3	0	1	6	7	4	5
11	11	8	9	10	15	12	13	14	3	0	1	2	7	4	5	6
12	12	13	14	15	8	9	10	11	4	5	6	7	0	1	2	3
13	13	14	15	12	9	10	11	8	5	6	7	4	1	2	3	0
14	14	15	12	13	10	11	8	9	6	7	4	5	2	3	0	1
15	15	12	13	14	11	8	9	10	7	4	5	6	3	0	1	2

Cycle graph

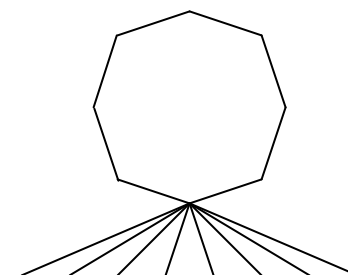


$C_4 \times C_2^2$, abelian, identity element $e = 0$, $a^4 = e$, $b^2 = e$, $c^2 = e$, $ba = ab$, $cb = bc$, $ca = ac$

[illegible]

	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15
0	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15
1	1	2	3	4	5	6	7	0	9	10	11	12	13	14	15	8
2	2	3	4	5	6	7	0	1	10	11	12	13	14	15	8	9
3	3	4	5	6	7	0	1	2	11	12	13	14	15	8	9	10
4	4	5	6	7	0	1	2	3	12	13	14	15	8	9	10	11
5	5	6	7	0	1	2	3	4	13	14	15	8	9	10	11	12
6	6	7	0	1	2	3	4	5	14	15	8	9	10	11	12	13
7	7	0	1	2	3	4	5	6	15	8	9	10	11	12	13	14
8	8	15	14	13	12	11	10	9	0	7	6	5	4	3	2	1
9	9	8	15	14	13	12	11	10	1	0	7	6	5	4	3	2
10	10	9	8	15	14	13	12	11	2	1	0	7	6	5	4	3
11	11	10	9	8	15	14	13	12	3	2	1	0	7	6	5	4
12	12	11	10	9	8	15	14	13	4	3	2	1	0	7	6	5
13	13	12	11	10	9	8	15	14	5	4	3	2	1	0	7	6
14	14	13	12	11	10	9	8	15	6	5	4	3	2	1	0	7
15	15	14	13	12	11	10	9	8	7	6	5	4	3	2	1	0

Cycle graph

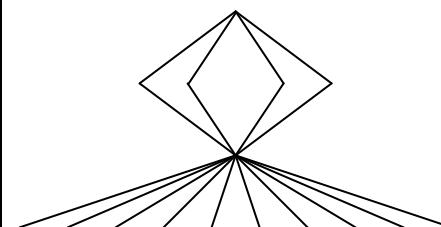


D_{16} , dihedral, nilpotent, identity element $e = 0$, $a^8 = e$, $b^2 = e$, $ba = a^{-1}b$

	e	a	a^2	a^3	a^4	a^5	a^6	a^7	b	ab	a^2b	a^3b	a^4b	a^5b	a^6b	a^7b
Element	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15
Order	1	8	4	8	2	8	4	8	2	2	2	2	2	2	2	2

	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15
0	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15
1	1	2	3	0	5	6	7	4	9	10	11	8	13	14	15	12
2	2	3	0	1	6	7	4	5	10	11	8	9	14	15	12	13
3	3	0	1	2	7	4	5	6	11	8	9	10	15	12	13	14
4	4	7	6	5	0	3	2	1	12	15	14	13	8	11	10	9
5	5	4	7	6	1	0	3	2	13	12	15	14	9	8	11	10
6	6	5	4	7	2	1	0	3	14	13	12	15	10	9	8	11
7	7	6	5	4	3	2	1	0	15	14	13	12	11	10	9	8
8	8	9	10	11	12	13	14	15	0	1	2	3	4	5	6	7
9	9	10	11	8	13	14	15	12	1	2	3	0	5	6	7	4
10	10	11	8	9	14	15	12	13	2	3	0	1	6	7	4	5
11	11	8	9	10	15	12	13	14	3	0	1	2	7	4	5	6
12	12	15	14	13	8	11	10	9	4	7	6	5	0	3	2	1
13	13	12	15	14	9	8	11	10	5	4	7	6	1	0	3	2
14	14	13	12	15	10	9	8	11	6	5	4	7	2	1	0	3
15	15	14	13	12	11	10	9	8	7	6	5	4	3	2	1	0

Cycle graph

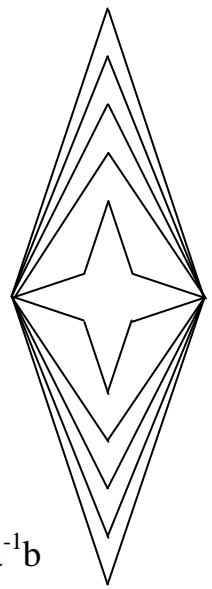


$D_8 \times C_2$, nilpotent, identity element $e = 0$, $a^4 = e$, $b^2 = e$, $c^2 = e$, $ba = a^{-1}b$, $ca = ac$, $cb = bc$

	e	a	a^2	a^3	b	ab	a^2b	a^3b	c	ac	a^2c	a^3c	bc	abc	a^2bc	a^3bc
Element	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15
Order	1	4	2	4	2	2	2	2	2	4	2	4	2	2	2	2

	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15
0	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15
1	1	2	3	4	5	6	7	0	9	10	11	12	13	14	15	8
2	2	3	4	5	6	7	0	1	10	11	12	13	14	15	8	9
3	3	4	5	6	7	0	1	2	11	12	13	14	15	8	9	10
4	4	5	6	7	0	1	2	3	12	13	14	15	8	9	10	11
5	5	6	7	0	1	2	3	4	13	14	15	8	9	10	11	12
6	6	7	0	1	2	3	4	5	14	15	8	9	10	11	12	13
7	7	0	1	2	3	4	5	6	15	8	9	10	11	12	13	14
8	8	15	14	13	12	11	10	9	4	3	2	1	0	7	6	5
9	9	8	15	14	13	12	11	10	5	4	3	2	1	0	7	6
10	10	9	8	15	14	13	12	11	6	5	4	3	2	1	0	7
11	11	10	9	8	15	14	13	12	7	6	5	4	3	2	1	0
12	12	11	10	9	8	15	14	13	0	7	6	5	4	3	2	1
13	13	12	11	10	9	8	15	14	1	0	7	6	5	4	3	2
14	14	13	12	11	10	9	8	15	2	1	0	7	6	5	4	3
15	15	14	13	12	11	10	9	8	3	2	1	0	7	6	5	4

Cycle graph

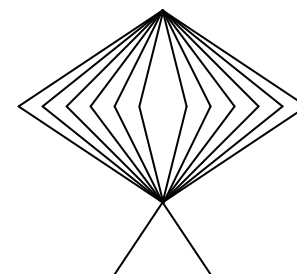


Q_{16} , nilpotent, dicyclic group, generalized Quaternion Group, identity element $e = 0$, $a^8 = e$, $b^2 = a^4$, $ba = a^{-1}b$

	e	a	a^2	a^3	a^4	a^5	a^6	a^7	b	ab	a^2b	a^3b	a^4b	a^5b	a^6b	a^7b
Element	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15
Order	1	8	4	8	2	8	4	8	4	4	4	4	4	4	4	4

	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15
0	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15
1	1	2	3	0	5	6	7	4	9	10	11	8	13	14	15	12
2	2	3	0	1	6	7	4	5	10	11	8	9	14	15	12	13
3	3	0	1	2	7	4	5	6	11	8	9	10	15	12	13	14
4	4	7	6	5	2	1	0	3	12	15	14	13	10	9	8	11
5	5	4	7	6	3	2	1	0	13	12	15	14	11	10	9	8
6	6	5	4	7	0	3	2	1	14	13	12	15	8	11	10	9
7	7	6	5	4	1	0	3	2	15	14	13	12	9	8	11	10
8	8	9	10	11	12	13	14	15	0	1	2	3	4	5	6	7
9	9	10	11	8	13	14	15	12	1	2	3	0	5	6	7	4
10	10	11	8	9	14	15	12	13	2	3	0	1	6	7	4	5
11	11	8	9	10	15	12	13	14	3	0	1	2	7	4	5	6
12	12	15	14	13	10	9	8	11	4	7	6	5	2	1	0	3
13	13	12	15	14	11	10	9	8	5	4	7	6	3	2	1	0
14	14	13	12	15	8	11	10	9	6	5	4	7	0	3	2	1
15	15	14	13	12	9	8	11	10	7	6	5	4	1	0	3	2

Cycle graph



$Q_8 \times C_2$, nilpotent, Hamiltonian group, identity element $e = 0$, $a^4 = e$, $b^2 = a^2$, $ba = a^{-1}b$, $c^2 = e$, $ca = ac$, $cb = bc$

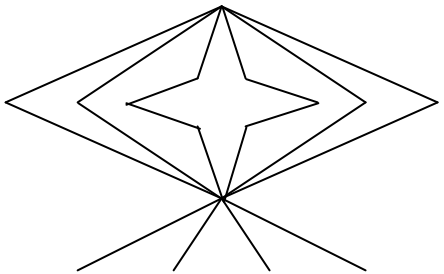
	e	a	a^2	a^3	b	ab	a^2b	a^3b	c	ac	a^2c	a^3c	bc	abc	a^2bc	a^3bc
Element	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15
Order	1	4	2	4	4	4	4	4	2	4	2	4	4	4	4	4

	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15
0	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15
1	1	2	3	4	5	6	7	0	9	10	11	12	13	14	15	8
2	2	3	4	5	6	7	0	1	10	11	12	13	14	15	8	9
3	3	4	5	6	7	0	1	2	11	12	13	14	15	8	9	10
4	4	5	6	7	0	1	2	3	12	13	14	15	8	9	10	11
5	5	6	7	0	1	2	3	4	13	14	15	8	9	10	11	12
6	6	7	0	1	2	3	4	5	14	15	8	9	10	11	12	13
7	7	0	1	2	3	4	5	6	15	8	9	10	11	12	13	14
8	8	11	14	9	12	15	10	13	0	3	6	1	4	7	2	5
9	9	12	15	10	13	8	11	14	1	4	7	2	5	0	3	6
10	10	13	8	11	14	9	12	15	2	5	0	3	6	1	4	7
11	11	14	9	12	15	10	13	8	3	6	1	4	7	2	5	0
12	12	15	10	13	8	11	14	9	4	7	2	5	0	3	6	1
13	13	8	11	14	9	12	15	10	5	0	3	6	1	4	7	2
14	14	9	12	15	10	13	8	11	6	1	4	7	2	5	0	3
15	15	10	13	8	11	14	9	12	7	2	5	0	3	6	1	4

Quasidihedral group, nilpotent, identity element $e = 0$, $a^8 = e$, $b^2 = e$, $bab = a^3$

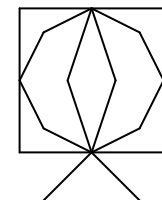
	e	a	a ²	a ³	a ⁴	a ⁵	a ⁶	a ⁷	b	ab	a ² b	a ³ b	a ⁴ b	a ⁵ b	a ⁶ b	a ⁷ b
Element	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15
Order	1	8	4	8	2	8	4	8	2	4	2	4	2	4	2	4

Cycle graph



	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15
0	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15
1	1	2	3	4	5	6	7	0	9	10	11	12	13	14	15	8
2	2	3	4	5	6	7	0	1	10	11	12	13	14	15	8	9
3	3	4	5	6	7	0	1	2	11	12	13	14	15	8	9	10
4	4	5	6	7	0	1	2	3	12	13	14	15	8	9	10	11
5	5	6	7	0	1	2	3	4	13	14	15	8	9	10	11	12
6	6	7	0	1	2	3	4	5	14	15	8	9	10	11	12	13
7	7	0	1	2	3	4	5	6	15	8	9	10	11	12	13	14
8	8	13	10	15	12	9	14	11	0	5	2	7	4	1	6	3
9	9	14	11	8	13	10	15	12	1	6	3	0	5	2	7	4
10	10	15	12	9	14	11	8	13	2	7	4	1	6	3	0	5
11	11	8	13	10	15	12	9	14	3	0	5	2	7	4	1	6
12	12	9	14	11	8	13	10	15	4	1	6	3	0	5	2	7
13	13	10	15	12	9	14	11	8	5	2	7	4	1	6	3	0
14	14	11	8	13	10	15	12	9	6	3	0	5	2	7	4	1
15	15	12	9	14	11	8	13	10	7	4	1	6	3	0	5	2

Cycle graph

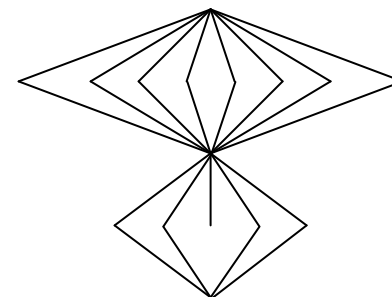


Modular group, (also known as Iwasawa group), nilpotent, identity element $e = 0$, $a^8 = e$, $b^2 = e$, $bab = a^5$

	e	a	a^2	a^3	a^4	a^5	a^6	a^7	b	ab	a^2b	a^3b	a^4b	a^5b	a^6b	a^7b
Element	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15
Order	1	8	4	8	2	8	4	8	2	8	4	8	2	8	4	8

	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15
0	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15
1	1	2	3	0	5	6	7	4	9	10	11	8	13	14	15	12
2	2	3	0	1	6	7	4	5	10	11	8	9	14	15	12	13
3	3	0	1	2	7	4	5	6	11	8	9	10	15	12	13	14
4	4	7	6	5	8	11	10	9	12	15	14	13	0	3	2	1
5	5	4	7	6	9	8	11	10	13	12	15	14	1	0	3	2
6	6	5	4	7	10	9	8	11	14	13	12	15	2	1	0	3
7	7	6	5	4	11	10	9	8	15	14	13	12	3	2	1	0
8	8	9	10	11	12	13	14	15	0	1	2	3	4	5	6	7
9	9	10	11	8	13	14	15	12	1	2	3	0	5	6	7	4
10	10	11	8	9	14	15	12	13	2	3	0	1	6	7	4	5
11	11	8	9	10	15	12	13	14	3	0	1	2	7	4	5	6
12	12	15	14	13	0	3	2	1	4	7	6	5	8	11	10	9
13	13	12	15	14	1	0	3	2	5	4	7	6	9	8	11	10
14	14	13	12	15	2	1	0	3	6	5	4	7	10	9	8	11
15	15	14	13	12	3	2	1	0	7	6	5	4	11	10	9	8

Cycle graph

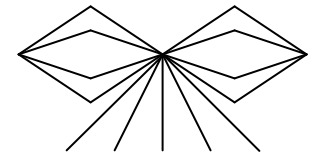


Semi-direct product of C_4 and C_4 , nilpotent, identity element $e = 0$, $a^4 = e$, $b^4 = e$, $ba^3 = ab$

	e	a	a^2	a^3	b	ab	a^2b	a^3b	b^2	ab^2	a^2b^2	a^3b^2	b^3	ab^3	a^2b^3	a^3b^3
Element	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15
Order	1	4	2	4	4	4	4	4	2	4	2	4	4	4	4	4

	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15
0	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15
1	1	2	3	0	5	6	7	4	9	10	11	8	13	14	15	12
2	2	3	0	1	6	7	4	5	10	11	8	9	14	15	12	13
3	3	0	1	2	7	4	5	6	11	8	9	10	15	12	13	14
4	4	15	6	13	8	3	10	1	12	7	14	5	0	11	2	9
5	5	12	7	14	9	0	11	2	13	4	15	6	1	8	3	10
6	6	13	4	15	10	1	8	3	14	5	12	7	2	9	0	11
7	7	14	5	12	11	2	9	0	15	6	13	4	3	10	1	8
8	8	9	10	11	12	13	14	15	0	1	2	3	4	5	6	7
9	9	10	11	8	13	14	15	12	1	2	3	0	5	6	7	4
10	10	11	8	9	14	15	12	13	2	3	0	1	6	7	4	5
11	11	8	9	10	15	12	13	14	3	0	1	2	7	4	5	6
12	12	7	14	5	0	11	2	9	4	15	6	13	8	3	10	1
13	13	4	15	6	1	8	3	10	5	12	7	14	9	0	11	2
14	14	5	12	7	2	9	0	11	6	13	4	15	10	1	8	3
15	15	6	13	4	3	10	1	8	7	14	5	12	11	2	9	0

Cycle graph

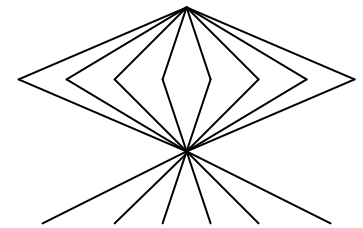


$G_{4,4}$ is semi-direct product of C_2^2 and C_4 , nilpotent, identity element $e = 0$, $a^4 = e$, $b^4 = e$, $abab = e$, $ba^3 = ab^3$

	e	a	a ²	a ³	b	ab	a ² b	a ³ b	b ²	ab ²	a ² b ²	a ³ b ²	b ³	ab ³	a ² b ³	a ³ b ³
Element	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15
Order	1	4	2	4	4	2	4	2	2	4	2	4	4	2	4	2

	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15
0	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15
1	1	2	3	0	5	6	7	4	9	10	11	8	13	14	15	12
2	2	3	0	1	6	7	4	5	10	11	8	9	14	15	12	13
3	3	0	1	2	7	4	5	6	11	8	9	10	15	12	13	14
4	4	5	6	7	0	1	2	3	12	13	14	15	8	9	10	11
5	5	6	7	4	1	2	3	0	13	14	15	12	9	10	11	8
6	6	7	4	5	2	3	0	1	14	15	12	13	10	11	8	9
7	7	4	5	6	3	0	1	2	15	12	13	14	11	8	9	10
8	8	9	10	11	14	15	12	13	0	1	2	3	6	7	4	5
9	9	10	11	8	15	12	13	14	1	2	3	0	7	4	5	6
10	10	11	8	9	12	13	14	15	2	3	0	1	4	5	6	7
11	11	8	9	10	13	14	15	12	3	0	1	2	5	6	7	4
12	12	13	14	15	10	11	8	9	4	5	6	7	2	3	0	1
13	13	14	15	12	11	8	9	10	5	6	7	4	3	0	1	2
14	14	15	12	13	8	9	10	11	6	7	4	5	0	1	2	3
15	15	12	13	14	9	10	11	8	7	4	5	6	1	2	3	0

Cycle graph



Group generated by using Pauli matrices, nilpotent, identity element $e = 0$, $a^4 = e$, $b^2 = e$, $c^2 = e$,
 $cbca^2b = e$, $bab = a$, $cac = a$

	e	a	a^2	a^3	b	ab	a^2b	a^3b	c	ac	a^2c	a^3c	bc	abc	a^2bc	a^3bc
Element	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15
Order	1	4	2	4	2	4	2	4	2	4	2	4	4	2	4	2

Glossary of Terms:

Let G be a finite group, of order $|G|$.

- The **center** of G is the set of elements which commute with all elements of G . It is a normal subgroup of G .

The center of G equals G if and only if G is abelian.

- Two elements g_1 and g_2 of G are **conjugate**, if there is an element $h \in G$ such that $hg_1h^{-1} = g_2$. The **conjugacy class** of an element $g \in G$ is the set of elements conjugate to g .
- In the same way, two subgroups H_1 and H_2 of G are **conjugate**, if there is an element $h \in G$ such that $hH_1h^{-1} = H_2$.

A subgroup H is **normal** if there is no other subgroup conjugate to it. G is a **simple group** if it contains no normal subgroup other than G and the trivial subgroup.

- The **commutator subgroup** or **derived subgroup** of G , $[G, G]$, is the subgroup generated by all the **commutators** $g_1g_2g_1^{-1}g_2^{-1}$. It is a normal subgroup of G , the smallest such that the quotient group is abelian.

$[G, G]$ is trivial if and only if G is abelian. G is a **perfect group** if $[G, G] = G$.

- The **derived series** of G is the series of subgroups

$$N_1 \supset N_2 \supset \dots \supset N_k,$$

where $N_1 = [G, G]$ (the commutator subgroup), and $N_i = [N_{i-1}, N_{i-1}]$ for $i > 1$. And the series stops at N_k such that $N_k = [N_k, N_k]$.

All the terms N_i in the derived series are normal subgroups of G .

G is a **solvable group** if the derived series stops at the trivial subgroup.

- The **exponent** of G is the lcm of orders of all elements of G . It divides $|G|$.
- The **lower central series** of G is the series of subgroups

$$N_1 \supset N_2 \supset \dots \supset N_k,$$

where $N_1 = [G, G]$ (the commutator subgroup), and $N_i = [G, N_{i-1}]$ for $i > 1$. And the series stops at N_k such that $N_k = [G, N_k]$.

All the terms N_i in the lower central series are normal subgroups of G .

- The **normal closure** of a subgroup H is the subgroup N of G generated by elements in H and all its conjugates. N is a normal subgroup of G .
- The **normalizer** of a subgroup H is the largest subgroup N of G containing H , such that H is a normal subgroup of N .
- Let p be a prime factor of $|G|$. A **p -Sylow subgroup** of G is a maximal subgroup H whose order is a power of p . $|H|$ equals the largest power of p dividing $|G|$.

A p -Sylow subgroup needs not to be normal, but all p -Sylow subgroups are conjugate to each other.

- The **upper central series** of G is the series of subgroups

$$N_1 \supset N_2 \supset \dots \supset N_k,$$

where N_k is the center of G , and N_i is the center of the quotient group G/N_{i+1} for $i < k$. And either $N_1 = G$, or G/N_1 has trivial center.

All the terms N_i in the upper central series are normal subgroups of G .

G is a **nilpotent group** if $N_1 = G$.

Types of groups:

- (1) Cyclic group of N elements. There exist only one cyclic group for any given group order, the rest of the cyclic groups of same order are all isomorphic to the original cyclic group. When N is prime, cyclic group is the only group structure that is being possible for order of N , and so is the case when N is square-free, i.e. N is the product of distinct primes such that for any two prime factors p, q of N , p does not divide $q-1$. For any cyclic group of order N , an element with order of N is known as the generator of the group. For such a group, there exist exactly $\phi(N)$ generators, i.e. number of numbers less than N that are co-prime to N .
- (2) Abelian group formed by using direct product of two smaller cyclic or abelian groups.
- (3) Other non-abelian groups formed by direct product of two smaller groups.
- (4) Dihedral group of $2N$ elements.
- (5) Quaternion group of 2^N elements.
- (6) Symmetry group formed by permutation of N elements under composition. It contains $N!$ elements. When $N = 3$, the symmetry group is isomorphic to the dihedral group of order 6. For values of $N \geq 4$, this is never true.
- (7) Alternating group formed by even permutations of N elements under composition operation, consisting of $(N!)/2$ elements. It is a subgroup of the symmetry group of order $N!$
- (8) Groups that are being formed by using semi-direct product of two smaller groups.
- (9) Quasidihedral groups, Modular (Iwasawa) groups for 2^N elements.
- (10) Frobenius group, solvable group, for kMN elements, where M, N are distinct prime numbers such that M divides $N-1$.
- (11) Dicyclic group for $4N$ elements. For $N = 2$, dicyclic group is isomorphic to Quaternion group. When N is a power of 2, then dicyclic group is isomorphic to generalized Quaternion group.

Groups of order upto 31 elements

Order 2: that cyclic group only

Order 3: that cyclic group only

Order 4: C_4, C_2^2 (Klein 4 group)

Order 5: cyclic group only

Order 6: C_6, D_6 (dihedral group) $\langle a, b \mid a^3 = e, b^2 = e, ba = a^{-1}b \rangle$

Order 7: cyclic group only

Order 8: $C_8, C_4 \times C_2, C_2^3, D_8,$

Quaternion Group $Q_8 \langle a, b \mid a^4 = e, a^2 = b^2, ba = a^{-1}b \rangle$ (This is dicyclic group)

Order 9: C_9, C_3^2

Order 10: C_{10}, D_{10}

Order 11: cyclic group only

Order 12: $C_{12}, C_2 \times C_6, D_{12}, T_{12}$ = semi-direct product of C_3 and C_4 (dicyclic group)

$\langle s, t \mid s^6 = e, s^3 = t^2, ts = s^{-1}t \rangle$ or also $\langle x, y \mid x^4 = e, y^3 = e, xy = y^{-1}x \rangle$,

A_4 is the alternating group that is being formed by using even permutations from among four elements under composition operation. It is a subgroup of symmetry group S_4 .

$A_4 = \langle a, b, c \mid a^2 = e, b^2 = e, c^3 = e, ba = ab, ca = abc, cb = ac \rangle$

Order 13: cyclic group only

Order 14: C_{14}, D_{14}

Order 15: cyclic group only

Order 16: $C_{16}, C_8 \times C_2, C_4 \times C_2^2, C_4^2, C_2^4, D_{16}, D_8 \times C_2$,

Generalized Quaternion Group (dicyclic group) $Q_{16} = \langle s, t \mid s^8 = e, s^4 = t^2, ts = s^{-1}t \rangle$

Hamiltonian Group $Q_8 \times C_2$

Quasidihedral group (also known as Semidihedral group) $\langle s, t \mid s^8 = t^2 = e, st = ts^3 \rangle$

Modular group (also known as Iwasawa group) $\langle s, t \mid s^8 = t^2 = e, st = ts^5 \rangle$

Semi-direct product of C_4 and C_4 $\langle s, t \mid s^4 = t^4 = e, st = ts^3 \rangle$

$G_{4,4}$ = Semi-direct product of C_2^2 and C_4 $\langle s, t \mid s^4 = t^4 = e, stst = e, ts^3 = st^3 \rangle$

Group that is being generated by using Pauli matrices

$\langle a, b, c \mid a^4 = b^2 = c^2 = e, cbca^2b = e, bab = cac = a \rangle$

Order 17: cyclic group only

Order 18: $C_{18}, C_6 \times C_3, D_{18}, D_6 \times C_3$,

(semi-direct product of C_3 and C_3) $\times C_2 = \langle x, y, z \mid x^2 = y^3 = z^3 = e, yz = zy, yxy = x, zxz = x \rangle$

Order 19: cyclic group only

Order 20: $C_{20}, C_{10} \times C_2, D_{20}$, Frobenius group $\langle s, t \mid s^4 = t^5 = e, ts = st^2 \rangle$,

semi direct product of C_5 and $C_4 = \langle s, t \mid s^4 = t^5 = e, st = t^{-1}s \rangle$ (dicyclic group)

Order 21: C_{21} , Frobenius group $\langle a, b \mid a^3 = b^7 = e, ba = ab^2 \rangle$

Order 22: C_{22}, D_{22}

Order 23: cyclic group only

Order 25: C_{25}, C_5^2

Order 26: C_{26}, D_{26}

Order 27: $C_{27}, C_9 \times C_3, C_3^3, \langle s, t \mid s^9 = t^3 = e, st = ts^4 \rangle$,

$\langle x, y, z \mid x^3 = y^3 = z^3 = e, yz = zyx, xy = yx, xz = zx \rangle$

Order 28: $C_{28}, C_2 \times C_{14}, D_{28}$,

semi direct product of C_7 and $C_4 = \langle s, t \mid s^4 = t^7 = e, st = t^{-1}s \rangle$ (dicyclic group)

Order 29: cyclic group only

Order 30: $C_{30}, D_{30}, D_{10} \times C_3, D_6 \times C_5$

Order 31: cyclic group only

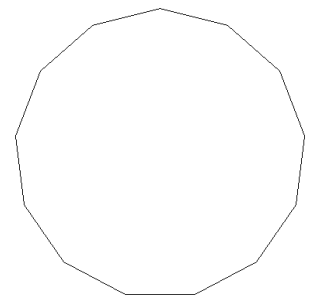
Order 24 (15 groups)

1. Semi-direct product of C_3 and $C_8 = \langle a, b \mid a^8 = b^3 = e, bab = a \rangle$
2. $C_{24} = C_8 \times C_3$
3. Semi-direct product of Q_8 and $C_3 =$ Special linear group over $GF(3)$
 $\langle a, b \mid a^4 = e, a^2 = b^2, c^3 = e, ba = a^{-1}b, ac = cb, cab = bc \rangle$
4. Dicyclic group of order 24: $Q_{12} = \langle a, b \mid a^{12} = b^6, b^4 = e, ab = b^{-1}a \rangle$
5. $D_6 \times C_4$
6. $D_{24} =$ semi direct product of C_4 and D_6
7. Semi direct product of C_6 and $C_4 =$ Dicyclic group of order $12 \times C_2 = T_{12} \times C_2$
 $\langle a, b \mid a^4 = b^6 = e, bab = a \rangle$
8. Semi direct product of C_3 and D_8
 $\langle a, b, c \mid a^3 = e, b^4 = e, c^2 = e, cb = b^{-1}c, ba = a^{-1}b, ac = ca \rangle$
9. $C_{12} \times C_2 = C_6 \times C_4$
10. $D_8 \times C_3 =$ semi direct product of C_4 and $C_6 =$ semi direct product of C_2^2 and C_6
11. $Q_8 \times C_3$
12. S_4 is the symmetry group that is being formed by using permutations upon four elements, under composition operation.
13. $A_4 \times C_2 =$ semi direct product of C_2^3 and C_3
14. $D_{12} \times C_2 = D_6 \times C_2^2$ is dihedral group that is formed from $C_6 \times C_2$
15. $C_6 \times C_2^2 = C_3 \times C_2^3$

Order 13 (1 group)

	0	1	2	3	4	5	6	7	8	9	10	11	12
0	0	1	2	3	4	5	6	7	8	9	10	11	12
1	1	2	3	4	5	6	7	8	9	10	11	12	0
2	2	3	4	5	6	7	8	9	10	11	12	0	1
3	3	4	5	6	7	8	9	10	11	12	0	1	2
4	4	5	6	7	8	9	10	11	12	0	1	2	3
5	5	6	7	8	9	10	11	12	0	1	2	3	4
6	6	7	8	9	10	11	12	0	1	2	3	4	5
7	7	8	9	10	11	12	0	1	2	3	4	5	6
8	8	9	10	11	12	0	1	2	3	4	5	6	7
9	9	10	11	12	0	1	2	3	4	5	6	7	8
10	10	11	12	0	1	2	3	4	5	6	7	8	9
11	11	12	0	1	2	3	4	5	6	7	8	9	10
12	12	0	1	2	3	4	5	6	7	8	9	10	11

Cycle graph



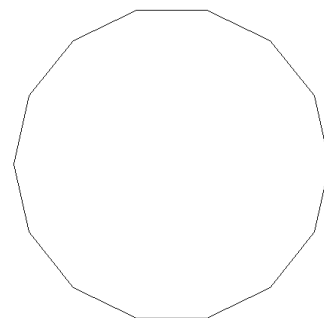
C₁₃, cyclic, identity element e = 0, a¹³ = e

[illegible]

Order 14 (2 groups)

	0	1	2	3	4	5	6	7	8	9	10	11	12	13
0	0	1	2	3	4	5	6	7	8	9	10	11	12	13
1	1	2	3	4	5	6	7	8	9	10	11	12	13	0
2	2	3	4	5	6	7	8	9	10	11	12	13	0	1
3	3	4	5	6	7	8	9	10	11	12	13	0	1	2
4	4	5	6	7	8	9	10	11	12	13	0	1	2	3
5	5	6	7	8	9	10	11	12	13	0	1	2	3	4
6	6	7	8	9	10	11	12	13	0	1	2	3	4	5
7	7	8	9	10	11	12	13	0	1	2	3	4	5	6
8	8	9	10	11	12	13	0	1	2	3	4	5	6	7
9	9	10	11	12	13	0	1	2	3	4	5	6	7	8
10	10	11	12	13	0	1	2	3	4	5	6	7	8	9
11	11	12	13	0	1	2	3	4	5	6	7	8	9	10
12	12	13	0	1	2	3	4	5	6	7	8	9	10	11
13	13	0	1	2	3	4	5	6	7	8	9	10	11	12

Cycle graph

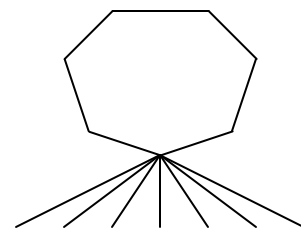


C_{14} , cyclic, identity element $e = 0$, $a^{14} = e$

	e	a	a ²	a ³	a ⁴	a ⁵	a ⁶	a ⁷	a ⁸	a ⁹	a ¹⁰	a ¹¹	a ¹²	a ¹³
Element	0	1	2	3	4	5	6	7	8	9	10	11	12	13
Order	1	14	7	14	7	14	7	2	7	14	7	14	7	14

	0	1	2	3	4	5	6	7	8	9	10	11	12	13
0	0	1	2	3	4	5	6	7	8	9	10	11	12	13
1	1	2	3	4	5	6	0	8	9	10	11	12	13	7
2	2	3	4	5	6	0	1	9	10	11	12	13	7	8
3	3	4	5	6	0	1	2	10	11	12	13	7	8	9
4	4	5	6	0	1	2	3	11	12	13	7	8	9	10
5	5	6	0	1	2	3	4	12	13	7	8	9	10	11
6	6	0	1	2	3	4	5	13	7	8	9	10	11	12
7	7	13	12	11	10	9	8	0	6	5	4	3	2	1
8	8	7	13	12	11	10	9	1	0	6	5	4	3	2
9	9	8	7	13	12	11	10	2	1	0	6	5	4	3
10	10	9	8	7	13	12	11	3	2	1	0	6	5	4
11	11	10	9	8	7	13	12	4	3	2	1	0	6	5
12	12	11	10	9	8	7	13	5	4	3	2	1	0	6
13	13	12	11	10	9	8	7	6	5	4	3	2	1	0

Cycle graph



D_{14} , dihedral, identity element $e = 0$, $a^7 = e$, $b^2 = e$, $ba = a^{-1}b$

	e	a	a ²	a ³	a ⁴	a ⁵	a ⁶	b	ab	a ² b	a ³ b	a ⁴ b	a ⁵ b	a ⁶ b
Element	0	1	2	3	4	5	6	7	8	9	10	11	12	13
Order	1	14	7	14	7	14	7	2	2	2	2	2	2	2

	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14
0	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14
1	1	2	3	4	5	6	7	8	9	10	11	12	13	14	0
2	2	3	4	5	6	7	8	9	10	11	12	13	14	0	1
3	3	4	5	6	7	8	9	10	11	12	13	14	0	1	2
4	4	5	6	7	8	9	10	11	12	13	14	0	1	2	3
5	5	6	7	8	9	10	11	12	13	14	0	1	2	3	4
6	6	7	8	9	10	11	12	13	14	0	1	2	3	4	5
7	7	8	9	10	11	12	13	14	0	1	2	3	4	5	6
8	8	9	10	11	12	13	14	0	1	2	3	4	5	6	7
9	9	10	11	12	13	14	0	1	2	3	4	5	6	7	8
10	10	11	12	13	14	0	1	2	3	4	5	6	7	8	9
11	11	12	13	14	0	1	2	3	4	5	6	7	8	9	10
12	12	13	14	0	1	2	3	4	5	6	7	8	9	10	11
13	13	14	0	1	2	3	4	5	6	7	8	9	10	11	12
14	14	0	1	2	3	4	5	6	7	8	9	10	11	12	13

	e	a	a ²	a ³	a ⁴	a ⁵	a ⁶	a ⁷	a ⁸	a ⁹	a ¹⁰	a ¹¹	a ¹²	a ¹³	a ¹⁴
Element	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14
Order	1	15	15	5	15	3	5	15	15	5	3	15	5	15	15

	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16
0	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16
1	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	0
2	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	0	1
3	3	4	5	6	7	8	9	10	11	12	13	14	15	16	0	1	2
4	4	5	6	7	8	9	10	11	12	13	14	15	16	0	1	2	3
5	5	6	7	8	9	10	11	12	13	14	15	16	0	1	2	3	4
6	6	7	8	9	10	11	12	13	14	15	16	0	1	2	3	4	5
7	7	8	9	10	11	12	13	14	15	16	0	1	2	3	4	5	6
8	8	9	10	11	12	13	14	15	16	0	1	2	3	4	5	6	7
9	9	10	11	12	13	14	15	16	0	1	2	3	4	5	6	7	8
10	10	11	12	13	14	15	16	0	1	2	3	4	5	6	7	8	9
11	11	12	13	14	15	16	0	1	2	3	4	5	6	7	8	9	10
12	12	13	14	15	16	0	1	2	3	4	5	6	7	8	9	10	11
13	13	14	15	16	0	1	2	3	4	5	6	7	8	9	10	11	12
14	14	15	16	0	1	2	3	4	5	6	7	8	9	10	11	12	13
15	15	16	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14
16	16	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15

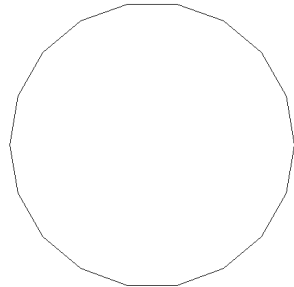
A circle with a center point labeled 'O'.

[illegible]

Order 18 (5 groups)

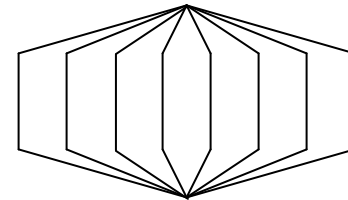
	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17
0	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17
1	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	0
2	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	0	1
3	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	0	1	2
4	4	5	6	7	8	9	10	11	12	13	14	15	16	17	0	1	2	3
5	5	6	7	8	9	10	11	12	13	14	15	16	17	0	1	2	3	4
6	6	7	8	9	10	11	12	13	14	15	16	17	0	1	2	3	4	5
7	7	8	9	10	11	12	13	14	15	16	17	0	1	2	3	4	5	6
8	8	9	10	11	12	13	14	15	16	17	0	1	2	3	4	5	6	7
9	9	10	11	12	13	14	15	16	17	0	1	2	3	4	5	6	7	8
10	10	11	12	13	14	15	16	17	0	1	2	3	4	5	6	7	8	9
11	11	12	13	14	15	16	17	0	1	2	3	4	5	6	7	8	9	10
12	12	13	14	15	16	17	0	1	2	3	4	5	6	7	8	9	10	11
13	13	14	15	16	17	0	1	2	3	4	5	6	7	8	9	10	11	12
14	14	15	16	17	0	1	2	3	4	5	6	7	8	9	10	11	12	13
15	15	16	17	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14
16	16	17	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15
17	17	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16

Cycle graph

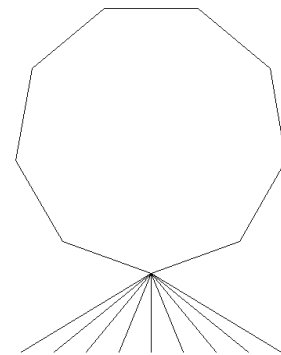


C_{18} , cyclic, identity element $e = 0$, $a^{18} = e$

	e	a	a ²	a ³	a ⁴	a ⁵	a ⁶	a ⁷	a ⁸	a ⁹	a ¹⁰	a ¹¹	a ¹²	a ¹³	a ¹⁴	a ¹⁵	a ¹⁶	a ¹⁷
Element	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17
Order	1	18	9	6	9	18	3	18	9	2	9	18	3	18	9	6	9	18

Cycle graph[illegible]

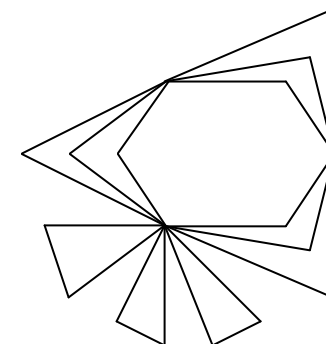
	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17
0	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17
1	1	2	3	4	5	6	7	8	0	10	11	12	13	14	15	16	17	9
2	2	3	4	5	6	7	8	0	1	11	12	13	14	15	16	17	9	10
3	3	4	5	6	7	8	0	1	2	12	13	14	15	16	17	9	10	11
4	4	5	6	7	8	0	1	2	3	13	14	15	16	17	9	10	11	12
5	5	6	7	8	0	1	2	3	4	14	15	16	17	9	10	11	12	13
6	6	7	8	0	1	2	3	4	5	15	16	17	9	10	11	12	13	14
7	7	8	0	1	2	3	4	5	6	16	17	9	10	11	12	13	14	15
8	8	0	1	2	3	4	5	6	7	17	9	10	11	12	13	14	15	16
9	9	17	16	15	14	13	12	11	10	0	8	7	6	5	4	3	2	1
10	10	9	17	16	15	14	13	12	11	1	0	8	7	6	5	4	3	2
11	11	10	9	17	16	15	14	13	12	2	1	0	8	7	6	5	4	3
12	12	11	10	9	17	16	15	14	13	3	2	1	0	8	7	6	5	4
13	13	12	11	10	9	17	16	15	14	4	3	2	1	0	8	7	6	5
14	14	13	12	11	10	9	17	16	15	5	4	3	2	1	0	8	7	6
15	15	14	13	12	11	10	9	17	16	6	5	4	3	2	1	0	8	7
16	16	15	14	13	12	11	10	9	17	7	6	5	4	3	2	1	0	8
17	17	16	15	14	13	12	11	10	9	8	7	6	5	4	3	2	1	0



D_{18} , dihedral, identity element $e = 0$, $a^9 = e$, $b^2 = e$, $ba = a^{-1}b$

	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17
0	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17
1	1	2	0	4	5	3	7	8	6	10	11	9	13	14	12	16	17	15
2	2	0	1	5	3	4	8	6	7	11	9	10	14	12	13	17	15	16
3	3	5	4	0	2	1	9	11	10	6	8	7	15	17	16	12	14	13
4	4	3	5	1	0	2	10	9	11	7	6	8	16	15	17	13	12	14
5	5	4	3	2	1	0	11	10	9	8	7	6	17	16	15	14	13	12
6	6	7	8	9	10	11	12	13	14	15	16	17	0	1	2	3	4	5
7	7	8	6	10	11	9	13	14	12	16	17	15	1	2	0	4	5	3
8	8	6	7	11	9	10	14	12	13	17	15	16	2	0	1	5	3	4
9	9	11	10	6	8	7	15	17	16	12	14	13	3	5	4	0	2	1
10	10	9	11	7	6	8	16	15	17	13	12	14	4	3	5	1	0	2
11	11	10	9	8	7	6	17	16	15	14	13	12	5	4	3	2	1	0
12	12	13	14	15	16	17	0	1	2	3	4	5	6	7	8	9	10	11
13	13	14	12	16	17	15	1	2	0	4	5	3	7	8	6	10	11	9
14	14	12	13	17	15	16	2	0	1	5	3	4	8	6	7	11	9	10
15	15	17	16	12	14	13	3	5	4	0	2	1	9	11	10	6	8	7
16	16	15	17	13	12	14	4	3	5	1	0	2	10	9	11	7	6	8
17	17	16	15	14	13	12	5	4	3	2	1	0	11	10	9	8	7	6

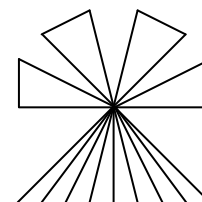
Cycle graph



$D_6 \times C_3$, solvable, identity element $e = 0$, $a^3 = e$, $b^2 = e$, $c^3 = e$, $ba = a^{-1}b$, $ca = ac$, $cb = bc$

	e	a	a ²	b	ab	a ² b	c	ac	a ² c	bc	abc	a ² bc	c ²	ac ²	a ² c ²	bc ²	abc ²	a ² bc ²
Element	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17
Order	1	3	3	2	2	2	3	3	3	6	6	6	3	3	3	6	6	6

Cycle graph


$$x^2 = e, y^3 = e, z^3 = e, yz = zy, yxy = x, zxz = x$$
[illegible]

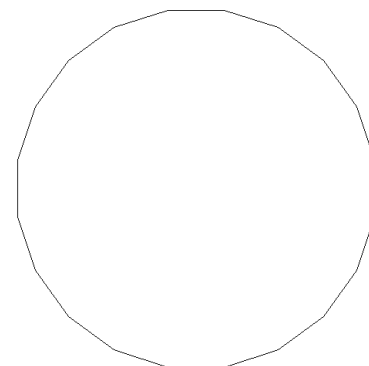
	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18
0	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18
1	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	0
2	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	0	1
3	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	0	1	2
4	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	0	1	2	3
5	5	6	7	8	9	10	11	12	13	14	15	16	17	18	0	1	2	3	4
6	6	7	8	9	10	11	12	13	14	15	16	17	18	0	1	2	3	4	5
7	7	8	9	10	11	12	13	14	15	16	17	18	0	1	2	3	4	5	6
8	8	9	10	11	12	13	14	15	16	17	18	0	1	2	3	4	5	6	7
9	9	10	11	12	13	14	15	16	17	18	0	1	2	3	4	5	6	7	8
10	10	11	12	13	14	15	16	17	18	0	1	2	3	4	5	6	7	8	9
11	11	12	13	14	15	16	17	18	0	1	2	3	4	5	6	7	8	9	10
12	12	13	14	15	16	17	18	0	1	2	3	4	5	6	7	8	9	10	11
13	13	14	15	16	17	18	0	1	2	3	4	5	6	7	8	9	10	11	12
14	14	15	16	17	18	0	1	2	3	4	5	6	7	8	9	10	11	12	13
15	15	16	17	18	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14
16	16	17	18	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15
17	17	18	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16
18	18	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17

[illegible]

Order 20 (5 groups)

	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19
0	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19
1	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	0
2	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	0	1
3	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	0	1	2
4	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	0	1	2	3
5	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	0	1	2	3	4
6	6	7	8	9	10	11	12	13	14	15	16	17	18	19	0	1	2	3	4	5
7	7	8	9	10	11	12	13	14	15	16	17	18	19	0	1	2	3	4	5	6
8	8	9	10	11	12	13	14	15	16	17	18	19	0	1	2	3	4	5	6	7
9	9	10	11	12	13	14	15	16	17	18	19	0	1	2	3	4	5	6	7	8
10	10	11	12	13	14	15	16	17	18	19	0	1	2	3	4	5	6	7	8	9
11	11	12	13	14	15	16	17	18	19	0	1	2	3	4	5	6	7	8	9	10
12	12	13	14	15	16	17	18	19	0	1	2	3	4	5	6	7	8	9	10	11
13	13	14	15	16	17	18	19	0	1	2	3	4	5	6	7	8	9	10	11	12
14	14	15	16	17	18	19	0	1	2	3	4	5	6	7	8	9	10	11	12	13
15	15	16	17	18	19	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14
16	16	17	18	19	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15
17	17	18	19	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16
18	18	19	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17
19	19	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18

Cycle graph

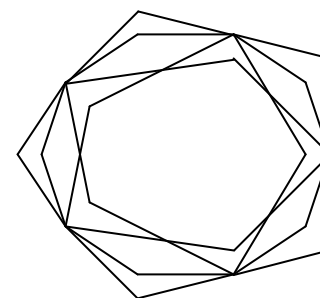


C_{20} , cyclic, identity element $e = 0$, $a^{20} = e$

	e	a	a ²	a ³	a ⁴	a ⁵	a ⁶	a ⁷	a ⁸	a ⁹	a ¹⁰	a ¹¹	a ¹²	a ¹³	a ¹⁴	a ¹⁵	a ¹⁶	a ¹⁷	a ¹⁸	a ¹⁹
Element	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19
Order	1	20	10	20	5	4	10	20	5	20	2	20	5	20	10	4	5	20	10	20

	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19
0	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19
1	1	2	3	4	5	6	7	8	9	0	11	12	13	14	15	16	17	18	19	10
2	2	3	4	5	6	7	8	9	0	1	12	13	14	15	16	17	18	19	10	11
3	3	4	5	6	7	8	9	0	1	2	13	14	15	16	17	18	19	10	11	12
4	4	5	6	7	8	9	0	1	2	3	14	15	16	17	18	19	10	11	12	13
5	5	6	7	8	9	0	1	2	3	4	15	16	17	18	19	10	11	12	13	14
6	6	7	8	9	0	1	2	3	4	5	16	17	18	19	10	11	12	13	14	15
7	7	8	9	0	1	2	3	4	5	6	17	18	19	10	11	12	13	14	15	16
8	8	9	0	1	2	3	4	5	6	7	18	19	10	11	12	13	14	15	16	17
9	9	0	1	2	3	4	5	6	7	8	19	10	11	12	13	14	15	16	17	18
10	10	11	12	13	14	15	16	17	18	19	0	1	2	3	4	5	6	7	8	9
11	11	12	13	14	15	16	17	18	19	10	1	2	3	4	5	6	7	8	9	0
12	12	13	14	15	16	17	18	19	10	11	2	3	4	5	6	7	8	9	0	1
13	13	14	15	16	17	18	19	10	11	12	3	4	5	6	7	8	9	0	1	2
14	14	15	16	17	18	19	10	11	12	13	4	5	6	7	8	9	0	1	2	3
15	15	16	17	18	19	10	11	12	13	14	5	6	7	8	9	0	1	2	3	4
16	16	17	18	19	10	11	12	13	14	15	6	7	8	9	0	1	2	3	4	5
17	17	18	19	10	11	12	13	14	15	16	7	8	9	0	1	2	3	4	5	6
18	18	19	10	11	12	13	14	15	16	17	8	9	0	1	2	3	4	5	6	7
19	19	10	11	12	13	14	15	16	17	18	9	0	1	2	3	4	5	6	7	8

Cycle graph

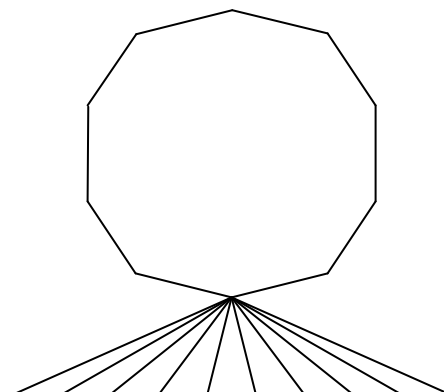


$C_{10} \times C_2$, abelian, identity element $e = 0$, $a^{10} = e$, $b^2 = e$, $ba = ab$

	e	a	a ²	a ³	a ⁴	a ⁵	a ⁶	a ⁷	a ⁸	a ⁹	b	ab	a ² b	a ³ b	a ⁴ b	a ⁵ b	a ⁶ b	a ⁷ b	a ⁸ b	a ⁹ b
Element	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19
Order	1	10	5	10	5	2	5	10	5	10	2	10	10	10	10	2	10	10	10	10

	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19
0	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19
1	1	2	3	4	5	6	7	8	9	0	11	12	13	14	15	16	17	18	19	10
2	2	3	4	5	6	7	8	9	0	1	12	13	14	15	16	17	18	19	10	11
3	3	4	5	6	7	8	9	0	1	2	13	14	15	16	17	18	19	10	11	12
4	4	5	6	7	8	9	0	1	2	3	14	15	16	17	18	19	10	11	12	13
5	5	6	7	8	9	0	1	2	3	4	15	16	17	18	19	10	11	12	13	14
6	6	7	8	9	0	1	2	3	4	5	16	17	18	19	10	11	12	13	14	15
7	7	8	9	0	1	2	3	4	5	6	17	18	19	10	11	12	13	14	15	16
8	8	9	0	1	2	3	4	5	6	7	18	19	10	11	12	13	14	15	16	17
9	9	0	1	2	3	4	5	6	7	8	19	10	11	12	13	14	15	16	17	18
10	10	19	18	17	16	15	14	13	12	11	0	9	8	7	6	5	4	3	2	1
11	11	10	19	18	17	16	15	14	13	12	1	0	9	8	7	6	5	4	3	2
12	12	11	10	19	18	17	16	15	14	13	2	1	0	9	8	7	6	5	4	3
13	13	12	11	10	19	18	17	16	15	14	3	2	1	0	9	8	7	6	5	4
14	14	13	12	11	10	19	18	17	16	15	4	3	2	1	0	9	8	7	6	5
15	15	14	13	12	11	10	19	18	17	16	5	4	3	2	1	0	9	8	7	6
16	16	15	14	13	12	11	10	19	18	17	6	5	4	3	2	1	0	9	8	7
17	17	16	15	14	13	12	11	10	19	18	7	6	5	4	3	2	1	0	9	8
18	18	17	16	15	14	13	12	11	10	19	8	7	6	5	4	3	2	1	0	9
19	19	18	17	16	15	14	13	12	11	10	9	8	7	6	5	4	3	2	1	0

Cycle graph

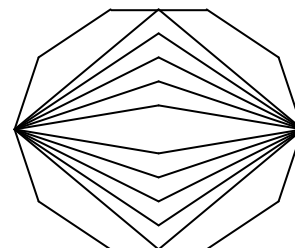


D_{20} , dihedral, identity element $e = 0$, $a^{10} = e$, $b^2 = e$, $ba = a^{-1}b$

[illegible]

	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19
0	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19
1	1	2	3	0	5	6	7	4	9	10	11	8	13	14	15	12	17	18	19	16
2	2	3	0	1	6	7	4	5	10	11	8	9	14	15	12	13	18	19	16	17
3	3	0	1	2	7	4	5	6	11	8	9	10	15	12	13	14	19	16	17	18
4	4	17	6	19	8	1	10	3	12	5	14	7	16	9	18	11	0	13	2	15
5	5	18	7	16	9	2	11	0	13	6	15	4	17	10	19	8	1	14	3	12
6	6	19	4	17	10	3	8	1	14	7	12	5	18	11	16	9	2	15	0	13
7	7	16	5	18	11	0	9	2	15	4	13	6	19	8	17	10	3	12	1	14
8	8	13	10	15	12	17	14	19	16	1	18	3	0	5	2	7	4	9	6	11
9	9	14	11	12	13	18	15	16	17	2	19	0	1	6	3	4	5	10	7	8
10	10	15	8	13	14	19	12	17	18	3	16	1	2	7	0	5	6	11	4	9
11	11	12	9	14	15	16	13	18	19	0	17	2	3	4	1	6	7	8	5	10
12	12	9	14	11	16	13	18	15	0	17	2	19	4	1	6	3	8	5	10	7
13	13	10	15	8	17	14	19	12	1	18	3	16	5	2	7	0	9	6	11	4
14	14	11	12	9	18	15	16	13	2	19	0	17	6	3	4	1	10	7	8	5
15	15	8	13	10	19	12	17	14	3	16	1	18	7	0	5	2	11	4	9	6
16	16	5	18	7	0	9	2	11	4	13	6	15	8	17	10	19	12	1	14	3
17	17	6	19	4	1	10	3	8	5	14	7	12	9	18	11	16	13	2	15	0
18	18	7	16	5	2	11	0	9	6	15	4	13	10	19	8	17	14	3	12	1
19	19	4	17	6	3	8	1	10	7	12	5	14	11	16	9	18	15	0	13	2

Cycle graph

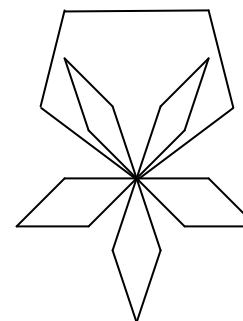


Semi-direct product of C_5 and C_4 , dicyclic group, solvable, identity element $e = 0$, $a^4 = e$, $b^5 = e$, $bab = a$

	e	a	a ²	a ³	b	ab	a ² b	a ³ b	b ²	ab ²	a ² b ²	a ³ b ²	b ³	ab ³	a ² b ³	a ³ b ³	b ⁴	ab ⁴	a ² b ⁴	a ³ b ⁴
Element	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19
Order	1	4	2	4	5	4	10	4	5	4	10	4	5	4	10	4	5	4	10	4

	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19
0	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19
1	1	2	3	0	5	6	7	4	9	10	11	8	13	14	15	12	17	18	19	16
2	2	3	0	1	6	7	4	5	10	11	8	9	14	15	12	13	18	19	16	17
3	3	0	1	2	7	4	5	6	11	8	9	10	15	12	13	14	19	16	17	18
4	4	9	18	15	8	13	2	19	12	17	6	3	16	1	10	7	0	5	14	11
5	5	10	19	12	9	14	3	16	13	18	7	0	17	2	11	4	1	6	15	8
6	6	11	16	13	10	15	0	17	14	19	4	1	18	3	8	5	2	7	12	9
7	7	8	17	14	11	12	1	18	15	16	5	2	19	0	9	6	3	4	13	10
8	8	17	14	7	12	1	18	11	16	5	2	15	0	9	6	19	4	13	10	3
9	9	18	15	4	13	2	19	8	17	6	3	12	1	10	7	16	5	14	11	0
10	10	19	12	5	14	3	16	9	18	7	0	13	2	11	4	17	6	15	8	1
11	11	16	13	6	15	0	17	10	19	4	1	14	3	8	5	18	7	12	9	2
12	12	5	10	19	16	9	14	3	0	13	18	7	4	17	2	11	8	1	6	15
13	13	6	11	16	17	10	15	0	1	14	19	4	5	18	3	8	9	2	7	12
14	14	7	8	17	18	11	12	1	2	15	16	5	6	19	0	9	10	3	4	13
15	15	4	9	18	19	8	13	2	3	12	17	6	7	16	1	10	11	0	5	14
16	16	13	6	11	0	17	10	15	4	1	14	19	8	5	18	3	12	9	2	7
17	17	14	7	8	1	18	11	12	5	2	15	16	9	6	19	0	13	10	3	4
18	18	15	4	9	2	19	8	13	6	3	12	17	10	7	16	1	14	11	0	5
19	19	12	5	10	3	16	9	14	7	0	13	18	11	4	17	2	15	8	1	6

Cycle graph



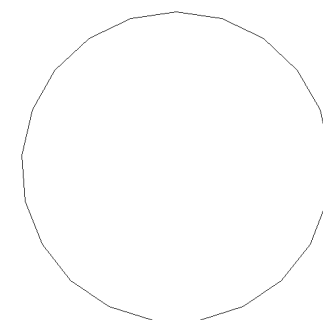
Frobenius group, solvable, identity element $e = 0$, $a^4 = e$, $b^5 = e$, $ba = ab^2$

	e	a	a ²	a ³	b	ab	a ² b	a ³ b	b ²	ab ²	a ² b ²	a ³ b ²	b ³	ab ³	a ² b ³	a ³ b ³	b ⁴	ab ⁴	a ² b ⁴	a ³ b ⁴
Element	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19
Order	1	4	2	4	5	4	2	4	5	4	2	4	5	4	2	4	5	4	2	4

Order 21 (2 groups)

	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20
0	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20
1	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	0
2	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	0	1
3	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	0	1	2
4	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	0	1	2	3
5	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	0	1	2	3	4
6	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	0	1	2	3	4	5
7	7	8	9	10	11	12	13	14	15	16	17	18	19	20	0	1	2	3	4	5	6
8	8	9	10	11	12	13	14	15	16	17	18	19	20	0	1	2	3	4	5	6	7
9	9	10	11	12	13	14	15	16	17	18	19	20	0	1	2	3	4	5	6	7	8
10	10	11	12	13	14	15	16	17	18	19	20	0	1	2	3	4	5	6	7	8	9
11	11	12	13	14	15	16	17	18	19	20	0	1	2	3	4	5	6	7	8	9	10
12	12	13	14	15	16	17	18	19	20	0	1	2	3	4	5	6	7	8	9	10	11
13	13	14	15	16	17	18	19	20	0	1	2	3	4	5	6	7	8	9	10	11	12
14	14	15	16	17	18	19	20	0	1	2	3	4	5	6	7	8	9	10	11	12	13
15	15	16	17	18	19	20	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14
16	16	17	18	19	20	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15
17	17	18	19	20	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16
18	18	19	20	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17
19	19	20	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18
20	20	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19

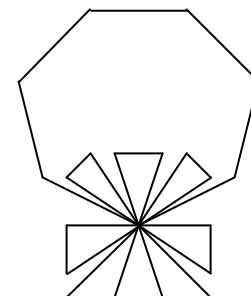
Cycle graph



C_{21} , cyclic, identity element $e = 0$, $a^{21} = e$

	e	a	a ²	a ³	a ⁴	a ⁵	a ⁶	a ⁷	a ⁸	a ⁹	a ¹⁰	a ¹¹	a ¹²	a ¹³	a ¹⁴	a ¹⁵	a ¹⁶	a ¹⁷	a ¹⁸	a ¹⁹	a ²⁰
Element	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20
Order	1	21	21	7	21	21	7	3	21	7	21	21	7	21	3	7	21	21	7	21	21

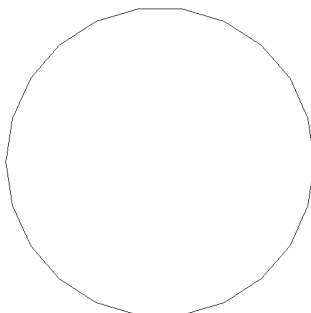
Cycle graph

[illegible]

Order 22 (2 groups)

	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21
0	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21
1	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	0
2	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	0	1
3	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	0	1	2
4	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	0	1	2	3
5	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	0	1	2	3	4
6	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	0	1	2	3	4	5
7	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	0	1	2	3	4	5	6
8	8	9	10	11	12	13	14	15	16	17	18	19	20	21	0	1	2	3	4	5	6	7
9	9	10	11	12	13	14	15	16	17	18	19	20	21	0	1	2	3	4	5	6	7	8
10	10	11	12	13	14	15	16	17	18	19	20	21	0	1	2	3	4	5	6	7	8	9
11	11	12	13	14	15	16	17	18	19	20	21	0	1	2	3	4	5	6	7	8	9	10
12	12	13	14	15	16	17	18	19	20	21	0	1	2	3	4	5	6	7	8	9	10	11
13	13	14	15	16	17	18	19	20	21	0	1	2	3	4	5	6	7	8	9	10	11	12
14	14	15	16	17	18	19	20	21	0	1	2	3	4	5	6	7	8	9	10	11	12	13
15	15	16	17	18	19	20	21	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14
16	16	17	18	19	20	21	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15
17	17	18	19	20	21	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16
18	18	19	20	21	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17
19	19	20	21	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18
20	20	21	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19
21	21	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20

Cycle graph



C_{22} , cyclic, identity element $e = 0$, $a^{22} = e$

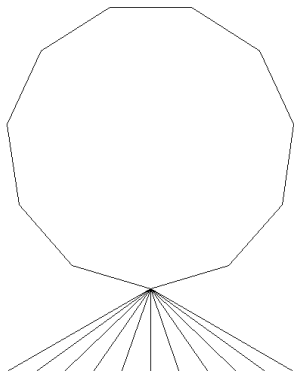
	e	a	a ²	a ³	a ⁴	a ⁵	a ⁶	a ⁷	a ⁸	a ⁹	a ¹⁰	a ¹¹	a ¹²	a ¹³	a ¹⁴	a ¹⁵	a ¹⁶	a ¹⁷	a ¹⁸	a ¹⁹	a ²⁰	a ²¹
Element	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21
Order	1	22	11	22	11	22	11	22	11	22	11	2	11	22	11	22	11	22	11	22	11	22

	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21
0	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21
1	1	2	3	4	5	6	7	8	9	10	0	12	13	14	15	16	17	18	19	20	21	11
2	2	3	4	5	6	7	8	9	10	0	1	13	14	15	16	17	18	19	20	21	11	12
3	3	4	5	6	7	8	9	10	0	1	2	14	15	16	17	18	19	20	21	11	12	13
4	4	5	6	7	8	9	10	0	1	2	3	15	16	17	18	19	20	21	11	12	13	14
5	5	6	7	8	9	10	0	1	2	3	4	16	17	18	19	20	21	11	12	13	14	15
6	6	7	8	9	10	0	1	2	3	4	5	17	18	19	20	21	11	12	13	14	15	16
7	7	8	9	10	0	1	2	3	4	5	6	18	19	20	21	11	12	13	14	15	16	17
8	8	9	10	0	1	2	3	4	5	6	7	19	20	21	11	12	13	14	15	16	17	18
9	9	10	0	1	2	3	4	5	6	7	8	20	21	11	12	13	14	15	16	17	18	19
10	10	0	1	2	3	4	5	6	7	8	9	21	11	12	13	14	15	16	17	18	19	20
11	11	21	20	19	18	17	16	15	14	13	12	0	10	9	8	7	6	5	4	3	2	1
12	12	11	21	20	19	18	17	16	15	14	13	1	0	10	9	8	7	6	5	4	3	2
13	13	12	11	21	20	19	18	17	16	15	14	2	1	0	10	9	8	7	6	5	4	3
14	14	13	12	11	21	20	19	18	17	16	15	3	2	1	0	10	9	8	7	6	5	4
15	15	14	13	12	11	21	20	19	18	17	16	4	3	2	1	0	10	9	8	7	6	5
16	16	15	14	13	12	11	21	20	19	18	17	5	4	3	2	1	0	10	9	8	7	6
17	17	16	15	14	13	12	11	21	20	19	18	6	5	4	3	2	1	0	10	9	8	7
18	18	17	16	15	14	13	12	11	21	20	19	7	6	5	4	3	2	1	0	10	9	8
19	19	18	17	16	15	14	13	12	11	21	20	8	7	6	5	4	3	2	1	0	10	9
20	20	19	18	17	16	15	14	13	12	11	21	9	8	7	6	5	4	3	2	1	0	10
21	21	20	19	18	17	16	15	14	13	12	11	10	9	8	7	6	5	4	3	2	1	0


D_{22} , dihedral, identity element $e = 0$, $a^{11} = e$, $b^2 = e$, $ba = a^{-1}b$

	e	a	a ²	a ³	a ⁴	a ⁵	a ⁶	a ⁷	a ⁸	a ⁹	a ¹⁰	b	ab	a ² b	a ³ b	a ⁴ b	a ⁵ b	a ⁶ b	a ⁷ b	a ⁸ b	a ⁹ b	a ¹⁰ b
Element	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21
Order	1	11	11	11	11	11	11	11	11	11	11	2	2	2	2	2	2	2	2	2	2	2

Cycle graph



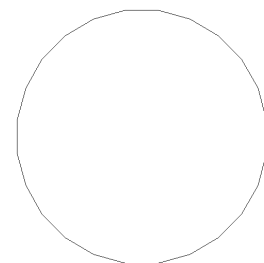
	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22
0	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22
1	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	0
2	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	0	1
3	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	0	1	2
4	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	0	1	2	3
5	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	0	1	2	3	4
6	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	0	1	2	3	4	5
7	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	0	1	2	3	4	5	6
8	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	0	1	2	3	4	5	6	7
9	9	10	11	12	13	14	15	16	17	18	19	20	21	22	0	1	2	3	4	5	6	7	8
10	10	11	12	13	14	15	16	17	18	19	20	21	22	0	1	2	3	4	5	6	7	8	9
11	11	12	13	14	15	16	17	18	19	20	21	22	0	1	2	3	4	5	6	7	8	9	10
12	12	13	14	15	16	17	18	19	20	21	22	0	1	2	3	4	5	6	7	8	9	10	11
13	13	14	15	16	17	18	19	20	21	22	0	1	2	3	4	5	6	7	8	9	10	11	12
14	14	15	16	17	18	19	20	21	22	0	1	2	3	4	5	6	7	8	9	10	11	12	13
15	15	16	17	18	19	20	21	22	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14
16	16	17	18	19	20	21	22	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15
17	17	18	19	20	21	22	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16
18	18	19	20	21	22	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17
19	19	20	21	22	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18
20	20	21	22	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19
21	21	22	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20
22	22	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21

[illegible]

Order 24 (15 groups)

	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23
0	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23
1	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23	0
2	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23	0	1
3	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23	0	1	2
4	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23	0	1	2	3
5	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23	0	1	2	3	4
6	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23	0	1	2	3	4	5
7	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23	0	1	2	3	4	5	6
8	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23	0	1	2	3	4	5	6	7
9	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23	0	1	2	3	4	5	6	7	8
10	10	11	12	13	14	15	16	17	18	19	20	21	22	23	0	1	2	3	4	5	6	7	8	9
11	11	12	13	14	15	16	17	18	19	20	21	22	23	0	1	2	3	4	5	6	7	8	9	10
12	12	13	14	15	16	17	18	19	20	21	22	23	0	1	2	3	4	5	6	7	8	9	10	11
13	13	14	15	16	17	18	19	20	21	22	23	0	1	2	3	4	5	6	7	8	9	10	11	12
14	14	15	16	17	18	19	20	21	22	23	0	1	2	3	4	5	6	7	8	9	10	11	12	13
15	15	16	17	18	19	20	21	22	23	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14
16	16	17	18	19	20	21	22	23	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15
17	17	18	19	20	21	22	23	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16
18	18	19	20	21	22	23	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17
19	19	20	21	22	23	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18
20	20	21	22	23	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19
21	21	22	23	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20
22	22	23	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21
23	23	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22

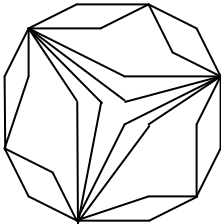
Cycle graph


 $C_{24} = C_8 \times C_3$, cyclic, identity element $e = 0$, $a^{24} = e$

	e	a	a ²	a ³	a ⁴	a ⁵	a ⁶	a ⁷	a ⁸	a ⁹	a ¹⁰	a ¹¹	a ¹²	a ¹³	a ¹⁴	a ¹⁵	a ¹⁶	a ¹⁷	a ¹⁸	a ¹⁹	a ²⁰	a ²¹	a ²²	a ²³
Element	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23
Order	1	24	12	8	6	24	4	24	3	8	12	24	2	24	12	8	3	24	4	24	6	8	12	24

	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23
0	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23
1	1	2	3	4	5	6	7	8	9	10	11	0	13	14	15	16	17	18	19	20	21	22	23	12
2	2	3	4	5	6	7	8	9	10	11	0	1	14	15	16	17	18	19	20	21	22	23	12	13
3	3	4	5	6	7	8	9	10	11	0	1	2	15	16	17	18	19	20	21	22	23	12	13	14
4	4	5	6	7	8	9	10	11	0	1	2	3	16	17	18	19	20	21	22	23	12	13	14	15
5	5	6	7	8	9	10	11	0	1	2	3	4	17	18	19	20	21	22	23	12	13	14	15	16
6	6	7	8	9	10	11	0	1	2	3	4	5	18	19	20	21	22	23	12	13	14	15	16	17
7	7	8	9	10	11	0	1	2	3	4	5	6	19	20	21	22	23	12	13	14	15	16	17	18
8	8	9	10	11	0	1	2	3	4	5	6	7	20	21	22	23	12	13	14	15	16	17	18	19
9	9	10	11	0	1	2	3	4	5	6	7	8	21	22	23	12	13	14	15	16	17	18	19	20
10	10	11	0	1	2	3	4	5	6	7	8	9	22	23	12	13	14	15	16	17	18	19	20	21
11	11	0	1	2	3	4	5	6	7	8	9	10	23	12	13	14	15	16	17	18	19	20	21	22
12	12	13	14	15	16	17	18	19	20	21	22	23	0	1	2	3	4	5	6	7	8	9	10	11
13	13	14	15	16	17	18	19	20	21	22	23	12	1	2	3	4	5	6	7	8	9	10	11	0
14	14	15	16	17	18	19	20	21	22	23	12	13	2	3	4	5	6	7	8	9	10	11	0	1
15	15	16	17	18	19	20	21	22	23	12	13	14	3	4	5	6	7	8	9	10	11	0	1	2
16	16	17	18	19	20	21	22	23	12	13	14	15	4	5	6	7	8	9	10	11	0	1	2	3
17	17	18	19	20	21	22	23	12	13	14	15	16	5	6	7	8	9	10	11	0	1	2	3	4
18	18	19	20	21	22	23	12	13	14	15	16	17	6	7	8	9	10	11	0	1	2	3	4	5
19	19	20	21	22	23	12	13	14	15	16	17	18	7	8	9	10	11	0	1	2	3	4	5	6
20	20	21	22	23	12	13	14	15	16	17	18	19	8	9	10	11	0	1	2	3	4	5	6	7
21	21	22	23	12	13	14	15	16	17	18	19	20	9	10	11	0	1	2	3	4	5	6	7	8
22	22	23	12	13	14	15	16	17	18	19	20	21	10	11	0	1	2	3	4	5	6	7	8	9
23	23	12	13	14	15	16	17	18	19	20	21	22	11	0	1	2	3	4	5	6	7	8	9	10

Cycle graph

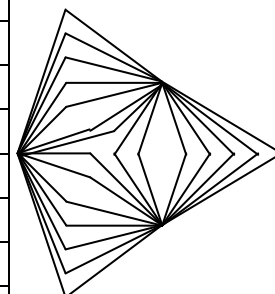


$C_{12} \times C_2 = C_6 \times C_4$, abelian, identity element $e = 0$, $a^{12} = e$, $b^2 = e$, $ba = ab$

	e	a	a ²	a ³	a ⁴	a ⁵	a ⁶	a ⁷	a ⁸	a ⁹	a ¹⁰	a ¹¹	b	ab	a ² b	a ³ b	a ⁴ b	a ⁵ b	a ⁶ b	a ⁷ b	a ⁸ b	a ⁹ b	a ¹⁰ b	a ¹¹ b
Element	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23
Order	1	12	6	4	3	12	2	12	3	4	6	12	2	12	6	4	6	12	2	12	6	4	6	12

	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23
0	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23
1	1	2	3	4	5	0	7	8	9	10	11	6	13	14	15	16	17	12	19	20	21	22	23	18
2	2	3	4	5	0	1	8	9	10	11	6	7	14	15	16	17	12	13	20	21	22	23	18	19
3	3	4	5	0	1	2	9	10	11	6	7	8	15	16	17	12	13	14	21	22	23	18	19	20
4	4	5	0	1	2	3	10	11	6	7	8	9	16	17	12	13	14	15	22	23	18	19	20	21
5	5	0	1	2	3	4	11	6	7	8	9	10	17	12	13	14	15	16	23	18	19	20	21	22
6	6	7	8	9	10	11	0	1	2	3	4	5	18	19	20	21	22	23	12	13	14	15	16	17
7	7	8	9	10	11	6	1	2	3	4	5	0	19	20	21	22	23	18	13	14	15	16	17	12
8	8	9	10	11	6	7	2	3	4	5	0	1	20	21	22	23	18	19	14	15	16	17	12	13
9	9	10	11	6	7	8	3	4	5	0	1	2	21	22	23	18	19	20	15	16	17	12	13	14
10	10	11	6	7	8	9	4	5	0	1	2	3	22	23	18	19	20	21	16	17	12	13	14	15
11	11	6	7	8	9	10	5	0	1	2	3	4	23	18	19	20	21	22	17	12	13	14	15	16
12	12	13	14	15	16	17	18	19	20	21	22	23	0	1	2	3	4	5	6	7	8	9	10	11
13	13	14	15	16	17	12	19	20	21	22	23	18	1	2	3	4	5	0	7	8	9	10	11	6
14	14	15	16	17	12	13	20	21	22	23	18	19	2	3	4	5	0	1	8	9	10	11	6	7
15	15	16	17	12	13	14	21	22	23	18	19	20	3	4	5	0	1	2	9	10	11	6	7	8
16	16	17	12	13	14	15	22	23	18	19	20	21	4	5	0	1	2	3	10	11	6	7	8	9
17	17	12	13	14	15	16	23	18	19	20	21	22	5	0	1	2	3	4	11	6	7	8	9	10
18	18	19	20	21	22	23	12	13	14	15	16	17	6	7	8	9	10	11	0	1	2	3	4	5
19	19	20	21	22	23	18	13	14	15	16	17	12	7	8	9	10	11	6	1	2	3	4	5	0
20	20	21	22	23	18	19	14	15	16	17	12	13	8	9	10	11	6	7	2	3	4	5	0	1
21	21	22	23	18	19	20	15	16	17	12	13	14	9	10	11	6	7	8	3	4	5	0	1	2
22	22	23	18	19	20	21	16	17	12	13	14	15	10	11	6	7	8	9	4	5	0	1	2	3
23	23	18	19	20	21	22	17	12	13	14	15	16	11	6	7	8	9	10	5	0	1	2	3	4

Cycle graph

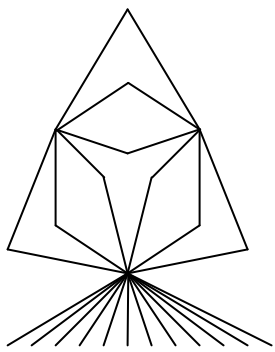


$C_6 \times C_2^2 = C_3 \times C_2^3$, abelian, identity element $e = 0$, $a^6 = e$, $b^2 = e$, $c^2 = e$, $ba = ab$, $ca = ac$, $cb = bc$

[illegible]

	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23
0	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23
1	1	2	3	4	5	0	7	8	9	10	11	6	13	14	15	16	17	12	19	20	21	22	23	18
2	2	3	4	5	0	1	8	9	10	11	6	7	14	15	16	17	12	13	20	21	22	23	18	19
3	3	4	5	0	1	2	9	10	11	6	7	8	15	16	17	12	13	14	21	22	23	18	19	20
4	4	5	0	1	2	3	10	11	6	7	8	9	16	17	12	13	14	15	22	23	18	19	20	21
5	5	0	1	2	3	4	11	6	7	8	9	10	17	12	13	14	15	16	23	18	19	20	21	22
6	6	11	10	9	8	7	0	5	4	3	2	1	18	23	22	21	20	19	12	17	16	15	14	13
7	7	6	11	10	9	8	1	0	5	4	3	2	19	18	23	22	21	20	13	12	17	16	15	14
8	8	7	6	11	10	9	2	1	0	5	4	3	20	19	18	23	22	21	14	13	12	17	16	15
9	9	8	7	6	11	10	3	2	1	0	5	4	21	20	19	18	23	22	15	14	13	12	17	16
10	10	9	8	7	6	11	4	3	2	1	0	5	22	21	20	19	18	23	16	15	14	13	12	17
11	11	10	9	8	7	6	5	4	3	2	1	0	23	22	21	20	19	18	17	16	15	14	13	12
12	12	13	14	15	16	17	18	19	20	21	22	23	0	1	2	3	4	5	6	7	8	9	10	11
13	13	14	15	16	17	12	19	20	21	22	23	18	1	2	3	4	5	0	7	8	9	10	11	6
14	14	15	16	17	12	13	20	21	22	23	18	19	2	3	4	5	0	1	8	9	10	11	6	7
15	15	16	17	12	13	14	21	22	23	18	19	20	3	4	5	0	1	2	9	10	11	6	7	8
16	16	17	12	13	14	15	22	23	18	19	20	21	4	5	0	1	2	3	10	11	6	7	8	9
17	17	12	13	14	15	16	23	18	19	20	21	22	5	0	1	2	3	4	11	6	7	8	9	10
18	18	23	22	21	20	19	12	17	16	15	14	13	6	11	10	9	8	7	0	5	4	3	2	1
19	19	18	23	22	21	20	13	12	17	16	15	14	7	6	11	10	9	8	1	0	5	4	3	2
20	20	19	18	23	22	21	14	13	12	17	16	15	8	7	6	11	10	9	2	1	0	5	4	3
21	21	20	19	18	23	22	15	14	13	12	17	16	9	8	7	6	11	10	3	2	1	0	5	4
22	22	21	20	19	18	23	16	15	14	13	12	17	10	9	8	7	6	11	4	3	2	1	0	5
23	23	22	21	20	19	18	17	16	15	14	13	12	11	10	9	8	7	6	5	4	3	2	1	0

Cycle graph

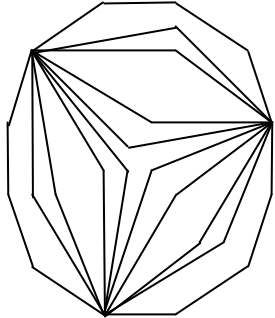


$D_{12} \times C_2 = D_6 \times C_2^2 = \text{dihedral}(C_6 \times C_2)$, solvable, identity element $e = 0$, $a^6 = e$, $b^2 = e$, $c^2 = e$, $ba = a^{-1}b$, $ca = ac$, $cb = bc$

	e	a	a ²	a ³	a ⁴	a ⁵	b	ab	a ² b	a ³ b	a ⁴ b	a ⁵ b	c	ac	a ² c	a ³ c	a ⁴ c	a ⁵ c	bc	abc	a ² bc	a ³ bc	a ⁴ bc	a ⁵ bc
Element	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23
Order	1	6	3	2	3	6	2	2	2	2	2	2	2	6	6	2	6	6	2	2	2	2	2	2

	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23
0	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23
1	1	2	3	0	5	6	7	4	9	10	11	8	13	14	15	12	17	18	19	16	21	22	23	20
2	2	3	0	1	6	7	4	5	10	11	8	9	14	15	12	13	18	19	16	17	22	23	20	21
3	3	0	1	2	7	4	5	6	11	8	9	10	15	12	13	14	19	16	17	18	23	20	21	22
4	4	7	6	5	0	3	2	1	12	15	14	13	8	11	10	9	20	23	22	21	16	19	18	17
5	5	4	7	6	1	0	3	2	13	12	15	14	9	8	11	10	21	20	23	22	17	16	19	18
6	6	5	4	7	2	1	0	3	14	13	12	15	10	9	8	11	22	21	20	23	18	17	16	19
7	7	6	5	4	3	2	1	0	15	14	13	12	11	10	9	8	23	22	21	20	19	18	17	16
8	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23	0	1	2	3	4	5	6	7
9	9	10	11	8	13	14	15	12	17	18	19	16	21	22	23	20	1	2	3	0	5	6	7	4
10	10	11	8	9	14	15	12	13	18	19	16	17	22	23	20	21	2	3	0	1	6	7	4	5
11	11	8	9	10	15	12	13	14	19	16	17	18	23	20	21	22	3	0	1	2	7	4	5	6
12	12	15	14	13	8	11	10	9	20	23	22	21	16	19	18	17	4	7	6	5	0	3	2	1
13	13	12	15	14	9	8	11	10	21	20	23	22	17	16	19	18	5	4	7	6	1	0	3	2
14	14	13	12	15	10	9	8	11	22	21	20	23	18	17	16	19	6	5	4	7	2	1	0	3
15	15	14	13	12	11	10	9	8	23	22	21	20	19	18	17	16	7	6	5	4	3	2	1	0
16	16	17	18	19	20	21	22	23	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15
17	17	18	19	16	21	22	23	20	1	2	3	0	5	6	7	4	9	10	11	8	13	14	15	12
18	18	19	16	17	22	23	20	21	2	3	0	1	6	7	4	5	10	11	8	9	14	15	12	13
19	19	16	17	18	23	20	21	22	3	0	1	2	7	4	5	6	11	8	9	10	15	12	13	14
20	20	23	22	21	16	19	18	17	4	7	6	5	0	3	2	1	12	15	14	13	8	11	10	9
21	21	20	23	22	17	16	19	18	5	4	7	6	1	0	3	2	13	12	15	14	9	8	11	10
22	22	21	20	23	18	17	16	19	6	5	4	7	2	1	0	3	14	13	12	15	10	9	8	11
23	23	22	21	20	19	18	17	16	7	6	5	4	3	2	1	0	15	14	13	12	11	10	9	8

Cycle graph



$D_8 \times C_3$ = semi-direct product of C_2^2 and C_6 , nilpotent, identity element $e = 0$, $a^4 = e$, $b^2 = e$, $c^3 = e$,
 $ba = a^{-1}b$, $ca = ac$, $cb = bc$

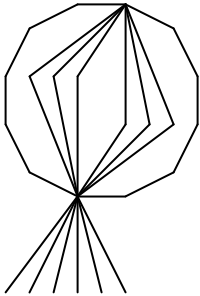
	e	a	a ²	a ³	b	ab	a ² b	a ³ b	c	ac	a ² c	a ³ c	bc	abc	a ² bc	a ³ bc	c ²	ac ²	a ² c ²	a ³ c ²	bc ²	abc ²	a ² bc ²	a ³ bc ²
Element	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23
Order	1	4	2	4	2	2	2	2	3	12	6	12	6	6	6	6	3	12	6	12	6	6	6	6

	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23
0	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23
1	1	2	0	4	5	3	7	8	6	10	11	9	13	14	12	16	17	15	19	20	18	22	23	21
2	2	0	1	5	3	4	8	6	7	11	9	10	14	12	13	17	15	16	20	18	19	23	21	22
3	3	5	4	0	2	1	9	11	10	6	8	7	15	17	16	12	14	13	21	23	22	18	20	19
4	4	3	5	1	0	2	10	9	11	7	6	8	16	15	17	13	12	14	22	21	23	19	18	20
5	5	4	3	2	1	0	11	10	9	8	7	6	17	16	15	14	13	12	23	22	21	20	19	18
6	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23	0	1	2	3	4	5
7	7	8	6	10	11	9	13	14	12	16	17	15	19	20	18	22	23	21	1	2	0	4	5	3
8	8	6	7	11	9	10	14	12	13	17	15	16	20	18	19	23	21	22	2	0	1	5	3	4
9	9	11	10	6	8	7	15	17	16	12	14	13	21	23	22	18	20	19	3	5	4	0	2	1
10	10	9	11	7	6	8	16	15	17	13	12	14	22	21	23	19	18	20	4	3	5	1	0	2
11	11	10	9	8	7	6	17	16	15	14	13	12	23	22	21	20	19	18	5	4	3	2	1	0
12	12	13	14	15	16	17	18	19	20	21	22	23	0	1	2	3	4	5	6	7	8	9	10	11
13	13	14	12	16	17	15	19	20	18	22	23	21	1	2	0	4	5	3	7	8	6	10	11	9
14	14	12	13	17	15	16	20	18	19	23	21	22	2	0	1	5	3	4	8	6	7	11	9	10
15	15	17	16	12	14	13	21	23	22	18	20	19	3	5	4	0	2	1	9	11	10	6	8	7
16	16	15	17	13	12	14	22	21	23	19	18	20	4	3	5	1	0	2	10	9	11	7	6	8
17	17	16	15	14	13	12	23	22	21	20	19	18	5	4	3	2	1	0	11	10	9	8	7	6
18	18	19	20	21	22	23	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17
19	19	20	18	22	23	21	1	2	0	4	5	3	7	8	6	10	11	9	13	14	12	16	17	15
20	20	18	19	23	21	22	2	0	1	5	3	4	8	6	7	11	9	10	14	12	13	17	15	16
21	21	23	22	18	20	19	3	5	4	0	2	1	9	11	10	6	8	7	15	17	16	12	14	13
22	22	21	23	19	18	20	4	3	5	1	0	2	10	9	11	7	6	8	16	15	17	13	12	14
23	23	22	21	20	19	18	5	4	3	2	1	0	11	10	9	8	7	6	17	16	15	14	13	12

$D_6 \times C_4$, solvable, identity element $e = 0$, $a^3 = e$, $b^2 = e$, $c^4 = e$, $ba = a^{-1}b$, $ca = ac$, $cb = bc$

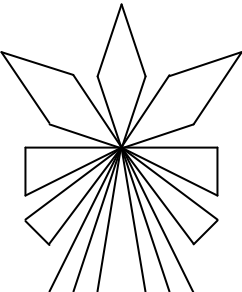
	e	a	a ²	b	ab	a ² b	c	ac	a ² c	bc	abc	a ² bc	c ²	ac ²	a ² c ²	bc ²	abc ²	a ² bc ²	c ³	ac ³	a ² c ³	bc ³	abc ³	a ² bc ³
Element	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23
Order	1	3	3	2	2	2	4	12	12	4	4	4	2	6	6	2	2	2	4	12	12	4	4	4

Cycle graph



	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23
0	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23
1	1	0	3	2	5	4	7	6	9	8	11	10	13	12	15	14	17	16	19	18	21	20	23	22
2	2	4	0	5	1	3	8	10	6	11	7	9	14	16	12	17	13	15	20	22	18	23	19	21
3	3	5	1	4	0	2	9	11	7	10	6	8	15	17	13	16	12	14	21	23	19	22	18	20
4	4	2	5	0	3	1	10	8	11	6	9	7	16	14	17	12	15	13	22	20	23	18	21	19
5	5	3	4	1	2	0	11	9	10	7	8	6	17	15	16	13	14	12	23	21	22	19	20	18
6	6	7	12	13	18	19	0	1	14	15	20	21	2	3	8	9	22	23	4	5	10	11	16	17
7	7	6	13	12	19	18	1	0	15	14	21	20	3	2	9	8	23	22	5	4	11	10	17	16
8	8	10	14	16	20	22	2	4	12	17	18	23	0	5	6	11	19	21	1	3	7	9	13	15
9	9	11	15	17	21	23	3	5	13	16	19	22	1	4	7	10	18	20	0	2	6	8	12	14
10	10	8	16	14	22	20	4	2	17	12	23	18	5	0	11	6	21	19	3	1	9	7	15	13
11	11	9	17	15	23	21	5	3	16	13	22	19	4	1	10	7	20	18	2	0	8	6	14	12
12	12	18	6	19	7	13	14	20	0	21	1	15	8	22	2	23	3	9	10	16	4	17	5	11
13	13	19	7	18	6	12	15	21	1	20	0	14	9	23	3	22	2	8	11	17	5	16	4	10
14	14	20	8	22	10	16	12	18	2	23	4	17	6	19	0	21	5	11	7	13	1	15	3	9
15	15	21	9	23	11	17	13	19	3	22	5	16	7	18	1	20	4	10	6	12	0	14	2	8
16	16	22	10	20	8	14	17	23	4	18	2	12	11	21	5	19	0	6	9	15	3	13	1	7
17	17	23	11	21	9	15	16	22	5	19	3	13	10	20	4	18	1	7	8	14	2	12	0	6
18	18	12	19	6	13	7	20	14	21	0	15	1	22	8	23	2	9	3	16	10	17	4	11	5
19	19	13	18	7	12	6	21	15	20	1	14	0	23	9	22	3	8	2	17	11	16	5	10	4
20	20	14	22	8	16	10	18	12	23	2	17	4	19	6	21	0	11	5	13	7	15	1	9	3
21	21	15	23	9	17	11	19	13	22	3	16	5	18	7	20	1	10	4	12	6	14	0	8	2
22	22	16	20	10	14	8	23	17	18	4	12	2	21	11	19	5	6	0	15	9	13	3	7	1
23	23	17	21	11	15	9	22	16	19	5	13	3	20	10	18	4	7	1	14	8	12	2	6	0

Cycle graph

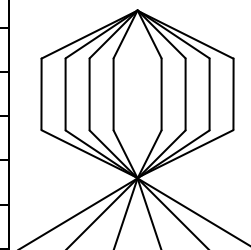


S_4 , solvable, identity element $e = 0$, $(1\ 2\ 3\ 4)$, is rather that symmetry group of order 24, that is being formed by using all permutations upon four elements, under composition operation. A_4 , alternating group of order 12, is a subgroup of this group.

	1234	1243	1324	1342	1423	1432	2134	2143	2314	2341	2413	2431	3124	3142	3214	3241	3412	3421	4123	4132	4213	4231	4312	4321
Element	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23
Order	1	2	2	3	3	2	2	2	3	4	4	3	3	4	2	3	2	4	4	3	3	2	4	2

	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23
0	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23
1	1	0	3	2	5	4	7	6	9	8	11	10	13	12	15	14	17	16	19	18	21	20	23	22
2	2	3	0	1	6	7	4	5	10	11	8	9	14	15	12	13	18	19	16	17	22	23	20	21
3	3	2	1	0	7	6	5	4	11	10	9	8	15	14	13	12	19	18	17	16	23	22	21	20
4	4	7	5	6	8	11	9	10	0	3	1	2	16	19	17	18	20	23	21	22	12	15	13	14
5	5	6	4	7	9	10	8	11	1	2	0	3	17	18	16	19	21	22	20	23	13	14	12	15
6	6	5	7	4	10	9	11	8	2	1	3	0	18	17	19	16	22	21	23	20	14	13	15	12
7	7	4	6	5	11	8	10	9	3	0	2	1	19	16	18	17	23	20	22	21	15	12	14	13
8	8	10	11	9	0	2	3	1	4	6	7	5	20	22	23	21	12	14	15	13	16	18	19	17
9	9	11	10	8	1	3	2	0	5	7	6	4	21	23	22	20	13	15	14	12	17	19	18	16
10	10	8	9	11	2	0	1	3	6	4	5	7	22	20	21	23	14	12	13	15	18	16	17	19
11	11	9	8	10	3	1	0	2	7	5	4	6	23	21	20	22	15	13	12	14	19	17	16	18
12	12	13	14	15	16	17	18	19	20	21	22	23	0	1	2	3	4	5	6	7	8	9	10	11
13	13	12	15	14	17	16	19	18	21	20	23	22	1	0	3	2	5	4	7	6	9	8	11	10
14	14	15	12	13	18	19	16	17	22	23	20	21	2	3	0	1	6	7	4	5	10	11	8	9
15	15	14	13	12	19	18	17	16	23	22	21	20	3	2	1	0	7	6	5	4	11	10	9	8
16	16	19	17	18	20	23	21	22	12	15	13	14	4	7	5	6	8	11	9	10	0	3	1	2
17	17	18	16	19	21	22	20	23	13	14	12	15	5	6	4	7	9	10	8	11	1	2	0	3
18	18	17	19	16	22	21	23	20	14	13	15	12	6	5	7	4	10	9	11	8	2	1	3	0
19	19	16	18	17	23	20	22	21	15	12	14	13	7	4	6	5	11	8	10	9	3	0	2	1
20	20	22	23	21	12	14	15	13	16	18	19	17	8	10	11	9	0	2	3	1	4	6	7	5
21	21	23	22	20	13	15	14	12	17	19	18	16	9	11	10	8	1	3	2	0	5	7	6	4
22	22	20	21	23	14	12	13	15	18	16	17	19	10	8	9	11	2	0	1	3	6	4	5	7
23	23	21	20	22	15	13	12	14	19	17	16	18	11	9	8	10	3	1	0	2	7	5	4	6

Cycle graph



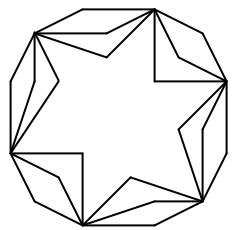
$A_4 \times C_2$ = semi direct product of C_2^3 and C_3 , solvable, identity element $e = 0$,

$a^2 = e, b^2 = e, c^3 = e, d^2 = e, ba = ab, ca = abc, cb = ac, da = ad, db = bd, dc = cd$

	e	a	b	ab	c	ac	bc	abc	c ²	ac ²	bc ²	abc ²	d	ad	bd	abd	cd	acd	bcd	abcd	c ² d	ac ² d	bc ² d	abc ² d
Element	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23
Order	1	2	2	2	3	3	3	3	3	3	3	3	2	2	2	2	6	6	6	6	6	6	6	6

	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23
0	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23
1	1	2	3	0	5	6	7	4	9	10	11	8	13	14	15	12	17	18	19	16	21	22	23	20
2	2	3	0	1	6	7	4	5	10	11	8	9	14	15	12	13	18	19	16	17	22	23	20	21
3	3	0	1	2	7	4	5	6	11	8	9	10	15	12	13	14	19	16	17	18	23	20	21	22
4	4	7	6	5	2	1	0	3	12	15	14	13	10	9	8	11	20	23	22	21	18	17	16	19
5	5	4	7	6	3	2	1	0	13	12	15	14	11	10	9	8	21	20	23	22	19	18	17	16
6	6	5	4	7	0	3	2	1	14	13	12	15	8	11	10	9	22	21	20	23	16	19	18	17
7	7	6	5	4	1	0	3	2	15	14	13	12	9	8	11	10	23	22	21	20	17	16	19	18
8	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23	0	1	2	3	4	5	6	7
9	9	10	11	8	13	14	15	12	17	18	19	16	21	22	23	20	1	2	3	0	5	6	7	4
10	10	11	8	9	14	15	12	13	18	19	16	17	22	23	20	21	2	3	0	1	6	7	4	5
11	11	8	9	10	15	12	13	14	19	16	17	18	23	20	21	22	3	0	1	2	7	4	5	6
12	12	15	14	13	10	9	8	11	20	23	22	21	18	17	16	19	4	7	6	5	2	1	0	3
13	13	12	15	14	11	10	9	8	21	20	23	22	19	18	17	16	5	4	7	6	3	2	1	0
14	14	13	12	15	8	11	10	9	22	21	20	23	16	19	18	17	6	5	4	7	0	3	2	1
15	15	14	13	12	9	8	11	10	23	22	21	20	17	16	19	18	7	6	5	4	1	0	3	2
16	16	17	18	19	20	21	22	23	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15
17	17	18	19	16	21	22	23	20	1	2	3	0	5	6	7	4	9	10	11	8	13	14	15	12
18	18	19	16	17	22	23	20	21	2	3	0	1	6	7	4	5	10	11	8	9	14	15	12	13
19	19	16	17	18	23	20	21	22	3	0	1	2	7	4	5	6	11	8	9	10	15	12	13	14
20	20	23	22	21	18	17	16	19	4	7	6	5	2	1	0	3	12	15	14	13	10	9	8	11
21	21	20	23	22	19	18	17	16	5	4	7	6	3	2	1	0	13	12	15	14	11	10	9	8
22	22	21	20	23	16	19	18	17	6	5	4	7	0	3	2	1	14	13	12	15	8	11	10	9
23	23	22	21	20	17	16	19	18	7	6	5	4	1	0	3	2	15	14	13	12	9	8	11	10

Cycle graph

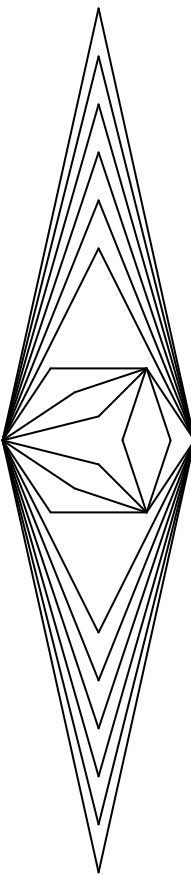


$Q_8 \times C_3$, nilpotent, identity element $e = 0$, $a^4 = e$, $b^2 = a^2$, $c^3 = e$, $ba = a^{-1}b$, $ca = ac$, $cb = bc$

	e	a	a ²	a ³	b	ab	a ² b	a ³ b	c	ac	a ² c	a ³ c	bc	abc	a ² bc	a ³ bc	c ²	ac ²	a ² c ²	a ³ c ²	bc ²	abc ²	a ² bc ²	a ³ bc ²
Element	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23
Order	1	4	2	4	4	4	4	4	3	12	6	12	12	12	12	12	3	12	6	12	12	12	12	12

	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23
0	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23
1	1	2	3	0	5	6	7	4	9	10	11	8	13	14	15	12	17	18	19	16	21	22	23	20
2	2	3	0	1	6	7	4	5	10	11	8	9	14	15	12	13	18	19	16	17	22	23	20	21
3	3	0	1	2	7	4	5	6	11	8	9	10	15	12	13	14	19	16	17	18	23	20	21	22
4	4	9	6	11	8	1	10	3	0	5	2	7	16	21	18	23	20	13	22	15	12	17	14	19
5	5	10	7	8	9	2	11	0	1	6	3	4	17	22	19	20	21	14	23	12	13	18	15	16
6	6	11	4	9	10	3	8	1	2	7	0	5	18	23	16	21	22	15	20	13	14	19	12	17
7	7	8	5	10	11	0	9	2	3	4	1	6	19	20	17	22	23	12	21	14	15	16	13	18
8	8	5	10	7	0	9	2	11	4	1	6	3	20	17	22	19	12	21	14	23	16	13	18	15
9	9	6	11	4	1	10	3	8	5	2	7	0	21	18	23	16	13	22	15	20	17	14	19	12
10	10	7	8	5	2	11	0	9	6	3	4	1	22	19	20	17	14	23	12	21	18	15	16	13
11	11	4	9	6	3	8	1	10	7	0	5	2	23	16	21	18	15	20	13	22	19	12	17	14
12	12	13	14	15	16	17	18	19	20	21	22	23	0	1	2	3	4	5	6	7	8	9	10	11
13	13	14	15	12	17	18	19	16	21	22	23	20	1	2	3	0	5	6	7	4	9	10	11	8
14	14	15	12	13	18	19	16	17	22	23	20	21	2	3	0	1	6	7	4	5	10	11	8	9
15	15	12	13	14	19	16	17	18	23	20	21	22	3	0	1	2	7	4	5	6	11	8	9	10
16	16	21	18	23	20	13	22	15	12	17	14	19	4	9	6	11	8	1	10	3	0	5	2	7
17	17	22	19	20	21	14	23	12	13	18	15	16	5	10	7	8	9	2	11	0	1	6	3	4
18	18	23	16	21	22	15	20	13	14	19	12	17	6	11	4	9	10	3	8	1	2	7	0	5
19	19	20	17	22	23	12	21	14	15	16	13	18	7	8	5	10	11	0	9	2	3	4	1	6
20	20	17	22	19	12	21	14	23	16	13	18	15	8	5	10	7	0	9	2	11	4	1	6	3
21	21	18	23	16	13	22	15	20	17	14	19	12	9	6	11	4	1	10	3	8	5	2	7	0
22	22	19	20	17	14	23	12	21	18	15	16	13	10	7	8	5	2	11	0	9	6	3	4	1
23	23	16	21	18	15	20	13	22	19	12	17	14	11	4	9	6	3	8	1	10	7	0	5	2

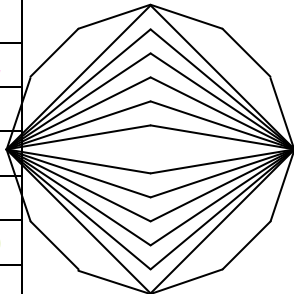
Cycle graph



$T_{12} \times C_2$ = dicyclic group of order $12 \times C_2$ = semi-direct product of C_6 and C_4 , solvable,
identity element $e = 0$, $a^4 = e$, $b^6 = e$, $bab = a$

	e	a	a ²	a ³	b ²	ab ²	a ² b ²	a ³ b ²	b ⁴	ab ⁴	a ² b ⁴	a ³ b ⁴	b ³	ab ³	a ² b ³	a ³ b ³	b ⁵	ab ⁵	a ² b ⁵	a ³ b ⁵	b	ab	a ² b	a ³ b
Element	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23
Order	1	4	2	4	3	4	6	4	3	4	6	4	2	4	2	4	6	4	6	4	6	4	6	4

Cycle graph

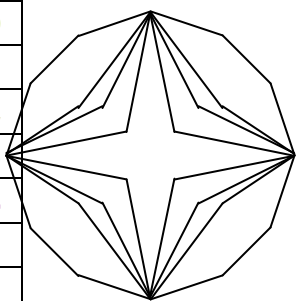


Q_{12} = dicyclic group of order 24, solvable, identity element $e = 0$, $a^{12} = e$, $b^2 = a^6$, $ba = a^{-1}b$

[illegible]

	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23
0	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23
1	1	2	3	4	5	6	7	0	9	10	11	12	13	14	15	8	17	18	19	20	21	22	23	16
2	2	3	4	5	6	7	0	1	10	11	12	13	14	15	8	9	18	19	20	21	22	23	16	17
3	3	4	5	6	7	0	1	2	11	12	13	14	15	8	9	10	19	20	21	22	23	16	17	18
4	4	5	6	7	0	1	2	3	12	13	14	15	8	9	10	11	20	21	22	23	16	17	18	19
5	5	6	7	0	1	2	3	4	13	14	15	8	9	10	11	12	21	22	23	16	17	18	19	20
6	6	7	0	1	2	3	4	5	14	15	8	9	10	11	12	13	22	23	16	17	18	19	20	21
7	7	0	1	2	3	4	5	6	15	8	9	10	11	12	13	14	23	16	17	18	19	20	21	22
8	8	17	10	19	12	21	14	23	16	1	18	3	20	5	22	7	0	9	2	11	4	13	6	15
9	9	18	11	20	13	22	15	16	17	2	19	4	21	6	23	0	1	10	3	12	5	14	7	8
10	10	19	12	21	14	23	8	17	18	3	20	5	22	7	16	1	2	11	4	13	6	15	0	9
11	11	20	13	22	15	16	9	18	19	4	21	6	23	0	17	2	3	12	5	14	7	8	1	10
12	12	21	14	23	8	17	10	19	20	5	22	7	16	1	18	3	4	13	6	15	0	9	2	11
13	13	22	15	16	9	18	11	20	21	6	23	0	17	2	19	4	5	14	7	8	1	10	3	12
14	14	23	8	17	10	19	12	21	22	7	16	1	18	3	20	5	6	15	0	9	2	11	4	13
15	15	16	9	18	11	20	13	22	23	0	17	2	19	4	21	6	7	8	1	10	3	12	5	14
16	16	9	18	11	20	13	22	15	0	17	2	19	4	21	6	23	8	1	10	3	12	5	14	7
17	17	10	19	12	21	14	23	8	1	18	3	20	5	22	7	16	9	2	11	4	13	6	15	0
18	18	11	20	13	22	15	16	9	2	19	4	21	6	23	0	17	10	3	12	5	14	7	8	1
19	19	12	21	14	23	8	17	10	3	20	5	22	7	16	1	18	11	4	13	6	15	0	9	2
20	20	13	22	15	16	9	18	11	4	21	6	23	0	17	2	19	12	5	14	7	8	1	10	3
21	21	14	23	8	17	10	19	12	5	22	7	16	1	18	3	20	13	6	15	0	9	2	11	4
22	22	15	16	9	18	11	20	13	6	23	0	17	2	19	4	21	14	7	8	1	10	3	12	5
23	23	8	17	10	19	12	21	14	7	16	1	18	3	20	5	22	15	0	9	2	11	4	13	6

Cycle graph

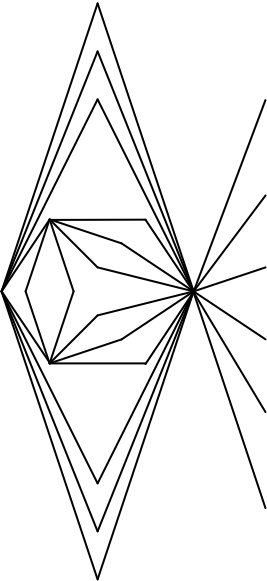


Semi-direct product of C_8 and C_3 , solvable, identity element $e = 0$, $a^8 = e$, $b^3 = e$, $bab = a$

	e	a	a ²	a ³	a ⁴	a ⁵	a ⁶	a ⁷	b	ab	a ² b	a ³ b	a ⁴ b	a ⁵ b	a ⁶ b	a ⁷ b	b ²	ab ²	a ² b ²	a ³ b ²	a ⁴ b ²	a ⁵ b ²	a ⁶ b ²	a ⁷ b ²
Element	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23
Order	1	8	4	8	2	8	4	8	3	8	12	8	6	8	12	8	3	8	12	8	6	8	12	8

	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23
0	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23
1	1	2	0	4	5	3	7	8	6	10	11	9	13	14	12	16	17	15	19	20	18	22	23	21
2	2	0	1	5	3	4	8	6	7	11	9	10	14	12	13	17	15	16	20	18	19	23	21	22
3	3	5	4	6	8	7	9	11	10	0	2	1	15	17	16	18	20	19	21	23	22	12	14	13
4	4	3	5	7	6	8	10	9	11	1	0	2	16	15	17	19	18	20	22	21	23	13	12	14
5	5	4	3	8	7	6	11	10	9	2	1	0	17	16	15	20	19	18	23	22	21	14	13	12
6	6	7	8	9	10	11	0	1	2	3	4	5	18	19	20	21	22	23	12	13	14	15	16	17
7	7	8	6	10	11	9	1	2	0	4	5	3	19	20	18	22	23	21	13	14	12	16	17	15
8	8	6	7	11	9	10	2	0	1	5	3	4	20	18	19	23	21	22	14	12	13	17	15	16
9	9	11	10	0	2	1	3	5	4	6	8	7	21	23	22	12	14	13	15	17	16	18	20	19
10	10	9	11	1	0	2	4	3	5	7	6	8	22	21	23	13	12	14	16	15	17	19	18	20
11	11	10	9	2	1	0	5	4	3	8	7	6	23	22	21	14	13	12	17	16	15	20	19	18
12	12	13	14	21	22	23	18	19	20	15	16	17	0	1	2	9	10	11	6	7	8	3	4	5
13	13	14	12	22	23	21	19	20	18	16	17	15	1	2	0	10	11	9	7	8	6	4	5	3
14	14	12	13	23	21	22	20	18	19	17	15	16	2	0	1	11	9	10	8	6	7	5	3	4
15	15	17	16	12	14	13	21	23	22	18	20	19	3	5	4	0	2	1	9	11	10	6	8	7
16	16	15	17	13	12	14	22	21	23	19	18	20	4	3	5	1	0	2	10	9	11	7	6	8
17	17	16	15	14	13	12	23	22	21	20	19	18	5	4	3	2	1	0	11	10	9	8	7	6
18	18	19	20	15	16	17	12	13	14	21	22	23	6	7	8	3	4	5	0	1	2	9	10	11
19	19	20	18	16	17	15	13	14	12	22	23	21	7	8	6	4	5	3	1	2	0	10	11	9
20	20	18	19	17	15	16	14	12	13	23	21	22	8	6	7	5	3	4	2	0	1	11	9	10
21	21	23	22	18	20	19	15	17	16	12	14	13	9	11	10	6	8	7	3	5	4	0	2	1
22	22	21	23	19	18	20	16	15	17	13	12	14	10	9	11	7	6	8	4	3	5	1	0	2
23	23	22	21	20	19	18	17	16	15	14	13	12	11	10	9	8	7	6	5	4	3	2	1	0

Cycle graph

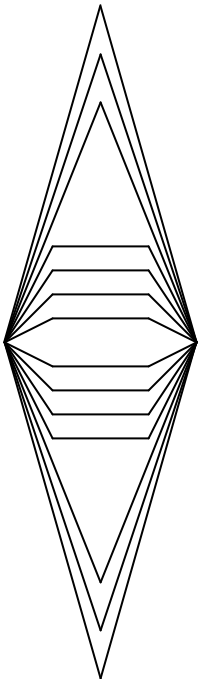


Semi-direct product of C_3 and D_8 , solvable, identity element $e = 0$, $a^3 = e$, $b^4 = e$, $c^2 = e$, $bc b = c$, $aba = b$, $ca = ac$

	e	a	a ²	b	ab	a ² b	b ²	ab ²	a ² b ²	b ³	ab ³	a ² b ³	c	ac	a ² c	bc	abc	a ² bc	b ² c	ab ² c	a ² b ² c	b ³ c	ab ³ c	a ² b ³ c
Element	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23
Order	1	3	3	4	4	4	2	6	6	4	4	4	2	6	6	2	2	2	2	6	6	2	2	2

	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23
0	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23
1	1	2	3	0	5	6	7	4	9	10	11	8	13	14	15	12	17	18	19	16	21	22	23	20
2	2	3	0	1	6	7	4	5	10	11	8	9	14	15	12	13	18	19	16	17	22	23	20	21
3	3	0	1	2	7	4	5	6	11	8	9	10	15	12	13	14	19	16	17	18	23	20	21	22
4	4	7	6	5	2	1	0	3	12	15	14	13	10	9	8	11	20	23	22	21	18	17	16	19
5	5	4	7	6	3	2	1	0	13	12	15	14	11	10	9	8	21	20	23	22	19	18	17	16
6	6	5	4	7	0	3	2	1	14	13	12	15	8	11	10	9	22	21	20	23	16	19	18	17
7	7	6	5	4	1	0	3	2	15	14	13	12	9	8	11	10	23	22	21	20	17	16	19	18
8	8	13	10	15	9	12	11	14	16	21	18	23	17	20	19	22	0	5	2	7	1	4	3	6
9	9	14	11	12	10	13	8	15	17	22	19	20	18	21	16	23	1	6	3	4	2	5	0	7
10	10	15	8	13	11	14	9	12	18	23	16	21	19	22	17	20	2	7	0	5	3	6	1	4
11	11	12	9	14	8	15	10	13	19	20	17	22	16	23	18	21	3	4	1	6	0	7	2	5
12	12	9	14	11	15	10	13	8	20	17	22	19	23	18	21	16	4	1	6	3	7	2	5	0
13	13	10	15	8	12	11	14	9	21	18	23	16	20	19	22	17	5	2	7	0	4	3	6	1
14	14	11	12	9	13	8	15	10	22	19	20	17	21	16	23	18	6	3	4	1	5	0	7	2
15	15	8	13	10	14	9	12	11	23	16	21	18	22	17	20	19	7	0	5	2	6	1	4	3
16	16	20	18	22	21	17	23	19	0	4	2	6	5	1	7	3	8	12	10	14	13	9	15	11
17	17	21	19	23	22	18	20	16	1	5	3	7	6	2	4	0	9	13	11	15	14	10	12	8
18	18	22	16	20	23	19	21	17	2	6	0	4	7	3	5	1	10	14	8	12	15	11	13	9
19	19	23	17	21	20	16	22	18	3	7	1	5	4	0	6	2	11	15	9	13	12	8	14	10
20	20	18	22	16	17	23	19	21	4	2	6	0	1	7	3	5	12	10	14	8	9	15	11	13
21	21	19	23	17	18	20	16	22	5	3	7	1	2	4	0	6	13	11	15	9	10	12	8	14
22	22	16	20	18	19	21	17	23	6	0	4	2	3	5	1	7	14	8	12	10	11	13	9	15
23	23	17	21	19	16	22	18	20	7	1	5	3	0	6	2	4	15	9	13	11	8	14	10	12

Cycle graph

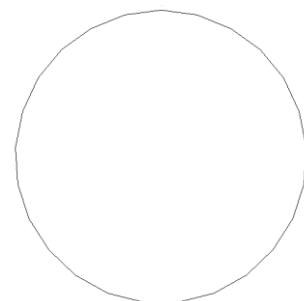


$SL_2(3)$ is that Special Linear Group over $GF(3)$, solvable, identity element $e = 0$,
 $a^4 = e, b^2 = a^2, c^3 = e, aba = b, cb = ac, cab = bc$

	e	a	a ²	a ³	b	ab	a ² b	a ³ b	c	ac	a ² c	a ³ c	bc	abc	a ² bc	a ³ bc	c ²	ac ²	a ² c ²	a ³ c ²	bc ²	abc ²	a ² bc ²	a ³ bc ²
Element	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23
Order	1	4	2	4	4	4	4	4	3	3	6	6	3	3	6	6	3	6	6	3	6	6	3	3

Order 25 (2 groups)

Cycle graph



	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24
0	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24
1	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24	0
2	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24	0	1
3	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24	0	1	2
4	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24	0	1	2	3
5	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24	0	1	2	3	4
6	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24	0	1	2	3	4	5
7	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24	0	1	2	3	4	5	6
8	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24	0	1	2	3	4	5	6	7
9	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24	0	1	2	3	4	5	6	7	8
10	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24	0	1	2	3	4	5	6	7	8	9
11	11	12	13	14	15	16	17	18	19	20	21	22	23	24	0	1	2	3	4	5	6	7	8	9	10
12	12	13	14	15	16	17	18	19	20	21	22	23	24	0	1	2	3	4	5	6	7	8	9	10	11
13	13	14	15	16	17	18	19	20	21	22	23	24	0	1	2	3	4	5	6	7	8	9	10	11	12
14	14	15	16	17	18	19	20	21	22	23	24	0	1	2	3	4	5	6	7	8	9	10	11	12	13
15	15	16	17	18	19	20	21	22	23	24	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14
16	16	17	18	19	20	21	22	23	24	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15
17	17	18	19	20	21	22	23	24	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16
18	18	19	20	21	22	23	24	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17
19	19	20	21	22	23	24	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18
20	20	21	22	23	24	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19
21	21	22	23	24	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20
22	22	23	24	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21
23	23	24	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22
24	24	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23

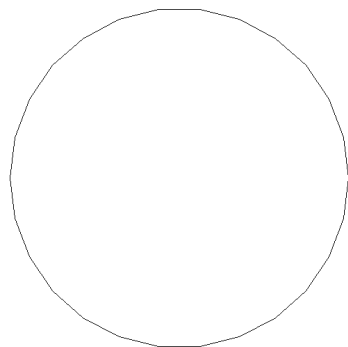
 C_{25} , cyclic, identity element $e = 0$, $a^{25} = e$

	e	a	a ²	a ³	a ⁴	a ⁵	a ⁶	a ⁷	a ⁸	a ⁹	a ¹⁰	a ¹¹	a ¹²	a ¹³	a ¹⁴	a ¹⁵	a ¹⁶	a ¹⁷	a ¹⁸	a ¹⁹	a ²⁰	a ²¹	a ²²	a ²³	a ²⁴
Element	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24
Order	1	25	25	25	25	5	25	25	25	25	5	25	25	25	25	5	25	25	25	25	5	25	25	25	25

Order 26 (2 groups)

	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24	25
0	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24	25
1	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24	25	0
2	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24	25	0	1
3	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24	25	0	1	2
4	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24	25	0	1	2	3
5	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24	25	0	1	2	3	4
6	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24	25	0	1	2	3	4	5
7	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24	25	0	1	2	3	4	5	6
8	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24	25	0	1	2	3	4	5	6	7
9	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24	25	0	1	2	3	4	5	6	7	8
10	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24	25	0	1	2	3	4	5	6	7	8	9
11	11	12	13	14	15	16	17	18	19	20	21	22	23	24	25	0	1	2	3	4	5	6	7	8	9	10
12	12	13	14	15	16	17	18	19	20	21	22	23	24	25	0	1	2	3	4	5	6	7	8	9	10	11
13	13	14	15	16	17	18	19	20	21	22	23	24	25	0	1	2	3	4	5	6	7	8	9	10	11	12
14	14	15	16	17	18	19	20	21	22	23	24	25	0	1	2	3	4	5	6	7	8	9	10	11	12	13
15	15	16	17	18	19	20	21	22	23	24	25	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14
16	16	17	18	19	20	21	22	23	24	25	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15
17	17	18	19	20	21	22	23	24	25	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16
18	18	19	20	21	22	23	24	25	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17
19	19	20	21	22	23	24	25	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18
20	20	21	22	23	24	25	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19
21	21	22	23	24	25	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20
22	22	23	24	25	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21
23	23	24	25	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22
24	24	25	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23
25	25	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24

Cycle graph



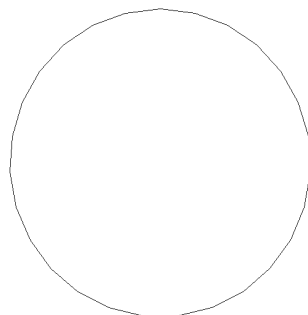
C_{26} , cyclic, identity element $e = 0$, $a^{26} = e$

	e	a	a ²	a ³	a ⁴	a ⁵	a ⁶	a ⁷	a ⁸	a ⁹	a ¹⁰	a ¹¹	a ¹²	a ¹³	a ¹⁴	a ¹⁵	a ¹⁶	a ¹⁷	a ¹⁸	a ¹⁹	a ²⁰	a ²¹	a ²²	a ²³	a ²⁴	a ²⁵
Element	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24	25
Order	1	26	13	26	13	26	13	26	13	26	13	26	13	2	13	26	13	26	13	26	13	26	13	26	13	26

Order 27 (5 groups)

	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24	25	26
0	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24	25	26
1	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24	25	26	0
2	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24	25	26	0	1
3	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24	25	26	0	1	2
4	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24	25	26	0	1	2	3
5	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24	25	26	0	1	2	3	4
6	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24	25	26	0	1	2	3	4	5
7	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24	25	26	0	1	2	3	4	5	6
8	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24	25	26	0	1	2	3	4	5	6	7
9	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24	25	26	0	1	2	3	4	5	6	7	8
10	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24	25	26	0	1	2	3	4	5	6	7	8	9
11	11	12	13	14	15	16	17	18	19	20	21	22	23	24	25	26	0	1	2	3	4	5	6	7	8	9	10
12	12	13	14	15	16	17	18	19	20	21	22	23	24	25	26	0	1	2	3	4	5	6	7	8	9	10	11
13	13	14	15	16	17	18	19	20	21	22	23	24	25	26	0	1	2	3	4	5	6	7	8	9	10	11	12
14	14	15	16	17	18	19	20	21	22	23	24	25	26	0	1	2	3	4	5	6	7	8	9	10	11	12	13
15	15	16	17	18	19	20	21	22	23	24	25	26	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14
16	16	17	18	19	20	21	22	23	24	25	26	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15
17	17	18	19	20	21	22	23	24	25	26	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16
18	18	19	20	21	22	23	24	25	26	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17
19	19	20	21	22	23	24	25	26	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18
20	20	21	22	23	24	25	26	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19
21	21	22	23	24	25	26	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20
22	22	23	24	25	26	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21
23	23	24	25	26	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22
24	24	25	26	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23
25	25	26	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24
26	26	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24	25

Cycle graph



C_{27} , cyclic, identity element $e = 0$, $a^{27} = e$

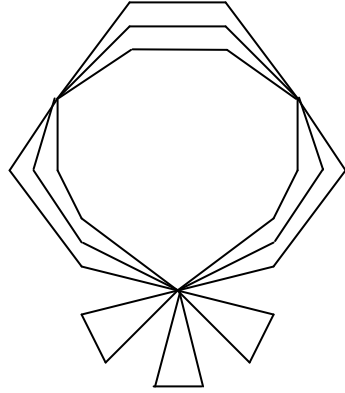
	e	a	a ²	a ³	a ⁴	a ⁵	a ⁶	a ⁷	a ⁸	a ⁹	a ¹⁰	a ¹¹	a ¹²	a ¹³	a ¹⁴	a ¹⁵	a ¹⁶	a ¹⁷	a ¹⁸	a ¹⁹	a ²⁰	a ²¹	a ²²	a ²³	a ²⁴	a ²⁵	a ²⁶
Element	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24	25	26
Order	1	27	27	9	27	27	9	27	27	3	27	27	9	27	27	9	27	27	3	27	27	9	27	27	9	27	27

	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24	25	26
0	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24	25	26
1	1	2	3	4	5	6	7	8	0	10	11	12	13	14	15	16	17	9	19	20	21	22	23	24	25	26	18
2	2	3	4	5	6	7	8	0	1	11	12	13	14	15	16	17	9	10	20	21	22	23	24	25	26	18	19
3	3	4	5	6	7	8	0	1	2	12	13	14	15	16	17	9	10	11	21	22	23	24	25	26	18	19	20
4	4	5	6	7	8	0	1	2	3	13	14	15	16	17	9	10	11	12	22	23	24	25	26	18	19	20	21
5	5	6	7	8	0	1	2	3	4	14	15	16	17	9	10	11	12	13	23	24	25	26	18	19	20	21	22
6	6	7	8	0	1	2	3	4	5	15	16	17	9	10	11	12	13	14	24	25	26	18	19	20	21	22	23
7	7	8	0	1	2	3	4	5	6	16	17	9	10	11	12	13	14	15	25	26	18	19	20	21	22	23	24
8	8	0	1	2	3	4	5	6	7	17	9	10	11	12	13	14	15	16	26	18	19	20	21	22	23	24	25
9	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24	25	26	0	1	2	3	4	5	6	7	8
10	10	11	12	13	14	15	16	17	9	19	20	21	22	23	24	25	26	18	1	2	3	4	5	6	7	8	0
11	11	12	13	14	15	16	17	9	10	20	21	22	23	24	25	26	18	19	2	3	4	5	6	7	8	0	1
12	12	13	14	15	16	17	9	10	11	21	22	23	24	25	26	18	19	20	3	4	5	6	7	8	0	1	2
13	13	14	15	16	17	9	10	11	12	22	23	24	25	26	18	19	20	21	4	5	6	7	8	0	1	2	3
14	14	15	16	17	9	10	11	12	13	23	24	25	26	18	19	20	21	22	5	6	7	8	0	1	2	3	4
15	15	16	17	9	10	11	12	13	14	24	25	26	18	19	20	21	22	23	6	7	8	0	1	2	3	4	5
16	16	17	9	10	11	12	13	14	15	25	26	18	19	20	21	22	23	24	7	8	0	1	2	3	4	5	6
17	17	9	10	11	12	13	14	15	16	26	18	19	20	21	22	23	24	25	8	0	1	2	3	4	5	6	7
18	18	19	20	21	22	23	24	25	26	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17
19	19	20	21	22	23	24	25	26	18	1	2	3	4	5	6	7	8	0	10	11	12	13	14	15	16	17	9
20	20	21	22	23	24	25	26	18	19	2	3	4	5	6	7	8	0	1	11	12	13	14	15	16	17	9	10
21	21	22	23	24	25	26	18	19	20	3	4	5	6	7	8	0	1	2	12	13	14	15	16	17	9	10	11
22	22	23	24	25	26	18	19	20	21	4	5	6	7	8	0	1	2	3	13	14	15	16	17	9	10	11	12
23	23	24	25	26	18	19	20	21	22	5	6	7	8	0	1	2	3	4	14	15	16	17	9	10	11	12	13
24	24	25	26	18	19	20	21	22	23	6	7	8	0	1	2	3	4	5	15	16	17	9	10	11	12	13	14
25	25	26	18	19	20	21	22	23	24	7	8	0	1	2	3	4	5	6	16	17	9	10	11	12	13	14	15
26	26	18	19	20	21	22	23	24	25	8	0	1	2	3	4	5	6	7	17	9	10	11	12	13	14	15	16

$C_9 \times C_3$, abelian, identity element $e = 0$, $a^9 = e$, $b^3 = e$, $ba = ab$

	e	a	a ²	a ³	a ⁴	a ⁵	a ⁶	a ⁷	a ⁸	b	ab	a ² b	a ³ b	a ⁴ b	a ⁵ b	a ⁶ b	a ⁷ b	a ⁸ b	b ²	ab ²	a ² b ²	a ³ b ²	a ⁴ b ²	a ⁵ b ²	a ⁶ b ²	a ⁷ b ²	a ⁸ b ²
Element	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24	25	26
Order	1	9	9	3	9	9	3	9	9	3	9	9	3	9	9	3	9	9	3	9	9	3	9	9	3	9	9

Cycle graph

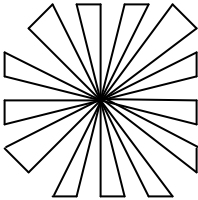


	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24	25	26
0	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24	25	26
1	1	2	0	4	5	3	7	8	6	10	11	9	13	14	12	16	17	15	19	20	18	22	23	21	25	26	24
2	2	0	1	5	3	4	8	6	7	11	9	10	14	12	13	17	15	16	20	18	19	23	21	22	26	24	25
3	3	4	5	6	7	8	0	1	2	12	13	14	15	16	17	9	10	11	21	22	23	24	25	26	18	19	20
4	4	5	3	7	8	6	1	2	0	13	14	12	16	17	15	10	11	9	22	23	21	25	26	24	19	20	18
5	5	3	4	8	6	7	2	0	1	14	12	13	17	15	16	11	9	10	23	21	22	26	24	25	20	18	19
6	6	7	8	0	1	2	3	4	5	15	16	17	9	10	11	12	13	14	24	25	26	18	19	20	21	22	23
7	7	8	6	1	2	0	4	5	3	16	17	15	10	11	9	13	14	12	25	26	24	19	20	18	22	23	21
8	8	6	7	2	0	1	5	3	4	17	15	16	11	9	10	14	12	13	26	24	25	20	18	19	23	21	22
9	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24	25	26	0	1	2	3	4	5	6	7	8
10	10	11	9	13	14	12	16	17	15	19	20	18	22	23	21	25	26	24	1	2	0	4	5	3	7	8	6
11	11	9	10	14	12	13	17	15	16	20	18	19	23	21	22	26	24	25	2	0	1	5	3	4	8	6	7
12	12	13	14	15	16	17	9	10	11	21	22	23	24	25	26	18	19	20	3	4	5	6	7	8	0	1	2
13	13	14	12	16	17	15	10	11	9	22	23	21	25	26	24	19	20	18	4	5	3	7	8	6	1	2	0
14	14	12	13	17	15	16	11	9	10	23	21	22	26	24	25	20	18	19	5	3	4	8	6	7	2	0	1
15	15	16	17	9	10	11	12	13	14	24	25	26	18	19	20	21	22	23	6	7	8	0	1	2	3	4	5
16	16	17	15	10	11	9	13	14	12	25	26	24	19	20	18	22	23	21	7	8	6	1	2	0	4	5	3
17	17	15	16	11	9	10	14	12	13	26	24	25	20	18	19	23	21	22	8	6	7	2	0	1	5	3	4
18	18	19	20	21	22	23	24	25	26	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17
19	19	20	18	22	23	21	25	26	24	1	2	0	4	5	3	7	8	6	10	11	9	13	14	12	16	17	15
20	20	18	19	23	21	22	26	24	25	2	0	1	5	3	4	8	6	7	11	9	10	14	12	13	17	15	16
21	21	22	23	24	25	26	18	19	20	3	4	5	6	7	8	0	1	2	12	13	14	15	16	17	9	10	11
22	22	23	21	25	26	24	19	20	18	4	5	3	7	8	6	1	2	0	13	14	12	16	17	15	10	11	9
23	23	21	22	26	24	25	20	18	19	5	3	4	8	6	7	2	0	1	14	12	13	17	15	16	11	9	10
24	24	25	26	18	19	20	21	22	23	6	7	8	0	1	2	3	4	5	15	16	17	9	10	11	12	13	14
25	25	26	24	19	20	18	22	23	21	7	8	6	1	2	0	4	5	3	16	17	15	10	11	9	13	14	12
26	26	24	25	20	18	19	23	21	22	8	6	7	2	0	1	5	3	4	17	15	16	11	9	10	14	12	13

C_3^3 , abelian, identity element $e = 0$, $a^3 = e$, $b^3 = e$, $c^3 = e$, $ba = ab$, $ca = ac$, $cb = bc$

	e	a	a ²	b	ab	a ² b	b ²	ab ²	a ² b ²	c	ac	a ² c	bc	abc	a ² bc	b ² c	ab ² c	a ² b ² c	c ²	ac ²	a ² c ²	bc ²	abc ²	a ² bc ²	b ² c ²	ab ² c ²	a ² b ² c ²
Element	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24	25	26
Order	1	3	3	3	3	3	3	3	3	3	3	3	3	3	3	3	3	3	3	3	3	3	3	3	3	3	3

Cycle graph

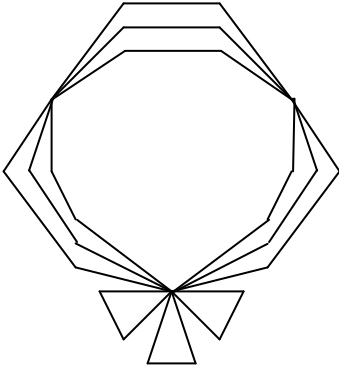


	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24	25	26
0	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24	25	26
1	1	2	3	4	5	6	7	8	0	10	11	12	13	14	15	16	17	9	19	20	21	22	23	24	25	26	18
2	2	3	4	5	6	7	8	0	1	11	12	13	14	15	16	17	9	10	20	21	22	23	24	25	26	18	19
3	3	4	5	6	7	8	0	1	2	12	13	14	15	16	17	9	10	11	21	22	23	24	25	26	18	19	20
4	4	5	6	7	8	0	1	2	3	13	14	15	16	17	9	10	11	12	22	23	24	25	26	18	19	20	21
5	5	6	7	8	0	1	2	3	4	14	15	16	17	9	10	11	12	13	23	24	25	26	18	19	20	21	22
6	6	7	8	0	1	2	3	4	5	15	16	17	9	10	11	12	13	14	24	25	26	18	19	20	21	22	23
7	7	8	0	1	2	3	4	5	6	16	17	9	10	11	12	13	14	15	25	26	18	19	20	21	22	23	24
8	8	0	1	2	3	4	5	6	7	17	9	10	11	12	13	14	15	16	26	18	19	20	21	22	23	24	25
9	9	16	14	12	10	17	15	13	11	18	25	23	21	19	26	24	22	20	0	7	5	3	1	8	6	4	2
10	10	17	15	13	11	9	16	14	12	19	26	24	22	20	18	25	23	21	1	8	6	4	2	0	7	5	3
11	11	9	16	14	12	10	17	15	13	20	18	25	23	21	19	26	24	22	2	0	7	5	3	1	8	6	4
12	12	10	17	15	13	11	9	16	14	21	19	26	24	22	20	18	25	23	3	1	8	6	4	2	0	7	5
13	13	11	9	16	14	12	10	17	15	22	20	18	25	23	21	19	26	24	4	2	0	7	5	3	1	8	6
14	14	12	10	17	15	13	11	9	16	23	21	19	26	24	22	20	18	25	5	3	1	8	6	4	2	0	7
15	15	13	11	9	16	14	12	10	17	24	22	20	18	25	23	21	19	26	6	4	2	0	7	5	3	1	8
16	16	14	12	10	17	15	13	11	9	25	23	21	19	26	24	22	20	18	7	5	3	1	8	6	4	2	0
17	17	15	13	11	9	16	14	12	10	26	24	22	20	18	25	23	21	19	8	6	4	2	0	7	5	3	1
18	18	22	26	21	25	20	24	19	23	0	4	8	3	7	2	6	1	5	9	13	17	12	16	11	15	10	14
19	19	23	18	22	26	21	25	20	24	1	5	0	4	8	3	7	2	6	10	14	9	13	17	12	16	11	15
20	20	24	19	23	18	22	26	21	25	2	6	1	5	0	4	8	3	7	11	15	10	14	9	13	17	12	16
21	21	25	20	24	19	23	18	22	26	3	7	2	6	1	5	0	4	8	12	16	11	15	10	14	9	13	17
22	22	26	21	25	20	24	19	23	18	4	8	3	7	2	6	1	5	0	13	17	12	16	11	15	10	14	9
23	23	18	22	26	21	25	20	24	19	5	0	4	8	3	7	2	6	1	14	9	13	17	12	16	11	15	10
24	24	19	23	18	22	26	21	25	20	6	1	5	0	4	8	3	7	2	15	10	14	9	13	17	12	16	11
25	25	20	24	19	23	18	22	26	21	7	2	6	1	5	0	4	8	3	16	11	15	10	14	9	13	17	12
26	26	21	25	20	24	19	23	18	22	8	3	7	2	6	1	5	0	4	17	12	16	11	15	10	14	9	13

nilpotent, identity element $e = 0$, $s^9 = e$, $t^3 = e$, $st = ts^4$

	e	s	s ²	s ³	s ⁴	s ⁵	s ⁶	s ⁷	s ⁸	t	st	s ² t	s ³ t	s ⁴ t	s ⁵ t	s ⁶ t	s ⁷ t	s ⁸ t	t ²	st ²	s ² t ²	s ³ t ²	s ⁴ t ²	s ⁵ t ²	s ⁶ t ²	s ⁷ t ²	s ⁸ t ²
Element	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24	25	26
Order	1	9	9	3	9	9	3	9	9	3	9	9	3	9	9	3	9	9	3	9	9	3	9	9	3	9	9

Cycle graph

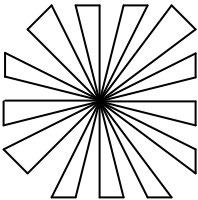


	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24	25	26
0	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24	25	26
1	1	2	0	4	5	3	7	8	6	10	11	9	13	14	12	16	17	15	19	20	18	22	23	21	25	26	24
2	2	0	1	5	3	4	8	6	7	11	9	10	14	12	13	17	15	16	20	18	19	23	21	22	26	24	25
3	3	4	5	6	7	8	0	1	2	12	13	14	15	16	17	9	10	11	21	22	23	24	25	26	18	19	20
4	4	5	3	7	8	6	1	2	0	13	14	12	16	17	15	10	11	9	22	23	21	25	26	24	19	20	18
5	5	3	4	8	6	7	2	0	1	14	12	13	17	15	16	11	9	10	23	21	22	26	24	25	20	18	19
6	6	7	8	0	1	2	3	4	5	15	16	17	9	10	11	12	13	14	24	25	26	18	19	20	21	22	23
7	7	8	6	1	2	0	4	5	3	16	17	15	10	11	9	13	14	12	25	26	24	19	20	18	22	23	21
8	8	6	7	2	0	1	5	3	4	17	15	16	11	9	10	14	12	13	26	24	25	20	18	19	23	21	22
9	9	10	11	14	12	13	16	17	15	18	19	20	23	21	22	25	26	24	0	1	2	5	3	4	7	8	6
10	10	11	9	12	13	14	17	15	16	19	20	18	21	22	23	26	24	25	1	2	0	3	4	5	8	6	7
11	11	9	10	13	14	12	15	16	17	20	18	19	22	23	21	24	25	26	2	0	1	4	5	3	6	7	8
12	12	13	14	17	15	16	10	11	9	21	22	23	26	24	25	19	20	18	3	4	5	8	6	7	1	2	0
13	13	14	12	15	16	17	11	9	10	22	23	21	24	25	26	20	18	19	4	5	3	6	7	8	2	0	1
14	14	12	13	16	17	15	9	10	11	23	21	22	25	26	24	18	19	20	5	3	4	7	8	6	0	1	2
15	15	16	17	11	9	10	13	14	12	24	25	26	20	18	19	22	23	21	6	7	8	2	0	1	4	5	3
16	16	17	15	9	10	11	14	12	13	25	26	24	18	19	20	23	21	22	7	8	6	0	1	2	5	3	4
17	17	15	16	10	11	9	12	13	14	26	24	25	19	20	18	21	22	23	8	6	7	1	2	0	3	4	5
18	18	19	20	22	23	21	26	24	25	0	1	2	4	5	3	8	6	7	9	10	11	13	14	12	17	15	16
19	19	20	18	23	21	22	24	25	26	1	2	0	5	3	4	6	7	8	10	11	9	14	12	13	15	16	17
20	20	18	19	21	22	23	25	26	24	2	0	1	3	4	5	7	8	6	11	9	10	12	13	14	16	17	15
21	21	22	23	25	26	24	20	18	19	3	4	5	7	8	6	2	0	1	12	13	14	16	17	15	11	9	10
22	22	23	21	26	24	25	18	19	20	4	5	3	8	6	7	0	1	2	13	14	12	17	15	16	9	10	11
23	23	21	22	24	25	26	19	20	18	5	3	4	6	7	8	1	2	0	14	12	13	15	16	17	10	11	9
24	24	25	26	19	20	18	23	21	22	6	7	8	1	2	0	5	3	4	15	16	17	10	11	9	14	12	13
25	25	26	24	20	18	19	21	22	23	7	8	6	2	0	1	3	4	5	16	17	15	11	9	10	12	13	14
26	26	24	25	18	19	20	22	23	21	8	6	7	0	1	2	4	5	3	17	15	16	9	10	11	13	14	12

nilpotent, identity element $e = 0$, $x^3 = e$, $y^3 = e$, $z^3 = e$, $xy = yx$, $xz = zx$, $yz = zy$

	e	x	x ²	y	xy	x ² y	y ²	xy ²	x ² y ²	z	xz	x ² z	yz	xyz	x ² yz	y ² z	xy ² z	x ² y ² z	z ²	xz ²	x ² z ²	yz ²	xyz ²	x ² yz ²	y ² z ²	xy ² z ²	x ² y ² z ²
Element	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24	25	26
Order	1	3	3	3	3	3	3	3	3	3	3	3	3	3	3	3	3	3	3	3	3	3	3	3	3	3	3

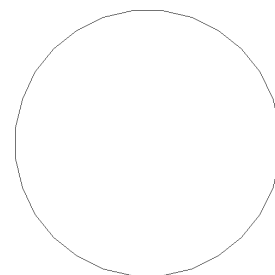
Cycle graph



Order 28 (4 groups)

	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24	25	26	27
0	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24	25	26	27
1	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24	25	26	27	0
2	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24	25	26	27	0	1
3	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24	25	26	27	0	1	2
4	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24	25	26	27	0	1	2	3
5	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24	25	26	27	0	1	2	3	4
6	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24	25	26	27	0	1	2	3	4	5
7	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24	25	26	27	0	1	2	3	4	5	6
8	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24	25	26	27	0	1	2	3	4	5	6	7
9	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24	25	26	27	0	1	2	3	4	5	6	7	8
10	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24	25	26	27	0	1	2	3	4	5	6	7	8	9
11	11	12	13	14	15	16	17	18	19	20	21	22	23	24	25	26	27	0	1	2	3	4	5	6	7	8	9	10
12	12	13	14	15	16	17	18	19	20	21	22	23	24	25	26	27	0	1	2	3	4	5	6	7	8	9	10	11
13	13	14	15	16	17	18	19	20	21	22	23	24	25	26	27	0	1	2	3	4	5	6	7	8	9	10	11	12
14	14	15	16	17	18	19	20	21	22	23	24	25	26	27	0	1	2	3	4	5	6	7	8	9	10	11	12	13
15	15	16	17	18	19	20	21	22	23	24	25	26	27	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14
16	16	17	18	19	20	21	22	23	24	25	26	27	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15
17	17	18	19	20	21	22	23	24	25	26	27	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16
18	18	19	20	21	22	23	24	25	26	27	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17
19	19	20	21	22	23	24	25	26	27	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18
20	20	21	22	23	24	25	26	27	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19
21	21	22	23	24	25	26	27	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20
22	22	23	24	25	26	27	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21
23	23	24	25	26	27	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22
24	24	25	26	27	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23
25	25	26	27	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24
26	26	27	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24	25
27	27	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24	25	26

Cycle graph

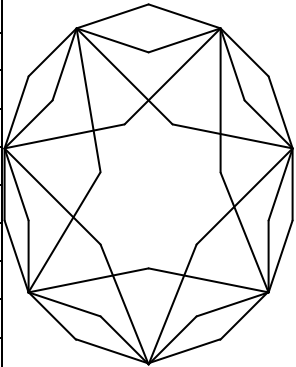


C_{28} , cyclic, identity element $e = 0$, $a^{28} = e$

	e	a	a ²	a ³	a ⁴	a ⁵	a ⁶	a ⁷	a ⁸	a ⁹	a ¹⁰	a ¹¹	a ¹²	a ¹³	a ¹⁴	a ¹⁵	a ¹⁶	a ¹⁷	a ¹⁸	a ¹⁹	a ²⁰	a ²¹	a ²²	a ²³	a ²⁴	a ²⁵	a ²⁶	a ²⁷
Element	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24	25	26	27
Order	1	28	14	28	7	28	14	4	7	28	14	28	7	28	2	28	7	28	14	28	7	4	14	28	7	28	14	28

	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24	25	26	27
0	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24	25	26	27
1	1	2	3	4	5	6	7	8	9	10	11	12	13	0	15	16	17	18	19	20	21	22	23	24	25	26	27	14
2	2	3	4	5	6	7	8	9	10	11	12	13	0	1	16	17	18	19	20	21	22	23	24	25	26	27	14	15
3	3	4	5	6	7	8	9	10	11	12	13	0	1	2	17	18	19	20	21	22	23	24	25	26	27	14	15	16
4	4	5	6	7	8	9	10	11	12	13	0	1	2	3	18	19	20	21	22	23	24	25	26	27	14	15	16	17
5	5	6	7	8	9	10	11	12	13	0	1	2	3	4	19	20	21	22	23	24	25	26	27	14	15	16	17	18
6	6	7	8	9	10	11	12	13	0	1	2	3	4	5	20	21	22	23	24	25	26	27	14	15	16	17	18	19
7	7	8	9	10	11	12	13	0	1	2	3	4	5	6	21	22	23	24	25	26	27	14	15	16	17	18	19	20
8	8	9	10	11	12	13	0	1	2	3	4	5	6	7	22	23	24	25	26	27	14	15	16	17	18	19	20	21
9	9	10	11	12	13	0	1	2	3	4	5	6	7	8	23	24	25	26	27	14	15	16	17	18	19	20	21	22
10	10	11	12	13	0	1	2	3	4	5	6	7	8	9	24	25	26	27	14	15	16	17	18	19	20	21	22	23
11	11	12	13	0	1	2	3	4	5	6	7	8	9	10	25	26	27	14	15	16	17	18	19	20	21	22	23	24
12	12	13	0	1	2	3	4	5	6	7	8	9	10	11	26	27	14	15	16	17	18	19	20	21	22	23	24	25
13	13	0	1	2	3	4	5	6	7	8	9	10	11	12	27	14	15	16	17	18	19	20	21	22	23	24	25	26
14	14	15	16	17	18	19	20	21	22	23	24	25	26	27	0	1	2	3	4	5	6	7	8	9	10	11	12	13
15	15	16	17	18	19	20	21	22	23	24	25	26	27	14	1	2	3	4	5	6	7	8	9	10	11	12	13	0
16	16	17	18	19	20	21	22	23	24	25	26	27	14	15	2	3	4	5	6	7	8	9	10	11	12	13	0	1
17	17	18	19	20	21	22	23	24	25	26	27	14	15	16	3	4	5	6	7	8	9	10	11	12	13	0	1	2
18	18	19	20	21	22	23	24	25	26	27	14	15	16	17	4	5	6	7	8	9	10	11	12	13	0	1	2	3
19	19	20	21	22	23	24	25	26	27	14	15	16	17	18	5	6	7	8	9	10	11	12	13	0	1	2	3	4
20	20	21	22	23	24	25	26	27	14	15	16	17	18	19	6	7	8	9	10	11	12	13	0	1	2	3	4	5
21	21	22	23	24	25	26	27	14	15	16	17	18	19	20	7	8	9	10	11	12	13	0	1	2	3	4	5	6
22	22	23	24	25	26	27	14	15	16	17	18	19	20	21	8	9	10	11	12	13	0	1	2	3	4	5	6	7
23	23	24	25	26	27	14	15	16	17	18	19	20	21	22	9	10	11	12	13	0	1	2	3	4	5	6	7	8
24	24	25	26	27	14	15	16	17	18	19	20	21	22	23	10	11	12	13	0	1	2	3	4	5	6	7	8	9
25	25	26	27	14	15	16	17	18	19	20	21	22	23	24	11	12	13	0	1	2	3	4	5	6	7	8	9	10
26	26	27	14	15	16	17	18	19	20	21	22	23	24	25	12	13	0	1	2	3	4	5	6	7	8	9	10	11
27	27	14	15	16	17	18	19	20	21	22	23	24	25	26	13	0	1	2	3	4	5	6	7	8	9	10	11	12

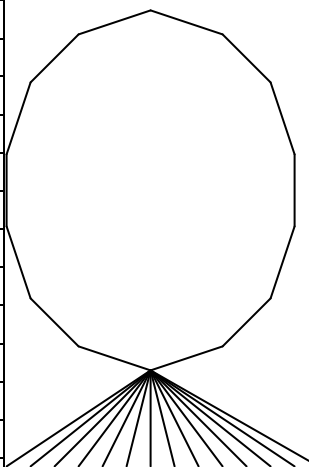
Cycle graph



$C_{14} \times C_2$, abelian, identity element $e = 0$, $a^{14} = e$, $b^2 = e$, $ba = ab$

	e	a	a ²	a ³	a ⁴	a ⁵	a ⁶	a ⁷	a ⁸	a ⁹	a ¹⁰	a ¹¹	a ¹²	a ¹³	b	ab	a ² b	a ³ b	a ⁴ b	a ⁵ b	a ⁶ b	a ⁷ b	a ⁸ b	a ⁹ b	a ¹⁰ b	a ¹¹ b	a ¹² b	a ¹³ b
Element	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24	25	26	27
Order	1	14	7	14	7	14	7	2	7	14	7	14	7	14	2	14	14	14	14	14	14	2	14	14	14	14	14	14

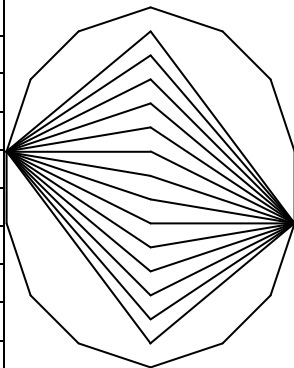
Cycle graph



D_{28} , dihedral, identity element $e = 0$, $a^{14} = e$, $b^2 = e$, $ba = a^{-1}b$

[illegible]

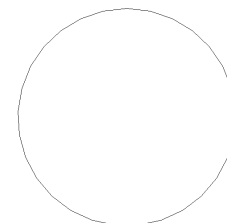
Cycle graph

[illegible]

Order 29 (1 group)

	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24	25	26	27	28
0	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24	25	26	27	28
1	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24	25	26	27	28	0
2	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24	25	26	27	28	0	1
3	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24	25	26	27	28	0	1	2
4	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24	25	26	27	28	0	1	2	3
5	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24	25	26	27	28	0	1	2	3	4
6	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24	25	26	27	28	0	1	2	3	4	5
7	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24	25	26	27	28	0	1	2	3	4	5	6
8	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24	25	26	27	28	0	1	2	3	4	5	6	7
9	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24	25	26	27	28	0	1	2	3	4	5	6	7	8
10	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24	25	26	27	28	0	1	2	3	4	5	6	7	8	9
11	11	12	13	14	15	16	17	18	19	20	21	22	23	24	25	26	27	28	0	1	2	3	4	5	6	7	8	9	10
12	12	13	14	15	16	17	18	19	20	21	22	23	24	25	26	27	28	0	1	2	3	4	5	6	7	8	9	10	11
13	13	14	15	16	17	18	19	20	21	22	23	24	25	26	27	28	0	1	2	3	4	5	6	7	8	9	10	11	12
14	14	15	16	17	18	19	20	21	22	23	24	25	26	27	28	0	1	2	3	4	5	6	7	8	9	10	11	12	13
15	15	16	17	18	19	20	21	22	23	24	25	26	27	28	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14
16	16	17	18	19	20	21	22	23	24	25	26	27	28	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15
17	17	18	19	20	21	22	23	24	25	26	27	28	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16
18	18	19	20	21	22	23	24	25	26	27	28	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17
19	19	20	21	22	23	24	25	26	27	28	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18
20	20	21	22	23	24	25	26	27	28	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19
21	21	22	23	24	25	26	27	28	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20
22	22	23	24	25	26	27	28	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21
23	23	24	25	26	27	28	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22
24	24	25	26	27	28	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23
25	25	26	27	28	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24
26	26	27	28	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24	25
27	27	28	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24	25	26
28	28	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24	25	26	27

Cycle graph



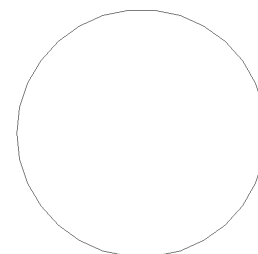
C_{29} , cyclic, identity element $e = 0$, $a^{29} = e$

[illegible]

Order 30 (4 groups)

	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24	25	26	27	28	29
0	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24	25	26	27	28	29
1	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24	25	26	27	28	29	0
2	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24	25	26	27	28	29	0	1
3	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24	25	26	27	28	29	0	1	2
4	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24	25	26	27	28	29	0	1	2	3
5	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24	25	26	27	28	29	0	1	2	3	4
6	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24	25	26	27	28	29	0	1	2	3	4	5
7	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24	25	26	27	28	29	0	1	2	3	4	5	6
8	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24	25	26	27	28	29	0	1	2	3	4	5	6	7
9	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24	25	26	27	28	29	0	1	2	3	4	5	6	7	8
10	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24	25	26	27	28	29	0	1	2	3	4	5	6	7	8	9
11	11	12	13	14	15	16	17	18	19	20	21	22	23	24	25	26	27	28	29	0	1	2	3	4	5	6	7	8	9	10
12	12	13	14	15	16	17	18	19	20	21	22	23	24	25	26	27	28	29	0	1	2	3	4	5	6	7	8	9	10	11
13	13	14	15	16	17	18	19	20	21	22	23	24	25	26	27	28	29	0	1	2	3	4	5	6	7	8	9	10	11	12
14	14	15	16	17	18	19	20	21	22	23	24	25	26	27	28	29	0	1	2	3	4	5	6	7	8	9	10	11	12	13
15	15	16	17	18	19	20	21	22	23	24	25	26	27	28	29	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14
16	16	17	18	19	20	21	22	23	24	25	26	27	28	29	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15
17	17	18	19	20	21	22	23	24	25	26	27	28	29	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16
18	18	19	20	21	22	23	24	25	26	27	28	29	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17
19	19	20	21	22	23	24	25	26	27	28	29	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18
20	20	21	22	23	24	25	26	27	28	29	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19
21	21	22	23	24	25	26	27	28	29	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20
22	22	23	24	25	26	27	28	29	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21
23	23	24	25	26	27	28	29	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22
24	24	25	26	27	28	29	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23
25	25	26	27	28	29	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24
26	26	27	28	29	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24	25
27	27	28	29	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24	25	26
28	28	29	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24	25	26	27
29	29	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24	25	26	27	28

Cycle graph



C_{30} , cyclic, identity element $e = 0$, $a^{30} = e$

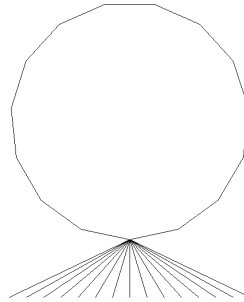
	e	a	a ²	a ³	a ⁴	a ⁵	a ⁶	a ⁷	a ⁸	a ⁹	a ¹⁰	a ¹¹	a ¹²	a ¹³	a ¹⁴	a ¹⁵	a ¹⁶	a ¹⁷	a ¹⁸	a ¹⁹	a ²⁰	a ²¹	a ²²	a ²³	a ²⁴	a ²⁵	a ²⁶	a ²⁷	a ²⁸	a ²⁹
Element	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24	25	26	27	28	29
Order	1	30	15	10	15	6	5	30	15	10	3	30	5	30	15	2	15	30	5	30	3	10	15	30	5	6	15	10	15	30

	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24	25	26	27	28	29
0	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24	25	26	27	28	29
1	1	2	3	4	5	6	7	8	9	10	11	12	13	14	0	16	17	18	19	20	21	22	23	24	25	26	27	28	29	15
2	2	3	4	5	6	7	8	9	10	11	12	13	14	0	1	17	18	19	20	21	22	23	24	25	26	27	28	29	15	16
3	3	4	5	6	7	8	9	10	11	12	13	14	0	1	2	18	19	20	21	22	23	24	25	26	27	28	29	15	16	17
4	4	5	6	7	8	9	10	11	12	13	14	0	1	2	3	19	20	21	22	23	24	25	26	27	28	29	15	16	17	18
5	5	6	7	8	9	10	11	12	13	14	0	1	2	3	4	20	21	22	23	24	25	26	27	28	29	15	16	17	18	19
6	6	7	8	9	10	11	12	13	14	0	1	2	3	4	5	21	22	23	24	25	26	27	28	29	15	16	17	18	19	20
7	7	8	9	10	11	12	13	14	0	1	2	3	4	5	6	22	23	24	25	26	27	28	29	15	16	17	18	19	20	21
8	8	9	10	11	12	13	14	0	1	2	3	4	5	6	7	23	24	25	26	27	28	29	15	16	17	18	19	20	21	22
9	9	10	11	12	13	14	0	1	2	3	4	5	6	7	8	24	25	26	27	28	29	15	16	17	18	19	20	21	22	23
10	10	11	12	13	14	0	1	2	3	4	5	6	7	8	9	25	26	27	28	29	15	16	17	18	19	20	21	22	23	24
11	11	12	13	14	0	1	2	3	4	5	6	7	8	9	10	26	27	28	29	15	16	17	18	19	20	21	22	23	24	25
12	12	13	14	0	1	2	3	4	5	6	7	8	9	10	11	27	28	29	15	16	17	18	19	20	21	22	23	24	25	26
13	13	14	0	1	2	3	4	5	6	7	8	9	10	11	12	28	29	15	16	17	18	19	20	21	22	23	24	25	26	27
14	14	0	1	2	3	4	5	6	7	8	9	10	11	12	13	29	15	16	17	18	19	20	21	22	23	24	25	26	27	28
15	15	29	28	27	26	25	24	23	22	21	20	19	18	17	16	0	14	13	12	11	10	9	8	7	6	5	4	3	2	1
16	16	15	29	28	27	26	25	24	23	22	21	20	19	18	17	1	0	14	13	12	11	10	9	8	7	6	5	4	3	2
17	17	16	15	29	28	27	26	25	24	23	22	21	20	19	18	2	1	0	14	13	12	11	10	9	8	7	6	5	4	3
18	18	17	16	15	29	28	27	26	25	24	23	22	21	20	19	3	2	1	0	14	13	12	11	10	9	8	7	6	5	4
19	19	18	17	16	15	29	28	27	26	25	24	23	22	21	20	4	3	2	1	0	14	13	12	11	10	9	8	7	6	5
20	20	19	18	17	16	15	29	28	27	26	25	24	23	22	21	5	4	3	2	1	0	14	13	12	11	10	9	8	7	6
21	21	20	19	18	17	16	15	29	28	27	26	25	24	23	22	6	5	4	3	2	1	0	14	13	12	11	10	9	8	7
22	22	21	20	19	18	17	16	15	29	28	27	26	25	24	23	7	6	5	4	3	2	1	0	14	13	12	11	10	9	8
23	23	22	21	20	19	18	17	16	15	29	28	27	26	25	24	8	7	6	5	4	3	2	1	0	14	13	12	11	10	9
24	24	23	22	21	20	19	18	17	16	15	29	28	27	26	25	9	8	7	6	5	4	3	2	1	0	14	13	12	11	10
25	25	24	23	22	21	20	19	18	17	16	15	29	28	27	26	10	9	8	7	6	5	4	3	2	1	0	14	13	12	11
26	26	25	24	23	22	21	20	19	18	17	16	15	29	28	27	11	10	9	8	7	6	5	4	3	2	1	0	14	13	12
27	27	26	25	24	23	22	21	20	19	18	17	16	15	29	28	12	11	10	9	8	7	6	5	4	3	2	1	0	14	13
28	28	27	26	25	24	23	22	21	20	19	18	17	16	15	29	13	12	11	10	9	8	7	6	5	4	3	2	1	0	14
29	29	28	27	26	25	24	23	22	21	20	19	18	17	16	15	14	13	12	11	10	9	8	7	6	5	4	3	2	1	0

D_{30} , dihedral, identity element $e = 0$, $a^{15} = e$, $b^2 = e$, $ba = a^{-1}b$

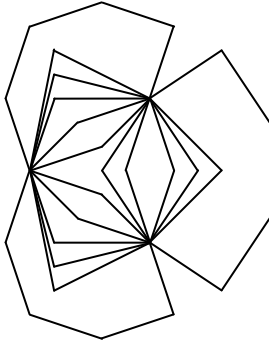
	e	a	a ²	a ³	a ⁴	a ⁵	a ⁶	a ⁷	a ⁸	a ⁹	a ¹⁰	a ¹¹	a ¹²	a ¹³	a ¹⁴	b	ab	a ² b	a ³ b	a ⁴ b	a ⁵ b	a ⁶ b	a ⁷ b	a ⁸ b	a ⁹ b	a ¹⁰ b	a ¹¹ b	a ¹² b	a ¹³ b	a ¹⁴ b
Element	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24	25	26	27	28	29
Order	1	15	15	5	15	3	5	15	15	5	3	15	5	15	15	2	2	2	2	2	2	2	2	2	2	2	2	2	2	2

Cycle graph



	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24	25	26	27	28	29
0	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24	25	26	27	28	29
1	1	2	3	4	0	6	7	8	9	5	11	12	13	14	10	16	17	18	19	15	21	22	23	24	20	26	27	28	29	25
2	2	3	4	0	1	7	8	9	5	6	12	13	14	10	11	17	18	19	15	16	22	23	24	20	21	27	28	29	25	26
3	3	4	0	1	2	8	9	5	6	7	13	14	10	11	12	18	19	15	16	17	23	24	20	21	22	28	29	25	26	27
4	4	0	1	2	3	9	5	6	7	8	14	10	11	12	13	19	15	16	17	18	24	20	21	22	23	29	25	26	27	28
5	5	9	8	7	6	0	4	3	2	1	15	19	18	17	16	10	14	13	12	11	25	29	28	27	26	20	24	23	22	21
6	6	5	9	8	7	1	0	4	3	2	16	15	19	18	17	11	10	14	13	12	26	25	29	28	27	21	20	24	23	22
7	7	6	5	9	8	2	1	0	4	3	17	16	15	19	18	12	11	10	14	13	27	26	25	29	28	22	21	20	24	23
8	8	7	6	5	9	3	2	1	0	4	18	17	16	15	19	13	12	11	10	14	28	27	26	25	29	23	22	21	20	24
9	9	8	7	6	5	4	3	2	1	0	19	18	17	16	15	14	13	12	11	10	29	28	27	26	25	24	23	22	21	20
10	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24	25	26	27	28	29	0	1	2	3	4	5	6	7	8	9
11	11	12	13	14	10	16	17	18	19	15	21	22	23	24	20	26	27	28	29	25	1	2	3	4	0	6	7	8	9	5
12	12	13	14	10	11	17	18	19	15	16	22	23	24	20	21	27	28	29	25	26	2	3	4	0	1	7	8	9	5	6
13	13	14	10	11	12	18	19	15	16	17	23	24	20	21	22	28	29	25	26	27	3	4	0	1	2	8	9	5	6	7
14	14	10	11	12	13	19	15	16	17	18	24	20	21	22	23	29	25	26	27	28	4	0	1	2	3	9	5	6	7	8
15	15	19	18	17	16	10	14	13	12	11	25	29	28	27	26	20	24	23	22	21	5	9	8	7	6	0	4	3	2	1
16	16	15	19	18	17	11	10	14	13	12	26	25	29	28	27	21	20	24	23	22	6	5	9	8	7	1	0	4	3	2
17	17	16	15	19	18	12	11	10	14	13	27	26	25	29	28	22	21	20	24	23	7	6	5	9	8	2	1	0	4	3
18	18	17	16	15	19	13	12	11	10	14	28	27	26	25	29	23	22	21	20	24	8	7	6	5	9	3	2	1	0	4
19	19	18	17	16	15	14	13	12	11	10	29	28	27	26	25	24	23	22	21	20	9	8	7	6	5	4	3	2	1	0
20	20	21	22	23	24	25	26	27	28	29	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19
21	21	22	23	24	20	26	27	28	29	25	1	2	3	4	0	6	7	8	9	5	11	12	13	14	10	16	17	18	19	15
22	22	23	24	20	21	27	28	29	25	26	2	3	4	0	1	7	8	9	5	6	12	13	14	10	11	17	18	19	15	16
23	23	24	20	21	22	28	29	25	26	27	3	4	0	1	2	8	9	5	6	7	13	14	10	11	12	18	19	15	16	17
24	24	20	21	22	23	29	25	26	27	28	4	0	1	2	3	9	5	6	7	8	14	10	11	12	13	19	15	16	17	18
25	25	29	28	27	26	20	24	23	22	21	5	9	8	7	6	0	4	3	2	1	15	19	18	17	16	10	14	13	12	11
26	26	25	29	28	27	21	20	24	23	22	6	5	9	8	7	1	0	4	3	2	16	15	19	18	17	11	10	14	13	12
27	27	26	25	29	28	22	21	20	24	23	7	6	5	9	8	2	1	0	4	3	17	16	15	19	18	12	11	10	14	13
28	28	27	26	25	29	23	22	21	20	24	8	7	6	5	9	3	2	1	0	4	18	17	16	15	19	13	12	11	10	14
29	29	28	27	26	25	24	23	22	21	20	9	8	7	6	5	4	3	2	1	0	19	18	17	16	15	14	13	12	11	10

Cycle graph

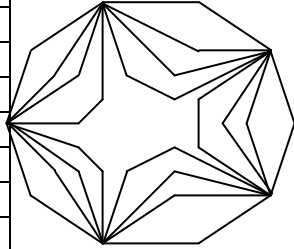


$D_{10} \times C_3$, solvable, identity element $e = 0$, $a^5 = e$, $b^2 = e$, $c^3 = e$, $ba = a^{-1}b$, $ca = ac$, $cb = bc$

	e	a	a ²	a ³	a ⁴	b	ab	a ² b	a ³ b	a ⁴ b	c	ac	a ² c	a ³ c	a ⁴ c	bc	abc	a ² bc	a ³ bc	a ⁴ bc	c ²	ac ²	a ² c ²	a ³ c ²	a ⁴ c ²	bc ²	abc ²	a ² bc ²	a ³ bc ²	a ⁴ bc ²	
Element	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24	25	26	27	28	29	
Order	1	5	5	5	5	2	2	2	2	2	3	15	15	15	15	6	6	6	6	6	6	3	15	15	15	15	6	6	6	6	6

	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24	25	26	27	28	29
0	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24	25	26	27	28	29
1	1	2	0	4	5	3	7	8	6	10	11	9	13	14	12	16	17	15	19	20	18	22	23	21	25	26	24	28	29	27
2	2	0	1	5	3	4	8	6	7	11	9	10	14	12	13	17	15	16	20	18	19	23	21	22	26	24	25	29	27	28
3	3	5	4	0	2	1	9	11	10	6	8	7	15	17	16	12	14	13	21	23	22	18	20	19	27	29	28	24	26	25
4	4	3	5	1	0	2	10	9	11	7	6	8	16	15	17	13	12	14	22	21	23	19	18	20	28	27	29	25	24	26
5	5	4	3	2	1	0	11	10	9	8	7	6	17	16	15	14	13	12	23	22	21	20	19	18	29	28	27	26	25	24
6	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24	25	26	27	28	29	0	1	2	3	4	5
7	7	8	6	10	11	9	13	14	12	16	17	15	19	20	18	22	23	21	25	26	24	28	29	27	1	2	0	4	5	3
8	8	6	7	11	9	10	14	12	13	17	15	16	20	18	19	23	21	22	26	24	25	29	27	28	2	0	1	5	3	4
9	9	11	10	6	8	7	15	17	16	12	14	13	21	23	22	18	20	19	27	29	28	24	26	25	3	5	4	0	2	1
10	10	9	11	7	6	8	16	15	17	13	12	14	22	21	23	19	18	20	28	27	29	25	24	26	4	3	5	1	0	2
11	11	10	9	8	7	6	17	16	15	14	13	12	23	22	21	20	19	18	29	28	27	26	25	24	5	4	3	2	1	0
12	12	13	14	15	16	17	18	19	20	21	22	23	24	25	26	27	28	29	0	1	2	3	4	5	6	7	8	9	10	11
13	13	14	12	16	17	15	19	20	18	22	23	21	25	26	24	28	29	27	1	2	0	4	5	3	7	8	6	10	11	9
14	14	12	13	17	15	16	20	18	19	23	21	22	26	24	25	29	27	28	2	0	1	5	3	4	8	6	7	11	9	10
15	15	17	16	12	14	13	21	23	22	18	20	19	27	29	28	24	26	25	3	5	4	0	2	1	9	11	10	6	8	7
16	16	15	17	13	12	14	22	21	23	19	18	20	28	27	29	25	24	26	4	3	5	1	0	2	10	9	11	7	6	8
17	17	16	15	14	13	12	23	22	21	20	19	18	29	28	27	26	25	24	5	4	3	2	1	0	11	10	9	8	7	6
18	18	19	20	21	22	23	24	25	26	27	28	29	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17
19	19	20	18	22	23	21	25	26	24	28	29	27	1	2	0	4	5	3	7	8	6	10	11	9	13	14	12	16	17	15
20	20	18	19	23	21	22	26	24	25	29	27	28	2	0	1	5	3	4	8	6	7	11	9	10	14	12	13	17	15	16
21	21	23	22	18	20	19	27	29	28	24	26	25	3	5	4	0	2	1	9	11	10	6	8	7	15	17	16	12	14	13
22	22	21	23	19	18	20	28	27	29	25	24	26	4	3	5	1	0	2	10	9	11	7	6	8	16	15	17	13	12	14
23	23	22	21	20	19	18	29	28	27	26	25	24	5	4	3	2	1	0	11	10	9	8	7	6	17	16	15	14	13	12
24	24	25	26	27	28	29	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23
25	25	26	24	28	29	27	1	2	0	4	5	3	7	8	6	10	11	9	13	14	12	16	17	15	19	20	18	22	23	21
26	26	24	25	29	27	28	2	0	1	5	3	4	8	6	7	11	9	10	14	12	13	17	15	16	20	18	19	23	21	22
27	27	29	28	24	26	25	3	5	4	0	2	1	9	11	10	6	8	7	15	17	16	12	14	13	21	23	22	18	20	19
28	28	27	29	25	24	26	4	3	5	1	0	2	10	9	11	7	6	8	16	15	17	13	12	14	22	21	23	19	18	20
29	29	28	27	26	25	24	5	4	3	2	1	0	11	10	9	8	7	6	17	16	15	14	13	12	23	22	21	20	19	18

Cycle graph



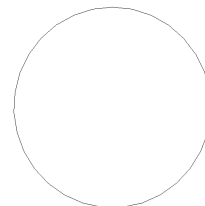
$D_6 \times C_5$, solvable, identity element $e = 0$, $a^3 = e$, $b^2 = e$, $c^5 = e$, $ba = a^{-1}b$, $ca = ac$, $cb = bc$

	e	a	a ²	b	ab	a ² b	c	ac	a ² c	bc	abc	a ² bc	c ²	ac ²	a ² c ²	bc ²	abc ²	a ² bc ²	c ³	ac ³	a ² c ³	bc ³	abc ³	a ² bc ³	c ⁴	ac ⁴	a ² c ⁴	bc ⁴	abc ⁴	a ² bc ⁴
Element	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24	25	26	27	28	29
Order	1	3	3	2	2	2	5	15	15	10	10	10	5	15	15	10	10	10	5	15	15	10	10	10	5	15	15	10	10	10

Order 31 (1 group)

	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24	25	26	27	28	29	30
0	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24	25	26	27	28	29	30
1	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24	25	26	27	28	29	30	0
2	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24	25	26	27	28	29	30	0	1
3	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24	25	26	27	28	29	30	0	1	2
4	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24	25	26	27	28	29	30	0	1	2	3
5	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24	25	26	27	28	29	30	0	1	2	3	4
6	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24	25	26	27	28	29	30	0	1	2	3	4	5
7	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24	25	26	27	28	29	30	0	1	2	3	4	5	6
8	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24	25	26	27	28	29	30	0	1	2	3	4	5	6	7
9	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24	25	26	27	28	29	30	0	1	2	3	4	5	6	7	8
10	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24	25	26	27	28	29	30	0	1	2	3	4	5	6	7	8	9
11	11	12	13	14	15	16	17	18	19	20	21	22	23	24	25	26	27	28	29	30	0	1	2	3	4	5	6	7	8	9	10
12	12	13	14	15	16	17	18	19	20	21	22	23	24	25	26	27	28	29	30	0	1	2	3	4	5	6	7	8	9	10	11
13	13	14	15	16	17	18	19	20	21	22	23	24	25	26	27	28	29	30	0	1	2	3	4	5	6	7	8	9	10	11	12
14	14	15	16	17	18	19	20	21	22	23	24	25	26	27	28	29	30	0	1	2	3	4	5	6	7	8	9	10	11	12	13
15	15	16	17	18	19	20	21	22	23	24	25	26	27	28	29	30	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14
16	16	17	18	19	20	21	22	23	24	25	26	27	28	29	30	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15
17	17	18	19	20	21	22	23	24	25	26	27	28	29	30	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16
18	18	19	20	21	22	23	24	25	26	27	28	29	30	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17
19	19	20	21	22	23	24	25	26	27	28	29	30	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18
20	20	21	22	23	24	25	26	27	28	29	30	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19
21	21	22	23	24	25	26	27	28	29	30	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20
22	22	23	24	25	26	27	28	29	30	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21
23	23	24	25	26	27	28	29	30	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22
24	24	25	26	27	28	29	30	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23
25	25	26	27	28	29	30	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24
26	26	27	28	29	30	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24	25
27	27	28	29	30	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24	25	26
28	28	29	30	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24	25	26	27
29	29	30	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24	25	26	27	28
30	30	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24	25	26	27	28	29

Cycle graph



C_{31} , cyclic, identity element $e = 0$, $a^{31} = e$

[illegible]

Summary

Groups of order 24 elements

Group Number	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15
Order 2	1	3	7	13	15	5	7	9	7	1	3	1	1	9	1
Order 3	2	2	2	2	2	2	2	8	8	2	2	2	2	2	8
Order 4	2	4	0	2	0	2	8	6	0	6	12	14	2	6	6
Order 6	2	6	14	2	6	10	2	0	8	2	6	2	2	6	8
Order 8	4	0	0	0	0	0	0	0	0	0	0	0	12	0	0
Order 12	4	8	0	4	0	4	4	0	0	12	0	4	4	0	0
Order 24	8	0	0	0	0	0	0	0	0	0	0	0	0	0	0
GAP serial	2	9	15	6	14	10	5	12	13	11	7	4	1	8	3

Thus, of course that it is true that each group of order 24 elements has got some different element order sequence from every other non-isomorphic group of that same order itself!

Groups of order 16 elements

Group Number	1	2	3	4	5	6	7	8	9	10	11	12	13	14
Order 2	1	3	3	15	7	9	11	1	3	5	3	3	7	7
Order 4	2	12	4	0	8	2	4	10	12	6	4	12	8	8
Order 8	4	0	8	0	0	4	0	4	0	4	8	0	0	0
Order 16	8	0	0	0	0	0	0	0	0	0	0	0	0	0
GAP serial	1	2	5	14	10	7	11	9	12	8	6	4	3	13

Some more of that extra terms for study upon that group theory concepts

If H is a subgroup of group G , and then a is an element of G , then the left coset aH is defined by set of all elements $a.h$ for each element h from within H . The right coset Ha is given up by set of all elements $h.a$ for each element h from within H . These left cosets and right cosets are subsets of elements of that group G itself. In any Abelian group, each left coset coincides with its corresponding right coset. The number of distinct left or right cosets of H in G is called as index of H in G . If H is normal subgroup of that group G , then set of all left cosets of G forms a group with respect to multiplication of left coset and is defined as $(aH)(bH) = (ab)H$, and is known as that factor group or that quotient group G/H . This same thing is indeed true for that right coset as well, with $(Ha)(Hb) = H(ab)$. The quotient group that is being obtained by using left coset, and that obtained by using right coset are both always being isomorphic to each other.

If G and H are two groups with same number of elements (either finite or infinite), then G and H are homomorphic to each other, if there exists some function f from elements of G to H , such that for all pairs of elements a, b from within G , $f(a.b) = f(a).f(b)$ holds out. The kernel of homomorphism f from group G to group H is the set of all elements of G that are being mapped up onto the identity element e of G , by using that function f itself.

In order words, that is, kernel of homomorphism f is equal to $\langle a \text{ belongs to } G, \text{ such that } f(a) = e \rangle$